PURDUE DEPARTMENT OF PHYSICS

Physics 22000 General Physics

Lecture 13 – Collisions and Extended Objects

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Momentum and Energy

• Recall that momentum is always conserved

$$\vec{p} = m\vec{v}$$

 $m_1\vec{v}_{1i} + m_2\vec{v}_{2i} = m_1\vec{v}_{1f} + m_2\vec{v}_{2f}$
(when there is no external impulse)
• Energy is also always conserved

$$U_i + W = U_f$$

(K_i + U_{gi} + U_{si}) + W = (K_f + U_{gf} + U_{sf} + \Delta U_{int})
$$\Delta U_{int} = U_{int f} - U_{int i}$$

Energy Conservation

- Energy is always conserved, but the different types of energy are not necessarily individually conserved.
- Kinetic energy can be transformed into internal energy (heating, or deforming an object).
- Examples include elastic and inelastic collisions of two objects...





Two Types of Collisions Next, suppose the objects squish, and stick together: 	
$1 \longrightarrow v_{1i}$	2
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Inelastic Collisions

- By measuring the final velocities, we can determine the amount of energy converted to internal energy due to deformation of the objects
- In general, you can't predict this value ahead of time.
- When objects deform, we cannot make any predictions about the amount of kinetic energy that is converted to internal energy
- Even in collisions where there is deformation, the momentum of the system remains constant.

Types of Collisions

Table 6.7 Types of collisions. Elastic collisions Indaxic collisions Totally inelastic collisions Both the momentum and kinetic energy of the system ac constant. The internal method ling objects actick together gether. Examples: Three are no perfectly collisions between arony roj duty objects (such as billiard ball) come close. Collisions are admost exactly elastic. The original for a system is constrained in the perfect operfect action of the system is contrained in the perfect operfect action of the system is contrained in the perfect operfect action of the perfect operfect action operfect operfect action



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 A gun is several centimeters from a 1.0-kg wooden block hanging at the end of strings. The gun fires a 10-g bullet that becomes embedded in the block, which swings upward a height of 0.20 m.



A Ballistic Pendulum

• Initial momentum (just before collision):

$$p_i = m_b v_b$$

- Final momentum (just after collision): $p_f = (M_B + m_b) v_{bBi}$
- Kinetic energy (just after collision):

$$K_f = \frac{1}{2}(M_B + m_b)v_{bBi}^2$$

• Final gravitational potential energy:
$$U_{gf} = (M_B + m_b)gy_{bBf}$$

A Ballistic Pendulum

 Kinetic energy is converted to gravitational potential energy:

$$K_f = \frac{1}{2}(M_B + m_b)v_{Bbi}^2 = (M_B + m_b)gy_{bBf} = U_g$$
$$v_{Bbi} = \sqrt{2gy_{bBf}}$$

• Momentum conservation:

$$\begin{split} m_b v_b &= (M_B + m_b) v_{bBi} \\ v_b &= \frac{M_B + m_b}{m_b} v_{bBi} = \frac{M_B + m_b}{m_b} \sqrt{2gy_{bBf}} \\ &= \frac{1.010 \ kg}{0.01 \ kg} \sqrt{2(9.8 \ m/s^2)(0.2 \ m)} = 200 \ m/s \end{split}$$

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Power

- Why is it more difficult for the same person to run up a flight of stairs than to walk if the change in gravitational potential energy of the person-Earth system is the same in both scenarios?
 - The amount of internal energy converted into gravitational energy is the same in both cases, but the rate of that conversion is not.
 - When you run upstairs, you convert the energy at a faster rate.
 - The rate at which the conversion occurs is called the power.



Power

- Power is sometimes expressed in horsepower (hp): 1 hp = 746 W.
- Horsepower is most often used to describe the power rating of engines or other machines.
 - A 50-hp gasoline engine (typical in cars) converts the internal energy of the fuel into other forms of energy at a rate of 50 x 746 W = 37,300 W, or 37.30 J/s.



More Complex Objects

- So far we have been modeling objects as point-like with no internal structure.
- Objects are actually extraordinarily complex, with many internal parts that rotate and move relative to one another.
- To study complex structures, we need to develop a new way of modeling objects and of analyzing their interactions.







Center of Mass

- Although the location of the center of mass depends on the mass distribution of the object, the mass of the object is not necessarily evenly distributed around the center of mass.
- We will learn more about the properties of the center of mass; we just want to caution you about taking the name of this point literally.

Where is the Gravitational Force Exerted on a Rigid Body?

- If the cardboard does not tip, all forces exerted on it pass through the center of mass.
- We can assume that the gravitational force exerted on an object is exerted at the location of its center of mass.
- That is why the object's center of mass is sometimes called the object's center of gravity.







Causing Rotation

- Three factors affect the turning ability of a force:
 - The place where the force is exerted
 - The magnitude of the force
 - The direction in which the force is exerted





Qualitative Expressions for the Turning Ability of a Force • If scale 1 is twice as far

- from the axis of rotation and pulls half as hard as scale 3, the stick remains in equilibrium.
- If scale 1 is three times farther from the axis of rotation and exerts onethird of the force of scale 3, the stick remains in equilibrium

reference frame.



Static Equilibrium $F_2 = 31 \text{ N}$ • An object is in static **1**² equilibrium when it remains at rest (does not đ undergo either translational But the stick can be stable with unequal forces pulling at appropriate different ¹ **1**3 or rotational motion) with respect to a particular observer in an inertial







The "Turning Ability" of a Force

- It is equal to the product of the magnitude of the force and the distance the force is exerted from the axis of rotation.
- It is positive when the force tends to turn the object counterclockwise and negative when it turns the object clockwise.
- When one force tends to rotate an object counterclockwise and another force rotates it clockwise, their effects can cancel.





Factors that Affect the "Turning Ability" of a Force

- The direction (counterclockwise or clockwise) that the force can potentially rotate the object
- The magnitude of the force F
- The distance *l* of the point of application of the force from the axis of rotation
- The angle that the force makes relative to a line from the axis of rotation to the point of application of the force



Conditions for Static Equilibrium

- An object is in static equilibrium if an observer in an inertial reference frame does not observe it to move or to rotate.
- An object modeled as a rigid body is in translational static equilibrium when the net force acting on it is zero:

$$\Sigma F_{\text{on } O x} = F_{1 \text{ on } O x} + F_{2 \text{ on } O x} + \dots + F_{n \text{ on } O x} = 0$$

$$\Sigma F_{\text{on } O y} = F_{1 \text{ on } O y} + F_{2 \text{ on } O y} + \dots + F_{n \text{ on } O y} = 0$$

Conditions for Static Equilibrium

- A rigid body is in turning or rotational static equilibrium if it is at rest with respect to the observer and the sum of the torques about any axis of rotation produced by the forces exerted on the object is zero.
 - positive torques are counterclockwise
 - negative torques are clockwise

$$\Sigma \tau = \tau_1 + \tau_2 + \dots + \tau_n = 0$$

Tip

 All of the gravitational forces exerted by Earth on the different parts of a rigid body can be summarized as a single gravitational force being exerted on the center of mass of the rigid body.

Another Tip

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• If a rigid body is in static equilibrium, the sum of the torques about any axis of rotation is zero. In problem solving, it is often helpful to place the imaginary axis at the point on the rigid body where the force you know least about is exerted. That force drops out of the second condition of the equilibrium, and you can then use that equation to solve for some other unknown quantity.









