

# The Crab and other Animals

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Most of you!



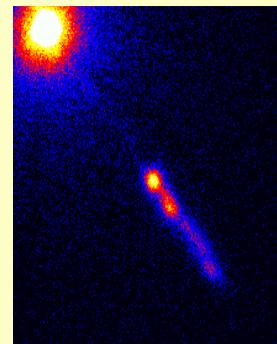
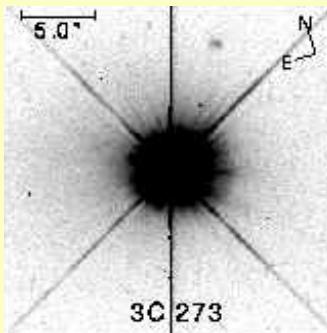
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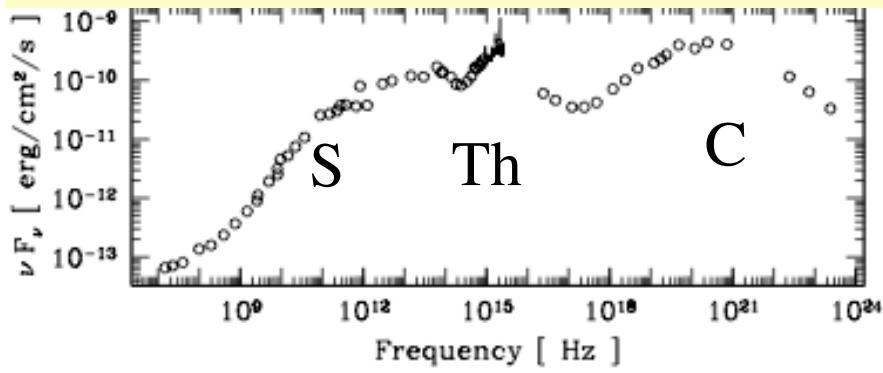
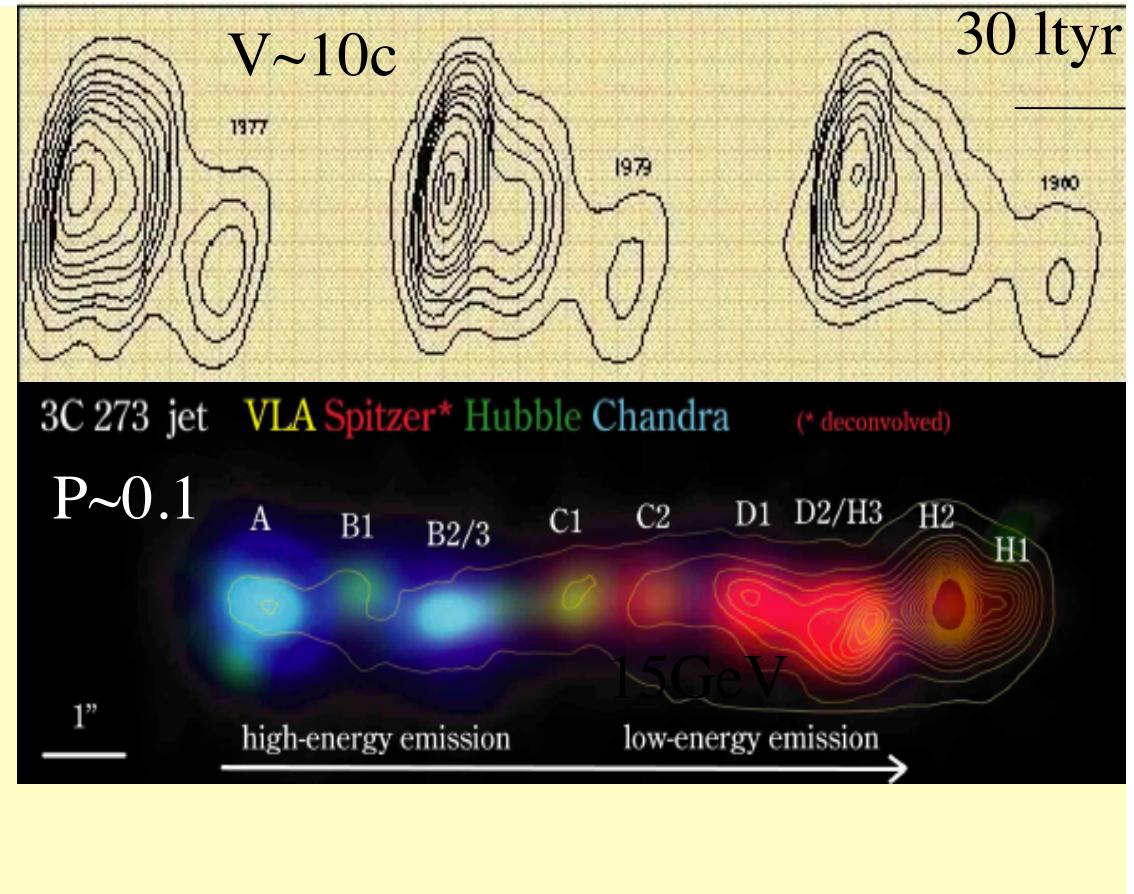
# Outline

- Observations of compact flares
- Crab Nebula - an introduction
- Crab Nebula - particle acceleration
- Knots, tangles and spheromaks
- Evolution, acceleration and radiation
- Instability and runaway acceleration
- MHD and kinetic simulations
- Summary

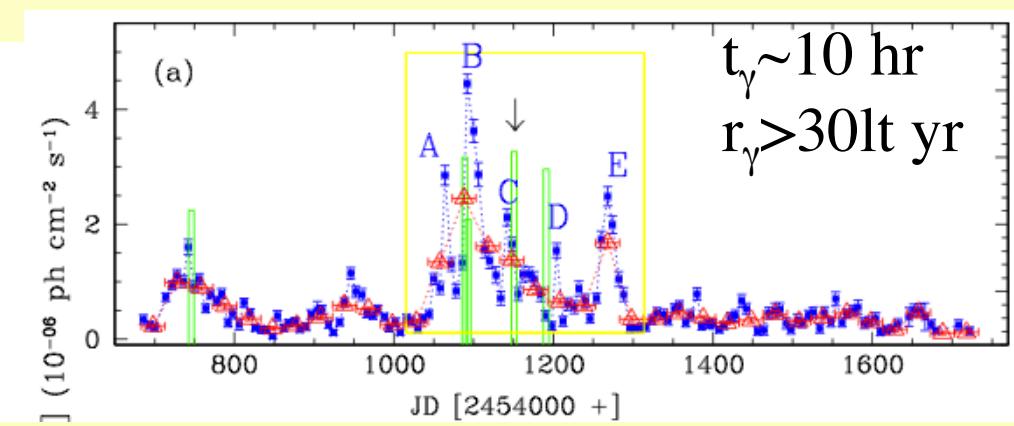
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$L_Q \sim 10 L_{\text{gal}} \sim 3 \times 10^{12} L_{\text{sun}}$   
 $M_{\text{BH}} \sim 10^9 M_{\text{sun}} \sim 1.5 \text{ lt hr}$



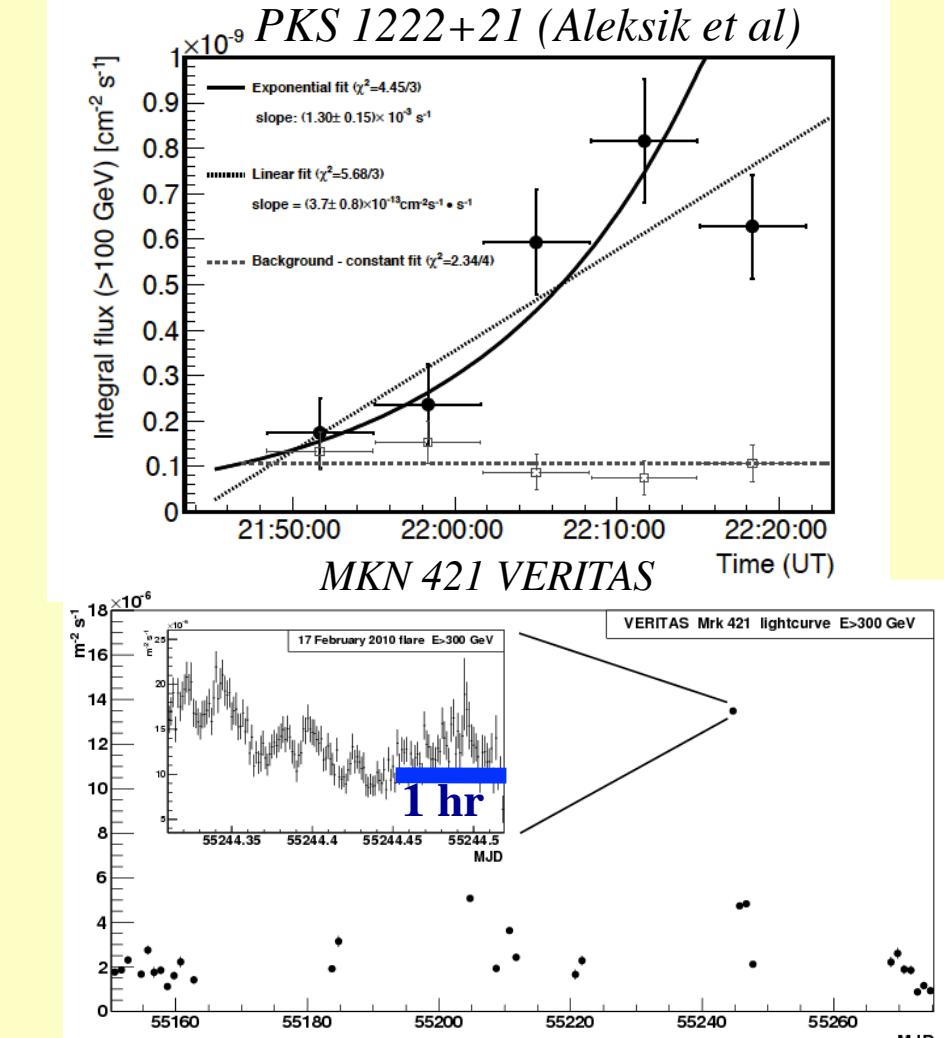
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$3$   
 $25 \text{ kpc}$

# TeV variation

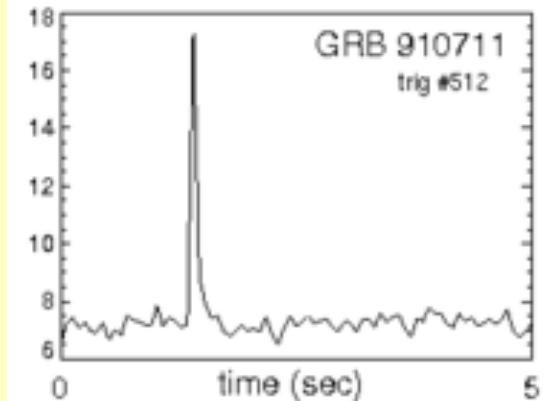
- M87
  - 1 day
- PKS 1222+21
  - 10 min
- MKN 501
  - 5 min?
- PKS 2155-304
  - 2 min?
- MKN 421
  - Radio –TeV hr - min? 20 X



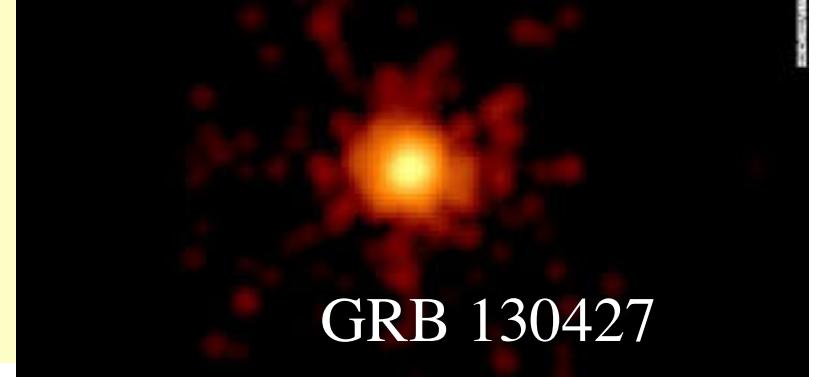
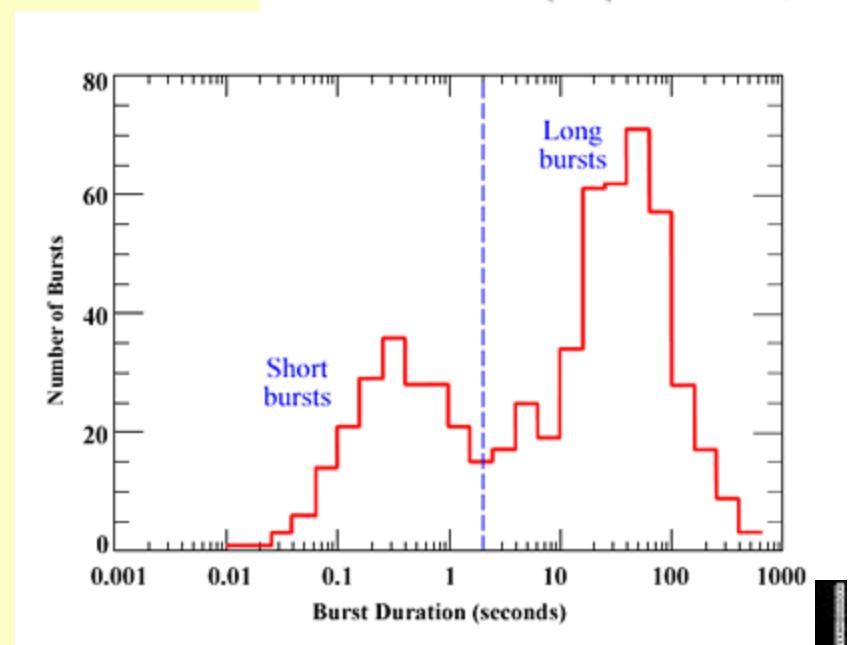
$$E_{\text{rad}} \gg P(ct_{\text{var}})^3$$

# Gamma Ray Bursts

- Long burst core collapse SN
  - Jets with  $\gamma \sim 1000$ ?
  - Rapid variability; high efficiency
- Short bursts NS-NS??
  - Hard spectrum
  - Small SFR/no SN
  - Delayed X-ray emission
  - Fermi-GBM statistics
  - Tidal capture events?
  - Gravitational radiation
  - Neutrinos



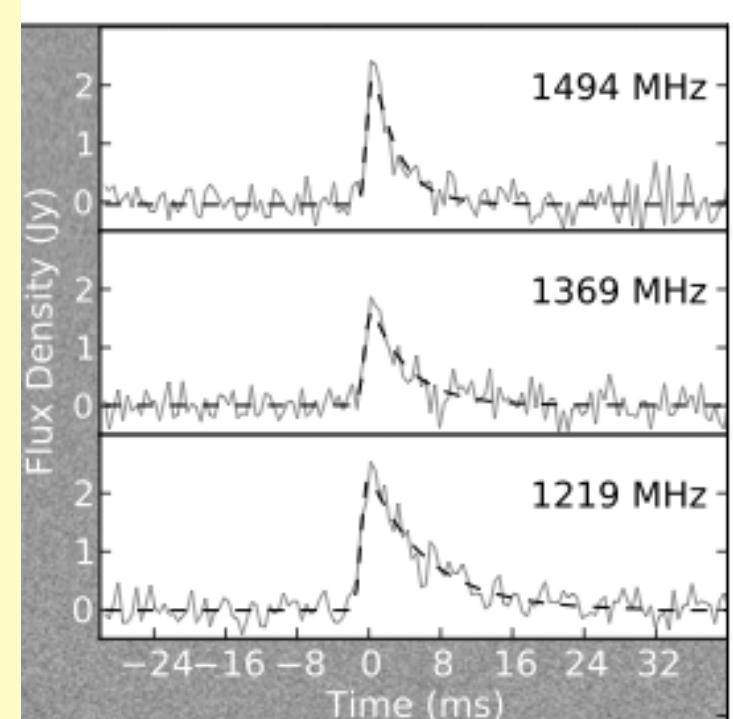
GRB



# Fast Radio Bursts

- New population of apparently high redshift radio transients
- Identifications unknown but dispersion and scattering consistent with cosmological origin
- $\sim 10^{39}$  erg radio emission in ms
- $\sim$  one every five minutes
- Many possible sources: WD-WD, NS-NS, NS-BH mergers, magnetar explosions...

(Lorimer et al 2007, Thornton et al 2013)

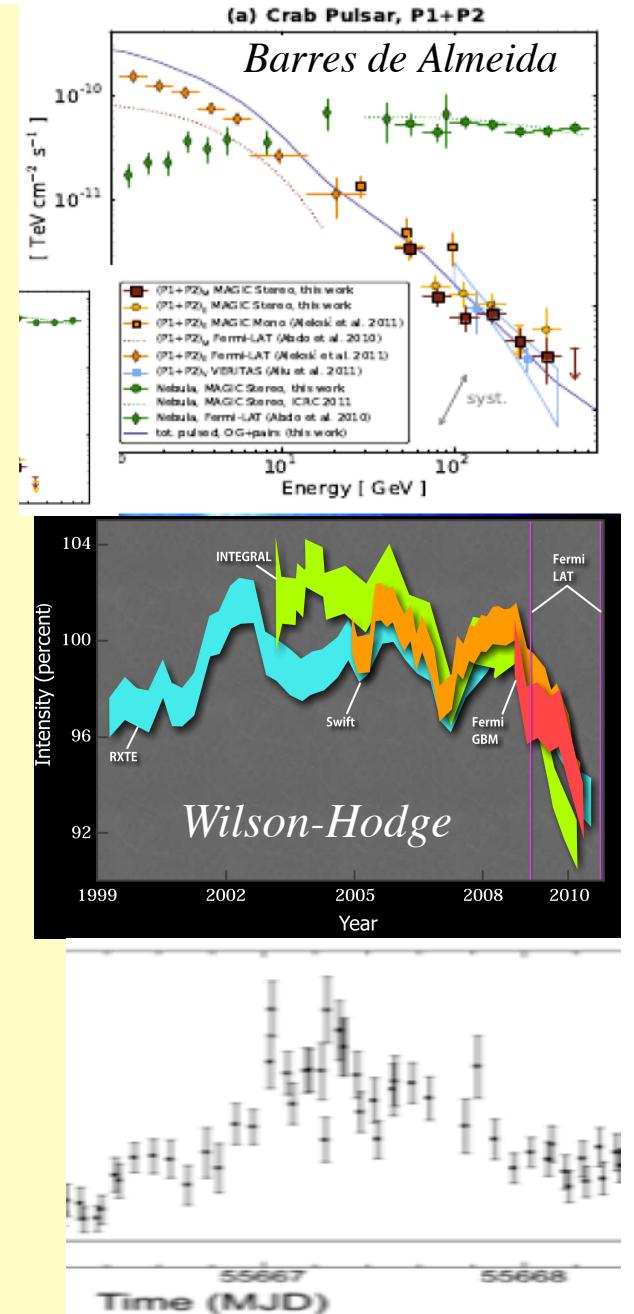


# Crab Pulsar and Nebula



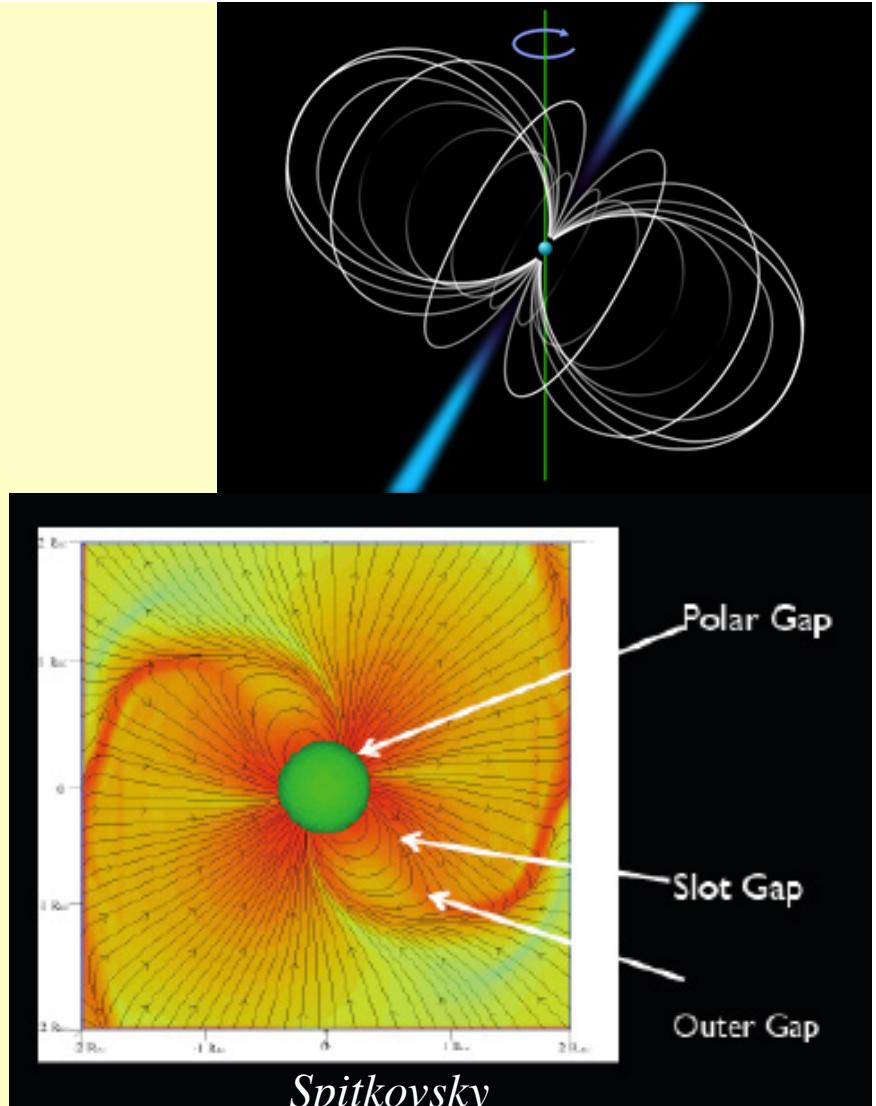
# Three Surprises

- **Crab pulsing at 400 GeV**
  - Curvature radiation to  $\sim$  GeV only
  - Mind the gap
- **Secular decline in Crab flux**
  - 30 yr timescale in 1000yr source
  - Unit!
- **$\sim$ 400MeV Crab flares**
  - 1-10hr variation in 10 lt yr nebula
  - Extreme particle acceleration

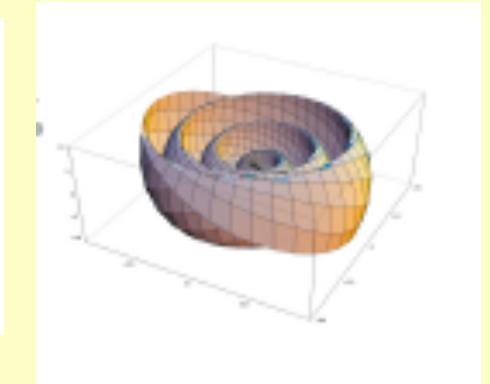
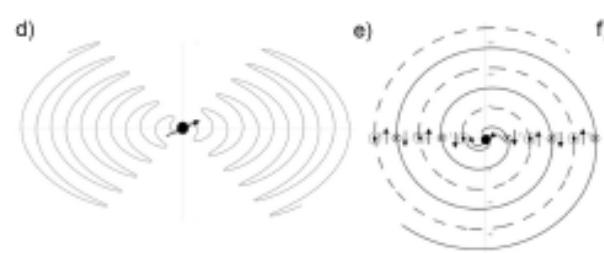
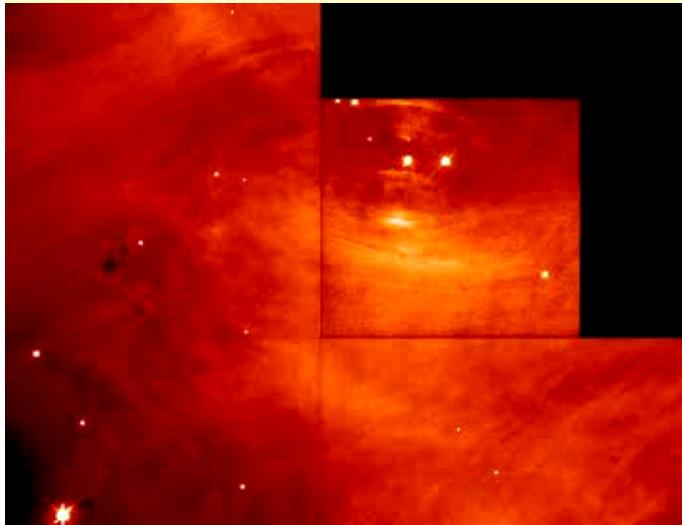


# Crab Pulsar

- Discovered in 1968
  - Turning point in history of astronomy
  - Predicted by Pacini
- $1.4 M_{\text{sun}}$ , 12km neutron star
  - 30 Hz spin frequency
  - Light cylinder  $R_L = c/\Omega \sim 100 R_{\text{NS}}$
  - 100MHz – 400 GeV pulsation
  - Steady slow down
  - 200 MT surface field; 70° inclination?
  - $\sim 50\text{PV}$ ;  $300\text{TA}$ ;  $2 \times 10^{31}\text{W} \sim -I\Omega\Omega'$
- Implications of 400GeV pulses
  - Inverse Compton scattering (*Lyutikov*)
  - Dissipation  $R_L$ ? (*Aharonian*)



# Restless Crab Nebula



*Spitkovsky*

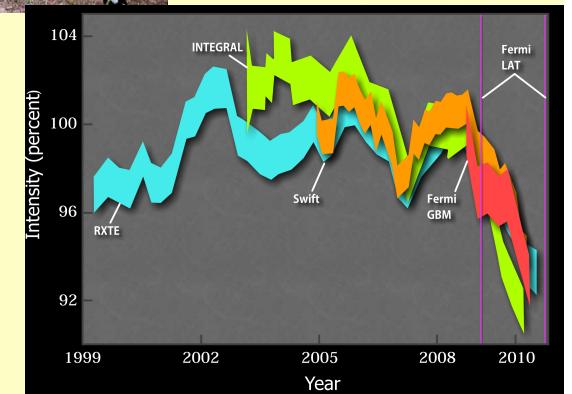
Arons, Komissarov

- What is the nature of the outflow?
  - EM,  $e^+/e^-$ , p, Fe
  - What is  $\sigma = B^2/\mu_0 n \gamma m c^2$ ?
- Where do currents close?
  - Wind is current not voltage source
  - Current is AC **and** DC
  - Stripes and toroidal
- Are currents “industrious” or “prodigal”?
  - $J \times B$  or  $-E \cdot j$



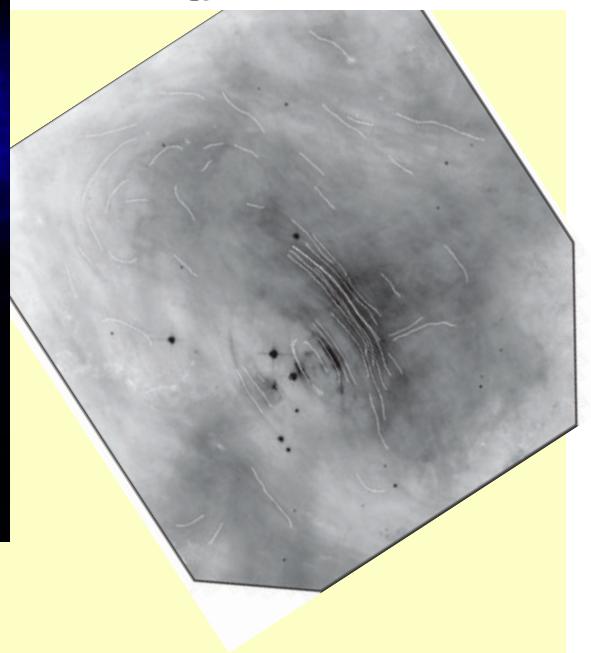
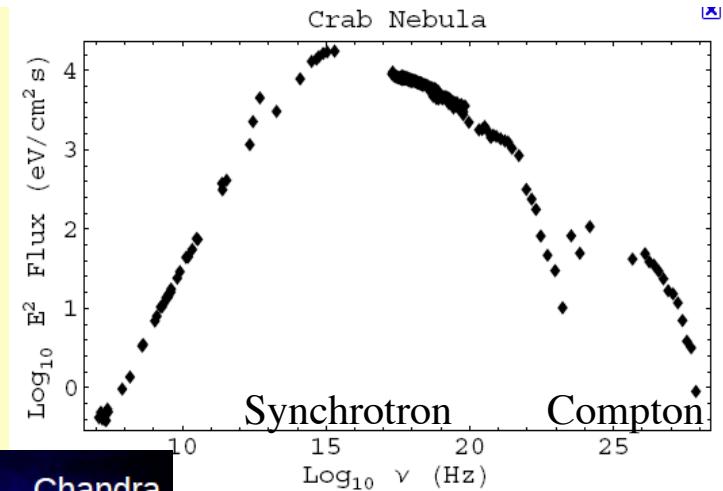
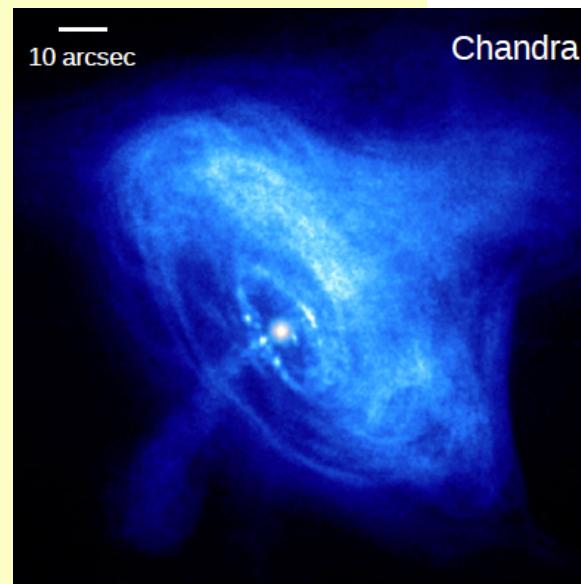
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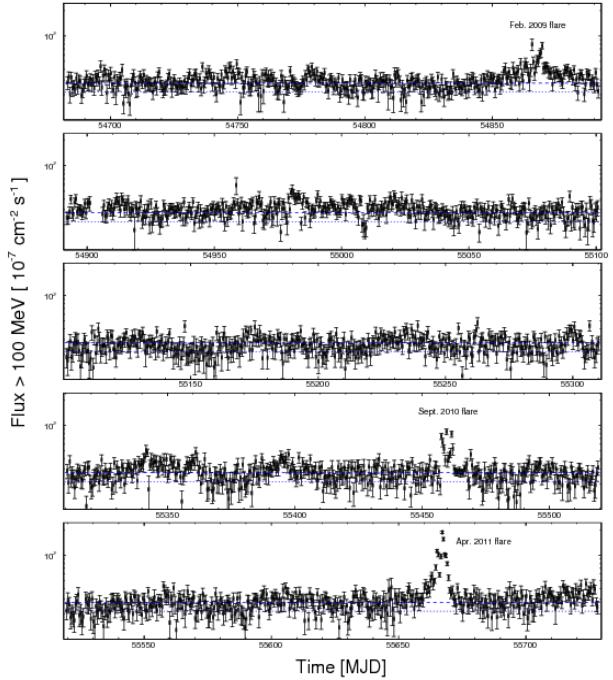
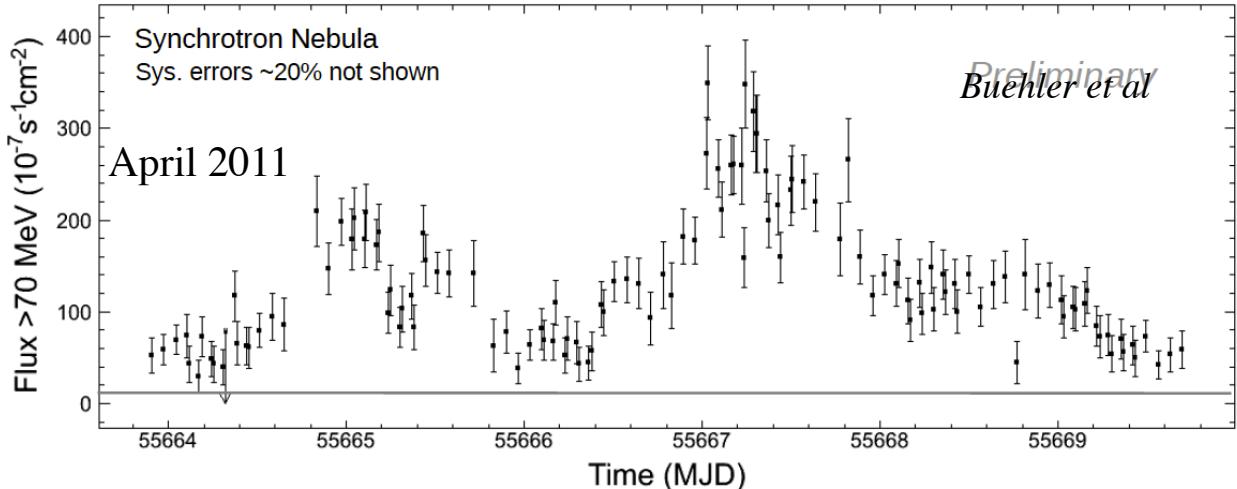


# Modeling the Nebula

- Spectral fitting
  - Synchrotron:Compton  $\Rightarrow B < B_{eq}$ 
    - Inhomogeneous
- Flux supply
  - No dissipation
    - $\sigma < 0.001$ ,  $\gamma \sim 10^6$
  - Dissipation
    - $\sigma < 100$
    - Axis
      - Jet
      - Kink instability (*Begelman, Lyubarsky Komissarov*)
    - Equator
      - Torus
      - CurrentSheet (*Arons*)



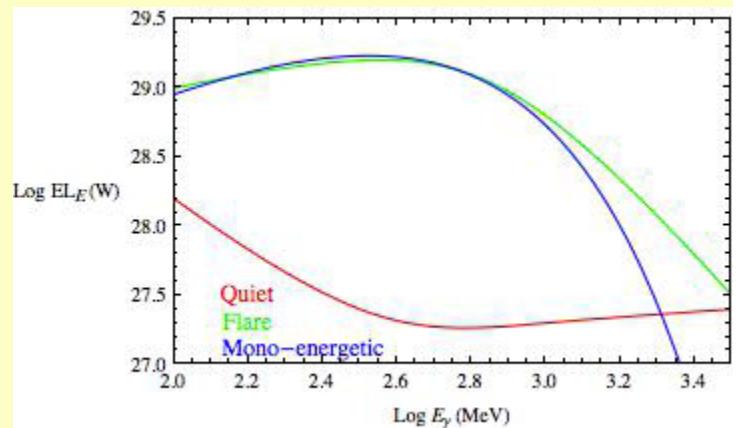
# Flaring behavior



- **1-10hr timescale depending on definition**
  - Are these flares or end of power spectrum?
- **Only seen at 0.1-1 GeV energy** Weisskopf , Max, Bietenholz...
- No associated ROX variation yet
- **Peak power~0.01 L<sub>neb</sub>**
  - Need >0.1 sterad if from wind
- **Flare energy ~ U<sub>neb</sub> x 10<sup>4</sup> ltd<sup>3</sup>**
  - Need overpressured region or beaming

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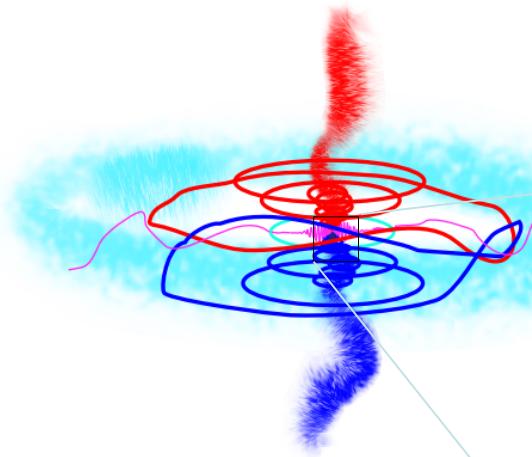
# Turbulence Spectrum

- **Top Down**
  - Large loops from wind ->small loops
    - cf fluid turbulence
  - Flares are “intermittency”
- **Bottom Up**
  - Tangled field from wind
    - Variable radial velocity
  - Reconnect, rearrange
    - Unknot, untangle?
- **How do we dissipate the flux?**

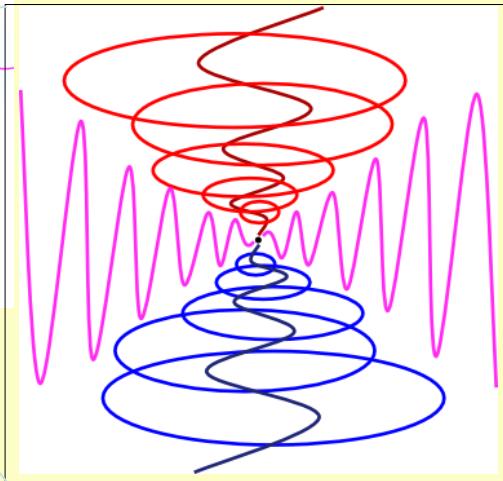
# Crab Pulsar and Nebula

- **Pulsar:** ~50 PV, ~300TA  $\sim 2 \times 10^{31} W$
- **Nebula:**  $L_{10\text{eV}} \sim 10^{31} W$ ,  $\sim 10^{42} J$ ,  $\sim 1000 \text{yr}$
- **Synch:**  $B \sim 100 \text{nT}$ ,  $E_{10\text{eV}} \sim 1 \text{TeV}$ ,  $t_{\text{cool}} \sim 10 \text{ yr}$
- **UV-X:**  $N_E \sim E^{-3.4}$ ;  $S_E \sim E^{-2.4}$
- **R-IR:**  $N_E \sim S_E \sim E^{-1.6}$
- **$\gamma$ -ray:**  $10^{27} \rightarrow 10^{29} W$
- **Flare:**  $E_{300\text{MeV}} \sim 3 \text{PeV}$ ;  $r_L \sim 1 \text{t day}$   $\phi_{\text{cool}} \sim 0.2$

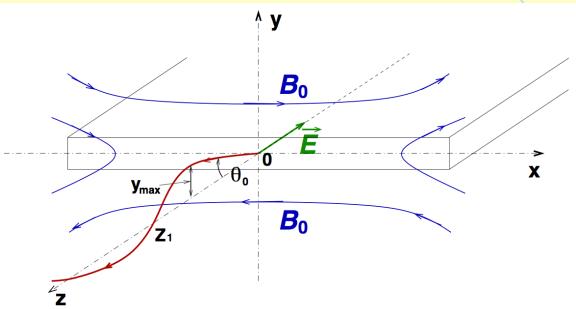
$\sigma?$     $\beta?$



## Magnetic Flux Removal?

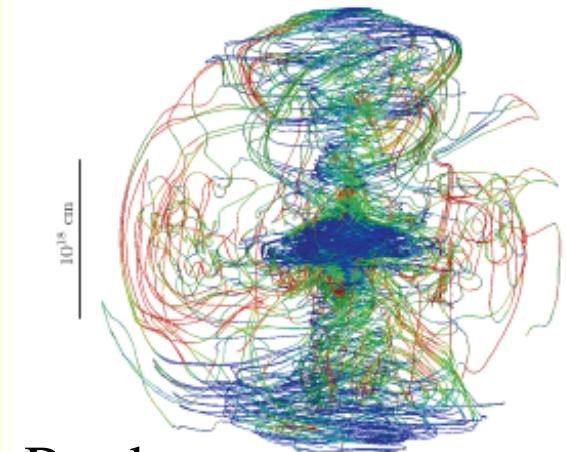
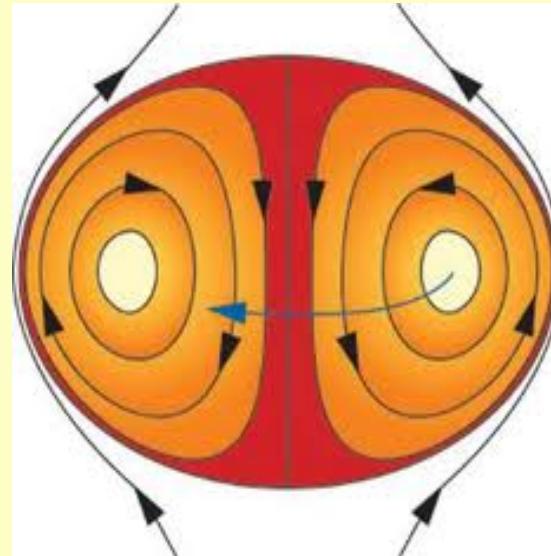


Spheromak

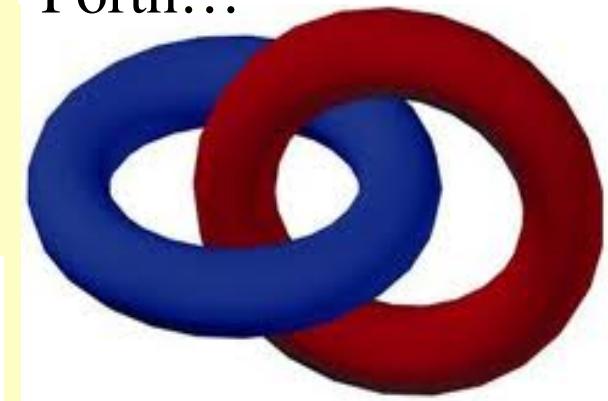


Reconnection

Steady reconnection  
of braided loops  
of magnetic flux at  
all latitude create  
complex network of  
linked islands/knots...



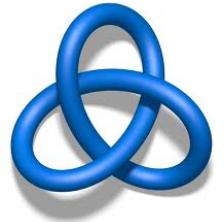
Porth...



$$K \equiv \int \mathbf{A} \cdot \mathbf{B} dV = 2\phi\psi$$

Woltjer/Taylor  
Overpressured  
Persistent

# Knots and Tangles

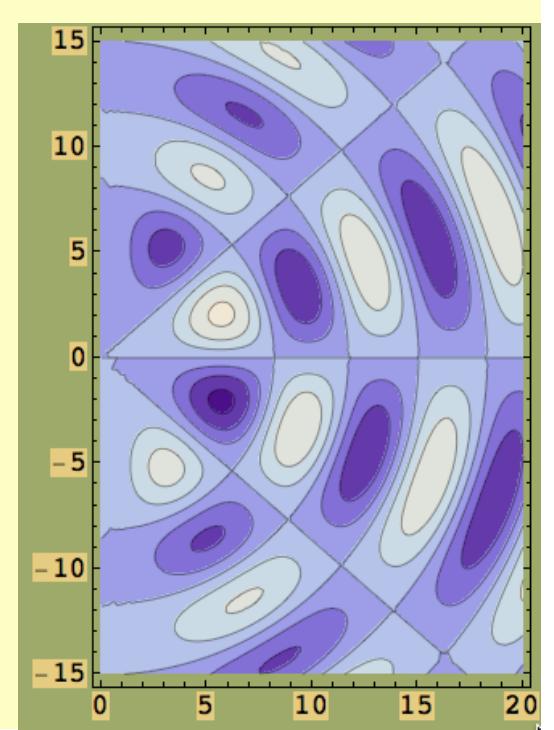
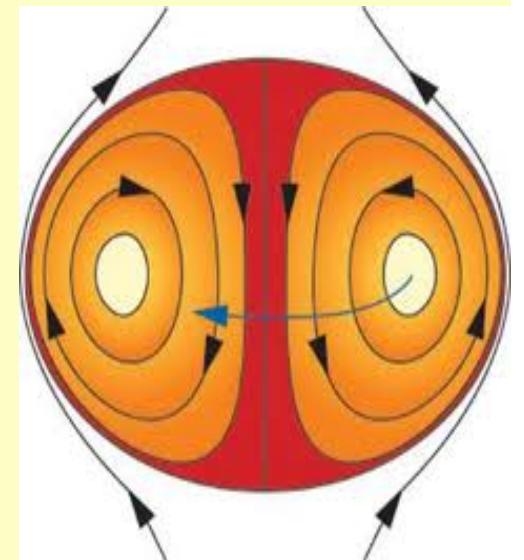
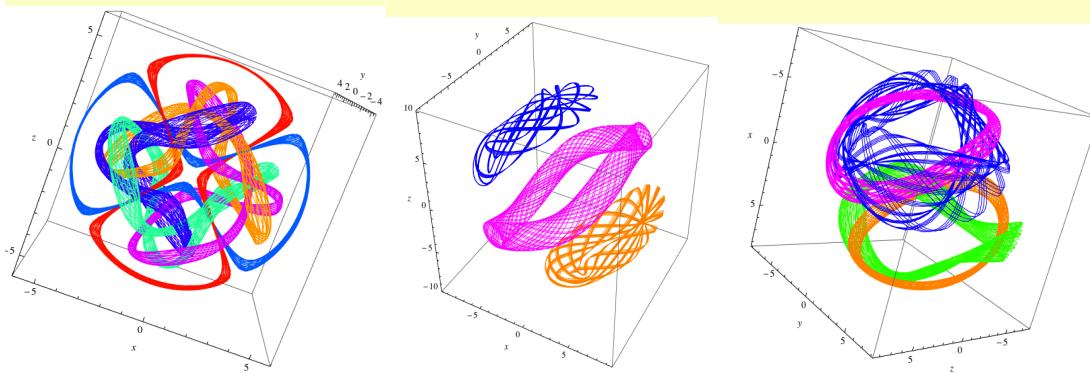
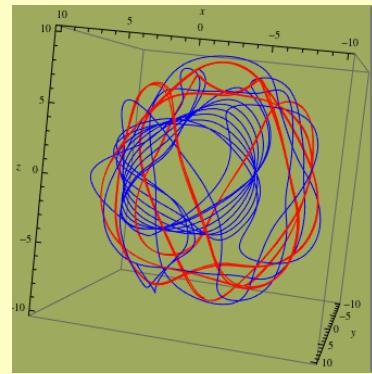
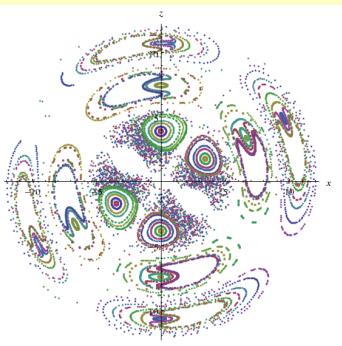


- Knot (eg trefoil)
  - Describable by polynomials
    - Tait, Alexander, Jones...:  $t+t^3-t^4$
  - Require reconnection to create and destroy
    - Slow
- Tangle/tonk/unknot (eg slip knot)
  - Can become unstable and transition to lower energy configuration at speed of light
  - Create  $E > c B$ ? and runaway electron acceleration throughout extended volume
  - Magnetic energy  $\rightarrow \gamma$ -rays
  - Followed by implosion, chain reaction?

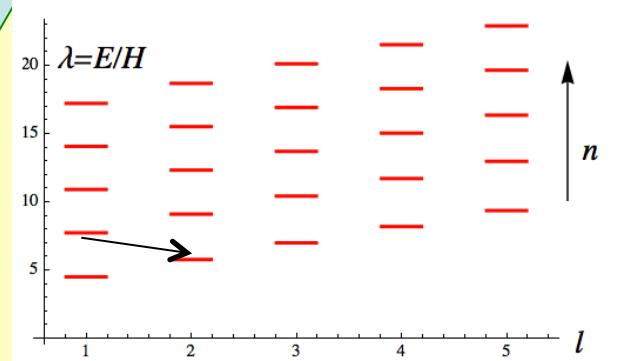
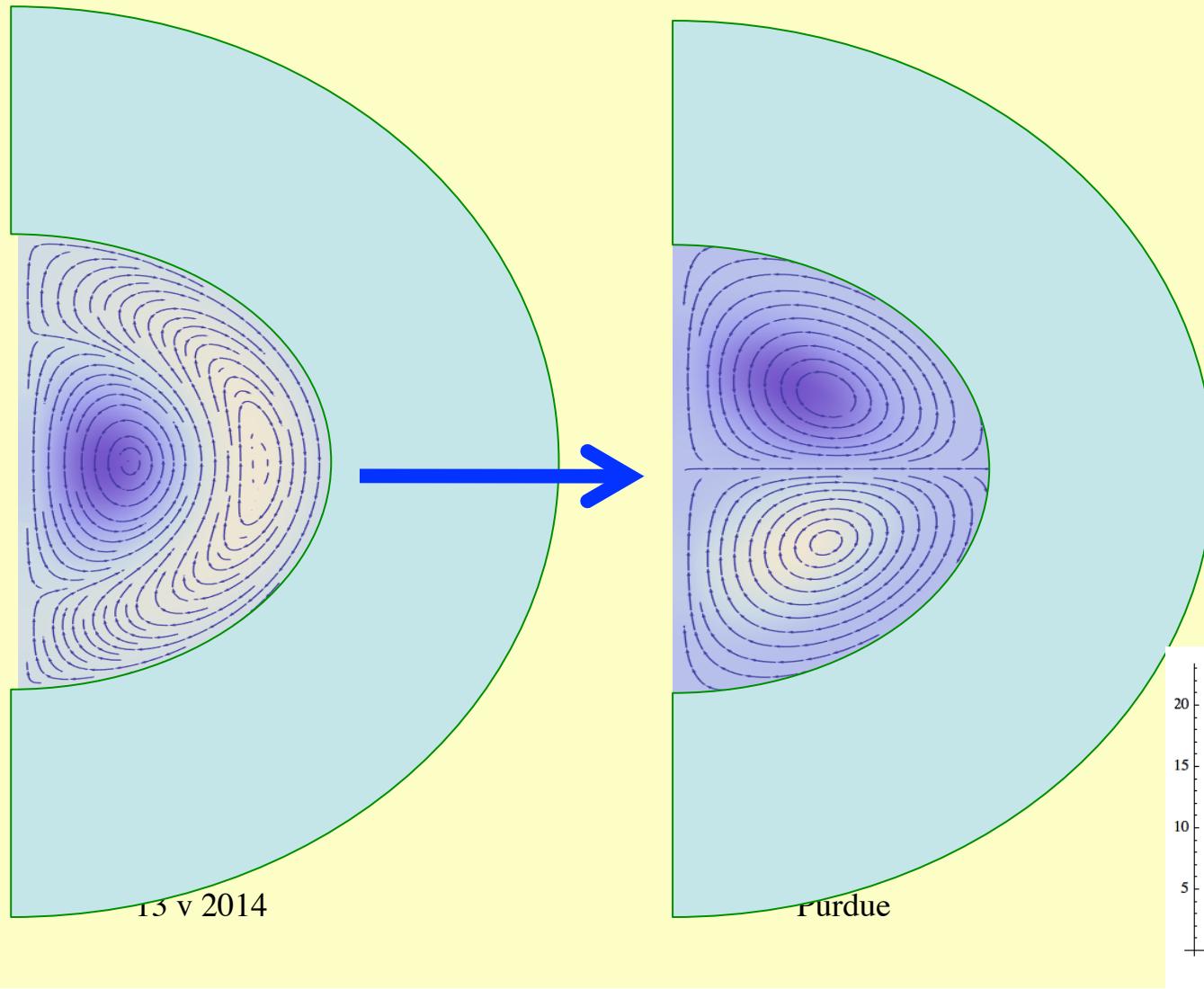


# Force-Free Equilibria

- Family of spheromak solutions
  - $n, l, m, s!$
- Magnetic ropes – field confined to nested surfaces
- Chaotic field
- Is this robust in the presence of turbulence?



# Permitted Transition



# Aside on MHD

- Most discussions assume isotropic pressure
  - $P \sim n^\gamma$ ;  $\gamma = 4/3, 5/3$ , for ER, NR
  - Appropriate when collisional
- Nebula plasma is strongly collisionless

- Pressure anisotropic.  $P_{\parallel}, P_{\perp}$  when  $r_L \ll L$

$$\rho \mathbf{a} = \rho \mathbf{g} - \nabla \cdot \mathbf{P} + \rho_e \mathbf{E} + \mathbf{j} \times \mathbf{B},$$

$$\Rightarrow \mathbf{j}_{\perp} = \frac{P_{\parallel} B \times (B \cdot \nabla) B}{B^4} - \left[ \nabla \times \left( \frac{P_{\perp} B}{B^2} \right) \right]_{\perp} + \frac{P_{\perp} B \times \nabla B}{B^3} + \frac{\rho_e E \times B}{B^2} + \rho \frac{g \times B}{B^2} + \rho \frac{a \times B}{B^2}$$

curvature

magnetization

gradient

ExB

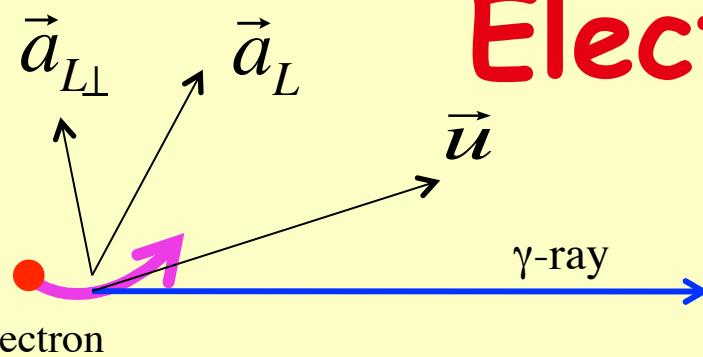
gravity acceleration

- $P_{\parallel} \sim n^2 B^{-1}$ ;  $P_{\perp} \sim n B^{1/2}$  ... changes dynamics, stability...

- When  $r_L \sim r$ , compose current from orbits (cf stars!)

# Particle Acceleration/Dissipation

- Spheromak+resistance
  - $U_{mag}$  -> heated plasma -> radiation
  - Isochoric vs isobaric
  - Implosion?
- Collision frequency
  - Electrostatic waves from counterstreaming pairs
  - Gyroresonant scattering
  - Firehose modes
  - Mirroring
- Low pitch angle particles may runaway
  - dominate dissipation?
  - $E \sim B R / t \sim (mc/e)d\gamma/dt \Rightarrow \gamma mc^2 \rightarrow eZ_0 I \sim 3 B_{-7} R_{14} \text{ PeV}$



# Electrodynamics

- 0.011 photons emitted in turning through angle  $\gamma^{-1}$
- Classical not quantum process

$$\frac{d\vec{u}}{dt} = \vec{a}_L - \frac{2r_e}{3c}\gamma^2 a_{L\perp}^2 \hat{\vec{u}}, \quad \frac{d\vec{x}}{dt} = \hat{\vec{u}}$$

$$\vec{a}_L = \frac{e}{m} \left( \frac{\vec{E}}{c} + \hat{\vec{u}} \times \vec{B} \right)$$

$$a_{L\perp}(\vec{x}, \hat{\vec{u}}) = \frac{e}{m} B_e = \frac{e}{m} \left[ B_\perp^2 + \left( \frac{E_\perp}{c} \right)^2 - 2 \frac{\vec{E} \times \vec{B} \cdot \hat{\vec{u}}}{c} \right]^{1/2}$$

- $\gamma_9^2 B_{e-7} = 16(E_\gamma/400\text{MeV})$ ;  $r_L = 1.7 \times 10^{13} \gamma_9 B_{e-7}^{-1} \text{ m}$
- Radiation reaction dominates when  $E_\gamma > \alpha^{-1} m_e c^2 \sim 70 \text{ MeV}$ ;  $\lambda < r_e$
- If only uniform magnetic field, electron cools in  $12^\circ$
- If add electric field,  $E > 5cB$  to avoid energy loss
- $E > cB$  in all frames.

Need 2 PeV electrons  
in a 100nT field

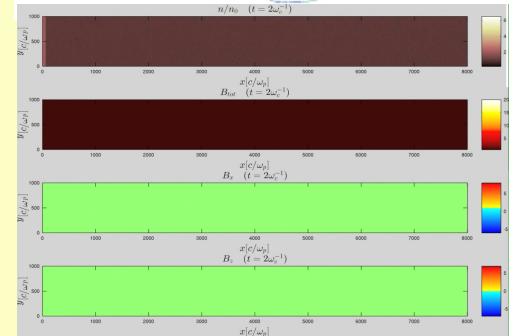
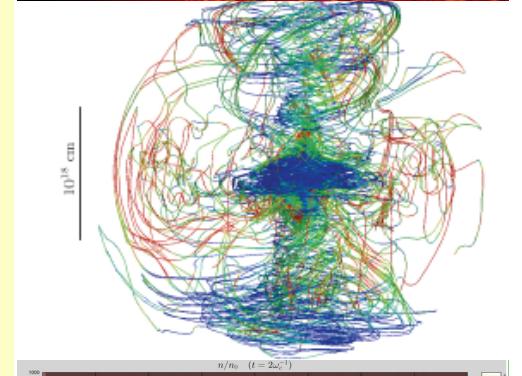
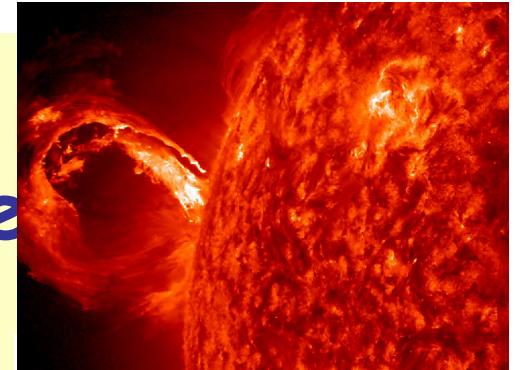
Jitter radiation? (Teraki, Takahara)

# Future

- Observations especially of flares
- MHD simulations
- Kinetic/PIC calculations
- Solar/space physics
- HED experiments
  - Z-Pinch
  - LCLS
  - NIF/OMEGA...

Sandia Z-pinch (stable?)  
~30 MA, ~30MV, ~100ns!,  
4 GK, ~300TW X-rays  
B~1 kT, r ~ 1mm??

Purdue



# Summary

- Many examples of intense flares from compact sites
- Crab Nebula continues to surprise, instruct, confound...
- Seem to need new, generic volumetric acceleration/ emission scheme for dissipating electromagnetic energy rapidly from compact regions of pair plasma
- Magnetic loops likely to become tangled/knotted
- Ohmic dissipation of knots/islands-> particle acceleration
- Current carried by the accelerated particles
- Runaway acceleration of minority of particles to high energy is possible - electromagnetic implosions
- In extreme cases major dissipation can be radiation-reaction limited - Synchrotron or Compton
- MHD simulations, kinetic calculations, HED experiments...