

Physics 56400 - Introduction to Elementary Particle
Physics - Part I.

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Office hours : Whenever - try your luck!

Text : Bettini, 2nd ed.
(Other editions are fine)

Other resources:

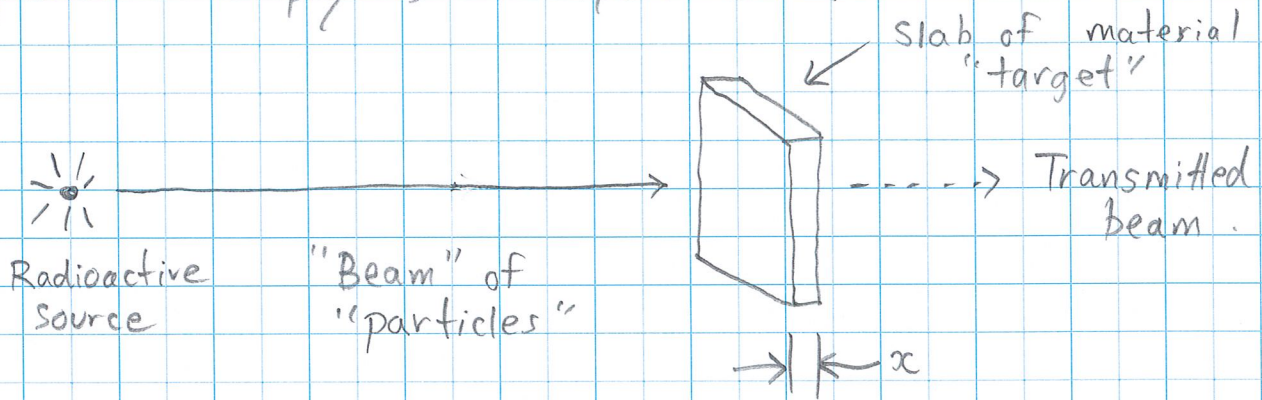
Web page : <http://www.physics.purdue.edu/> ...

... [/~mjones/phys56400/](http://www.physics.purdue.edu/~mjones/phys56400/)

Particle Data Group: <http://pdg.lbl.gov>

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Lets start by considering some very simple particle physics experiments.



The probability that a beam particle interacts with the target material as it traverses a slab of thickness dx is

$$P(x) = \frac{dx}{\lambda} \quad \text{Independent of } x!$$

Number of beam particles absorbed from x to $x+dx$:

$$dN = -N(x) \frac{dx}{\lambda}$$

$$\frac{dN}{N} = -\frac{dx}{\lambda}$$

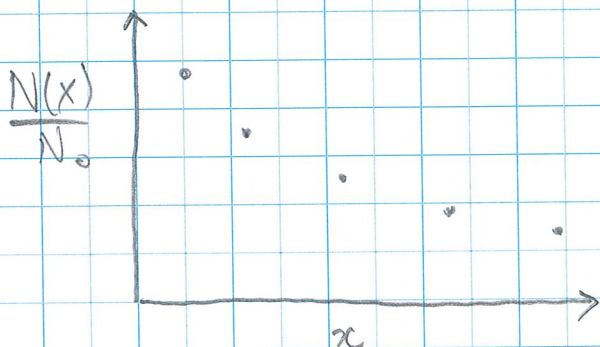
$$\log N(x) = -\frac{x}{\lambda} + k.$$

$$N(x) = N_0 e^{-x/\lambda}$$

The beam is exponentially attenuated by the target material.

How to measure λ ?

Measure $\frac{N(x)}{N_0}$ for various thicknesses x .



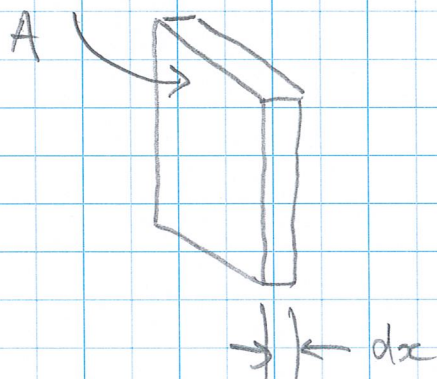
Fit an exponential function, or take $\log(N(x)/N_0)$ and fit a straight line.

What properties of the material determine the value of λ ?

We need to introduce a model for the interactions of beam and target particles.

Simple model: If a beam particle hits a target particle, it will "go away". Assume target particles are spheres of radius R . Assume beam particles are point-like.

How many target particles per unit area in a thin slice of material?



Volume $V = A dx$

Density ρ (mass per unit volume)

Atomic mass m (grams per mole)

Number of target particles:

$$N_T = N_A \frac{\rho}{m} V = N_A \frac{\rho}{m} A dx$$

Number of target particles per unit area:

$$\frac{N_T}{A} = \frac{N_A \rho}{m} dx$$

Probability of hitting a target particle:

$$P = \frac{N_T}{A} \cdot \pi R^2 = \frac{N_A \rho}{m} \cdot \pi R^2 dx$$

But this is just $P(x) = \frac{dx}{\lambda}$

$$\frac{1}{\lambda} = \frac{N_A \rho}{m} \pi R^2$$

$$\lambda = \frac{m}{N_A \rho \cdot \pi R^2}$$

In practice, it is common to normalize λ :

$$\lambda_I = \lambda \rho \quad (\text{units g/cm}^2)$$

$$\lambda_I = \frac{m}{N_A \pi R^2}$$

↖ Nuclear interaction length.

Does this make sense?

Simple nuclear model assumes uniform nuclear mass density.

$$\text{So } m \propto A \quad (\text{atomic number})$$

$$V \propto A$$

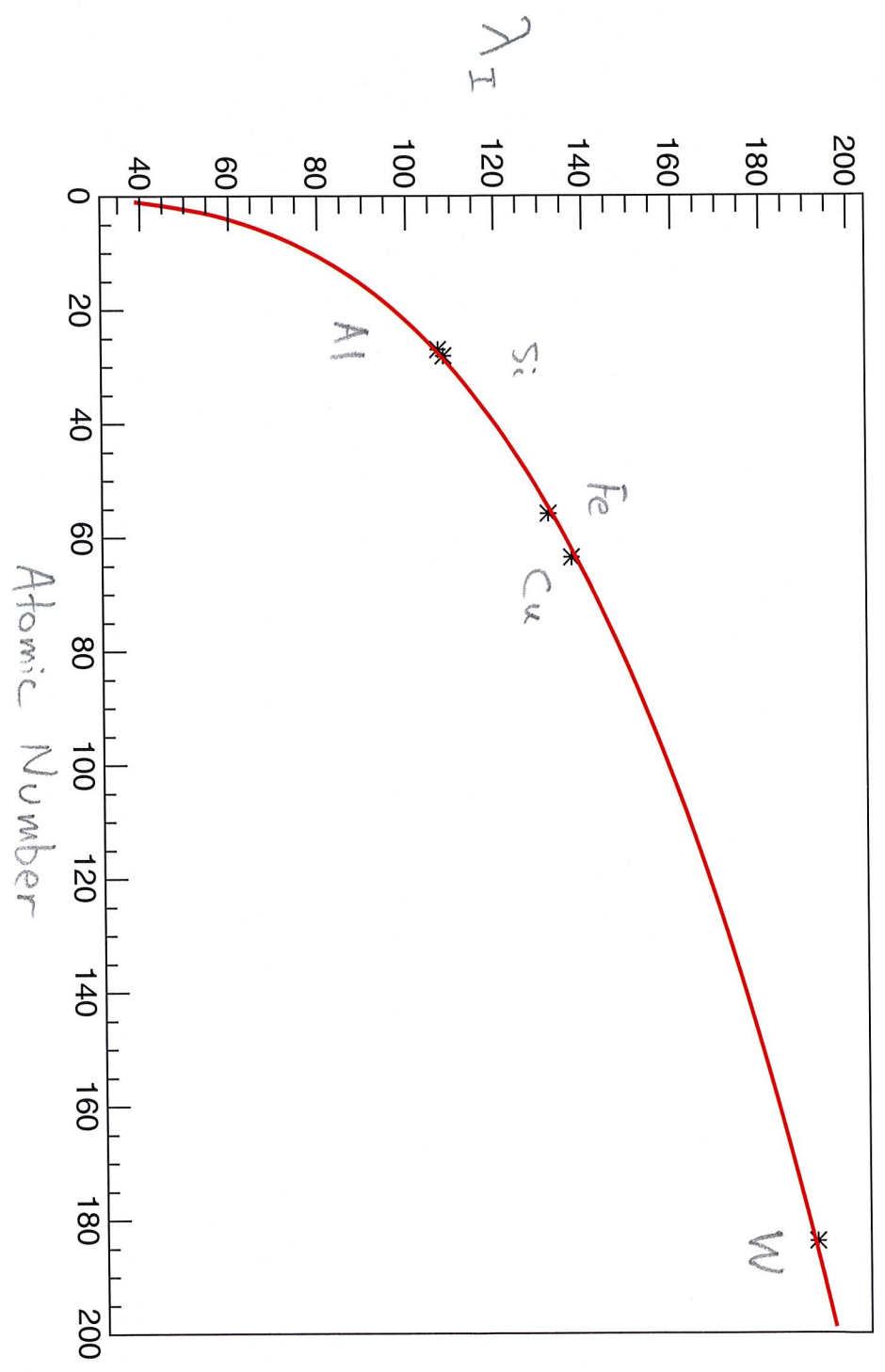
$$R \propto \sqrt[3]{A}$$

$$\text{So } \lambda_I \propto \frac{A}{A^{2/3}} \sim A^{1/3}$$

Can we estimate the size of a nucleon?

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$[O] \propto \lambda^4$



$$\lambda_I = k A^\alpha$$

$$k = 39 \text{ g/cm}^2$$

$$\alpha = 0.31$$