

Physics 21900

General Physics II

Electricity, Magnetism and Optics

Lecture 28 – Chapter 28.4-7

Radioactive Decays and Nuclear Reactions

Fall 2015 Semester

Prof. Matthew Jones

Announcement

Final Exam

Friday, December 18th 3:30-5:30 pm

Room PHYS 112

Covers material from lectures 16-28:

- Propagation of light, refraction and reflection
- Lenses and mirrors
- Diffraction and interference
- Electromagnetic waves, polarization
- Quantum optics, the Bohr model of hydrogen
- de Broglie waves
- Nuclear structure and decay

Nuclear Structure

- The chemical properties of the elements are mostly determined by the configuration of electrons in the outer orbits.
- A neutral atom contains equal numbers of electrons and protons.
- Protons are confined to the nucleus which is 10,000 times smaller than the atom and contains most of its mass.
- Neutrons counteract the electrostatic repulsion of the positive charge and stabilize the nucleus via the *strong nuclear force*.

Mass/Energy Relationship

- The kinetic energy formula $KE = \frac{1}{2} m v^2$ is only accurate when $v \ll c$.
- This is the case for classical mechanics
 - Balls rolling down incline planes
 - Planetary motion
- Generally not true for nuclear processes
- The special theory of relativity shows that energy and momentum are related by

$$E = \sqrt{m^2 c^4 + p^2 c^2}$$

- When $v \ll c$ this is approximately

$$E \approx mc^2 + \frac{p^2}{2m} = mc^2 + \frac{1}{2} m v^2$$

Mass/Energy Relationship

- For particles at rest, $v = 0$ and

$$E = mc^2$$

- Since $m = E/c^2$, a convenient unit for mass is eV/c^2 or MeV/c^2 .
- Example: what is the mass of a hydrogen atom in its ground state?

$$m_H = m_p + m_e - \frac{13.6 \text{ eV}}{c^2}$$

- The binding energy lowers the total mass compared to the masses of its constituents.
- This is a tiny effect for Hydrogen:

$$m_p = 938.28 \text{ MeV}/c^2$$

$$m_e = 0.511 \text{ MeV}/c^2$$

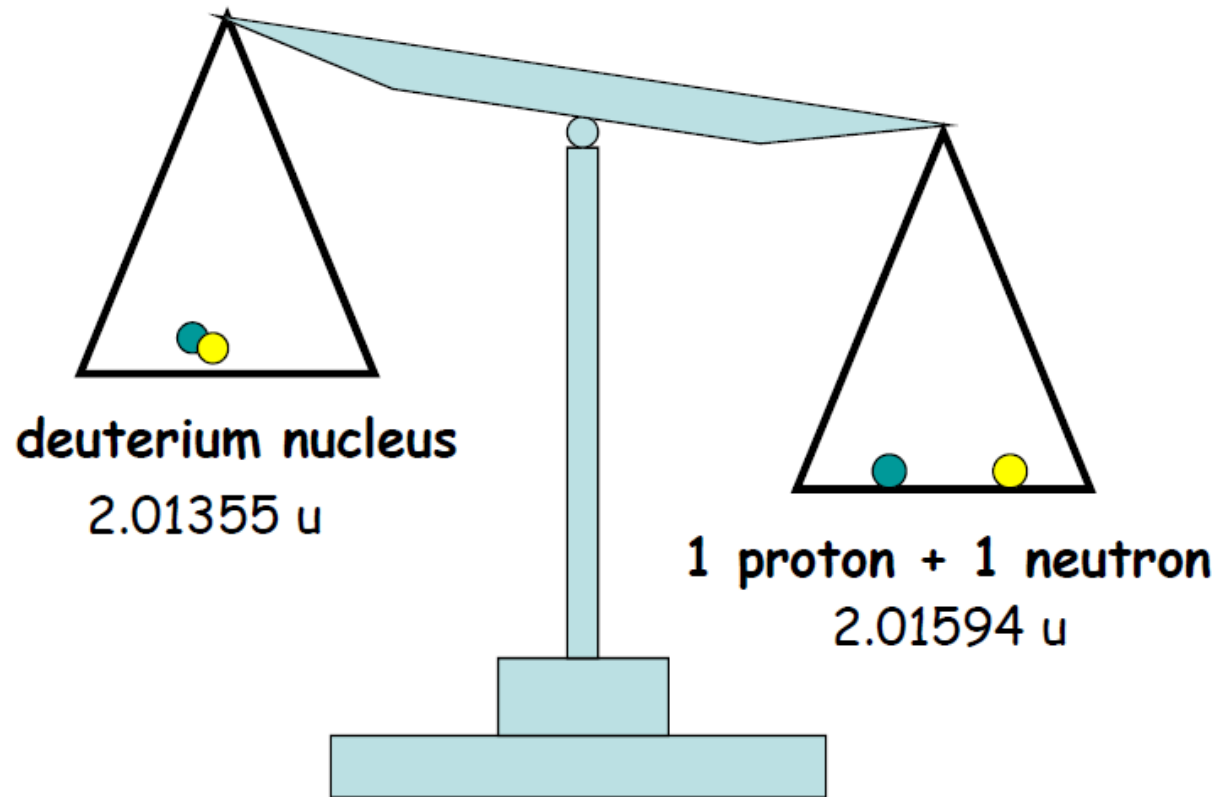
$$\Delta E = 13.6 \text{ eV}$$

- Total mass is 0.000001% lower than the mass of the proton and electron...

The mass of the parts is
more than the whole??

The mass of a
nucleus is NOT
equal to the
sum of its
parts!

$$\begin{array}{r} 2.01594 \text{ u} \\ - 2.01355 \text{ u} \\ \hline 0.00239 \text{ u} \end{array}$$



The "lost" mass (mass deficit)
is converted to a "binding
energy" given by $\Delta E = \Delta mc^2$

Nuclear Binding Energy

- The effect is much larger for nuclei.
- The strong nuclear force between an proton and a neutron is *attractive*.
 - a proton and neutron have a larger potential energy when separated by a large distance
 - just like two opposite point charges
- Deuterium (an isotope of hydrogen, 2H) is a bound state of a proton and a neutron.
- The binding energy of deuterium is $\Delta E = 2.22 \text{ MeV}$.

$$m_d = m_p + m_n - \Delta E$$

$$m_p = 938.28 \text{ MeV}/c^2$$

$$m_n = 939.57 \text{ MeV}/c^2$$

$$\Delta E = 2.22 \text{ MeV}$$

- This is a 0.1% effect but it is very important.

Nuclear Binding Energy

- An isotope X with atomic mass Z and atomic number A has binding energy

$$\Delta E = [Zm_p + Zm_e + (A - Z)m_n] - m_X$$

- Example: Binding energy of $^{56}_{26}\text{Fe}$

$$26 m_p = 26 (1.007276 u) = 26.1892 u$$

$$26 m_e = 26 (5.50 \times 10^{-4} u) = 0.0143 u$$

$$30 m_n = 30 (1.008665 u) = 30.2600 u$$

$$\text{TOTAL} = 56.4635 u$$

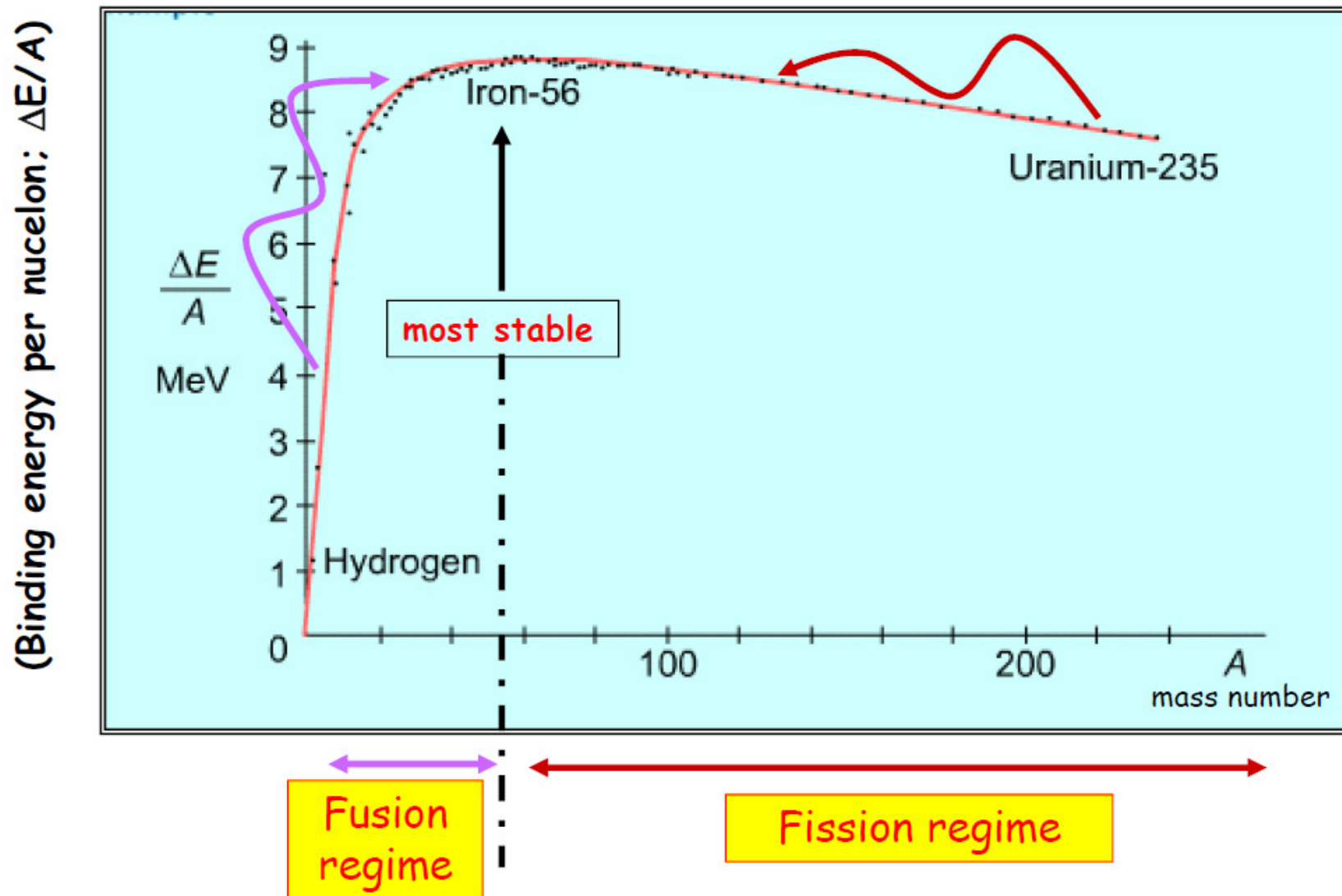
$$\text{Measured mass of } ^{56}_{26}\text{Fe} = 55.9349 u$$

$$\Delta E = 0.5286 u = 492.3 \text{ MeV}/c^2$$

$$\frac{\Delta E}{A} = \frac{492.3 \text{ MeV}}{56} = 8.8 \text{ MeV/nucleon}$$

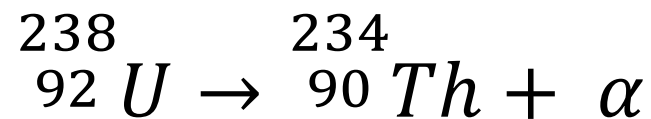
How much energy is required to remove one nucleon from a nucleus?

Answer depends on mass number $A=N+Z$



Radioactive Alpha Decay

- Neutrons stabilize the repulsive nature of protons in the nucleus
- If there are not enough neutrons, the nucleus becomes unstable and can eject an α particle.
- An α particle is the same as a helium nucleus: two protons and two neutrons.
- Example:



- Mass of the isotope decreases by 4
- Charge decreases by 2

$$\left. \begin{array}{l} m_{\text{U}238} = 238.0508 \text{ u} \\ m_{\text{Th}234} = 234.0436 \text{ u} \\ m_{\alpha} = 4.0015 \text{ u} \end{array} \right\} 238.0451 \text{ u} < 238.0508 \text{ u}$$

The rest of the energy goes into the kinetic energy of the decay products.

Radioactive Beta Decay

- A free neutron is unstable because it can decay into a proton and an electron

$$\left. \begin{aligned} m_n &= 939.5654 \text{ MeV}/c^2 \\ m_p &= 938.2720 \text{ MeV}/c^2 \\ m_e &= 0.5110 \text{ MeV}/c^2 \end{aligned} \right\} 938.7830 \text{ MeV}/c^2$$

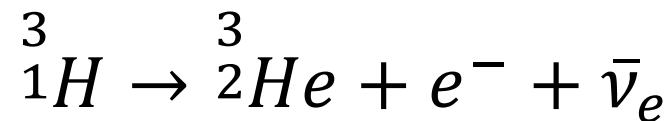
- The electron, when emitted in a nuclear decay, is called a β particle (but it is still just an electron)
- There is actually a third decay product called an electron anti-neutrino, which is almost (but not quite) massless

$$n \rightarrow p + e^- + \bar{\nu}_e$$

Radioactive Beta Decay

- Isotopes with too many neutrons typically undergo beta decay.

- Example: Tritium is ${}^3_1\text{H}$ (1 proton + 2 neutrons)

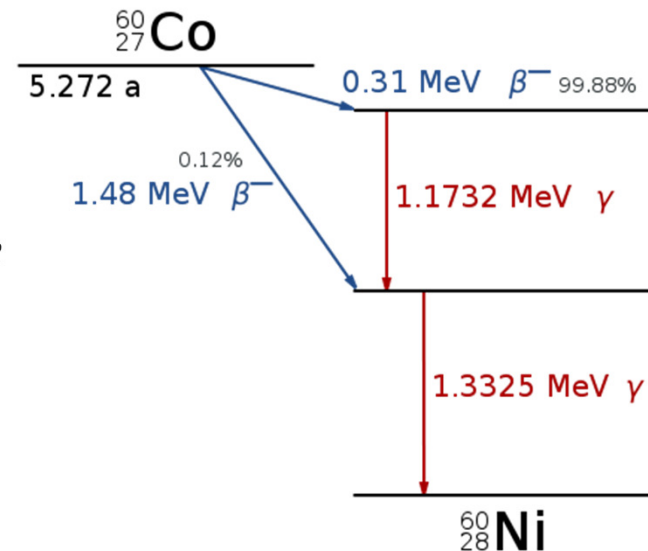
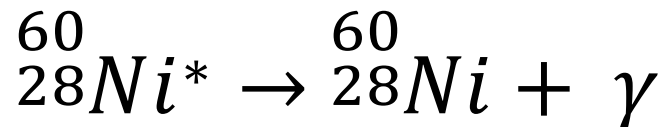


- One of the neutrons decayed into a proton
- The atomic mass doesn't change because the number of nucleons remains unchanged
- The atomic number increases by 1 to conserve charge

Radioactive Gamma Decay

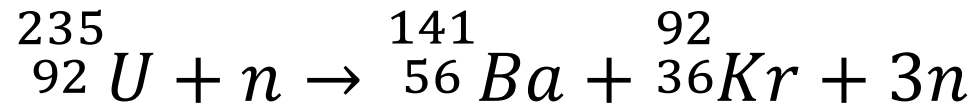
- The protons and neutrons in a nucleus are arranged in orbits, just like electrons in an atom.
- Nucleons in an excited state decay to a less excited state by emitting a high energy photon
- Neither the atomic mass nor the atomic number change
- Isotopes usually end up in an excited state due to a previous radioactive decay

- Example:



Nuclear Fission

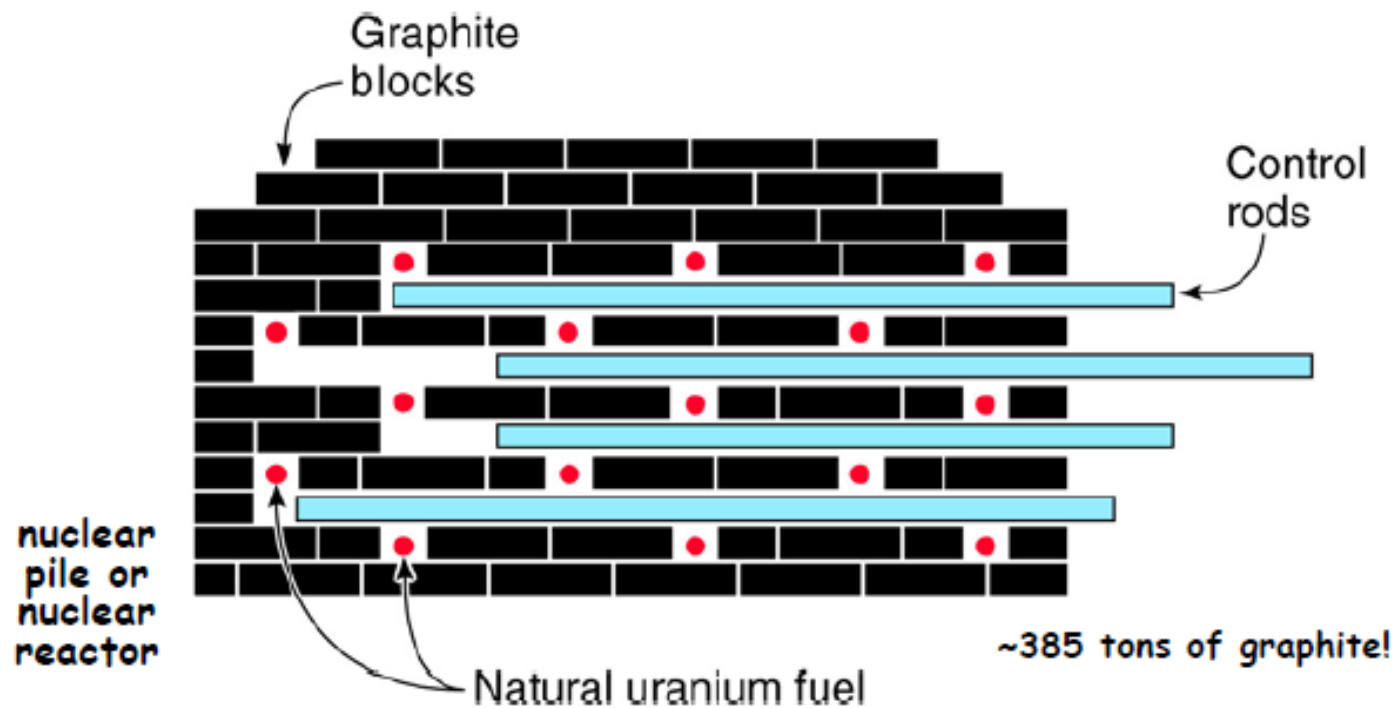
- Some heavy nuclei are so unstable that they just fall to pieces (spontaneous fission)
- Some heavy nuclei absorb a neutron and then fall apart (neutron induced fission)
- Example:



- Because one neutron is absorbed and 3 neutrons are produced, it is possible to sustain a chain reaction.
- However, only 0.72% of natural uranium is ${}^{235}_{92}\text{U}$
- The more abundant isotope ${}^{238}_{92}\text{U}$ captures fast neutrons but does not undergo fission.
- To make a chain reaction, you need to slow down the neutrons before they can be absorbed.

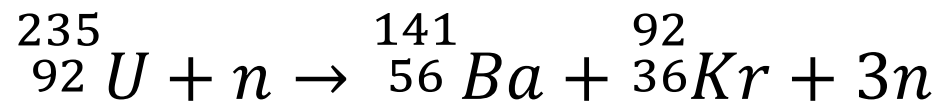
First controlled nuclear chain reaction
University of Chicago
3:30 PM, December 2, 1942
(dawn of nuclear power)

Graphite (carbon) was selected as a "moderator" to slow the neutrons emitted from the Uranium fuel.



Nuclear Fission

- How much energy is released?
- Consider the reaction:

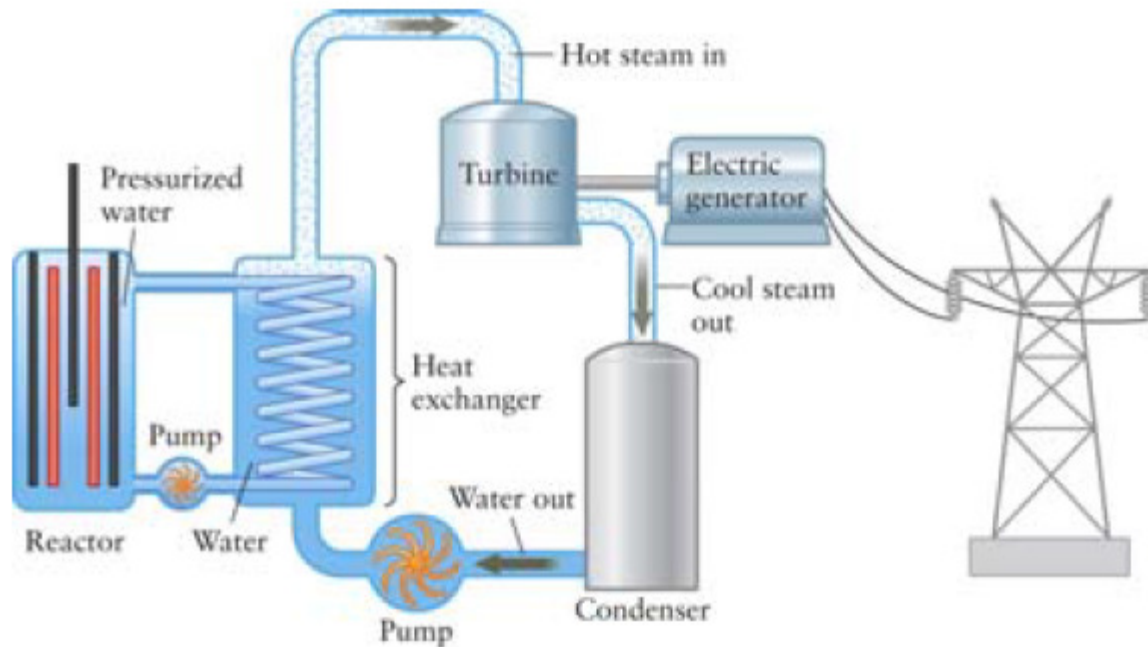


$$\left. \begin{array}{l} m_{\text{U}235} = 235.0439 \text{ u} \\ m_n = 1.0087 \text{ u} \end{array} \right\} 236.0526 \text{ u}$$

$$\left. \begin{array}{l} m_{\text{Ba}141} = 140.9144 \text{ u} \\ m_{\text{Kr}92} = 91.9263 \text{ u} \\ 3 m_n = 3.0261 \text{ u} \end{array} \right\} 235.8668 \text{ u}$$

- Mass difference: $0.1858 \text{ u} = 173 \text{ MeV}/c^2$
- Energy released: $173 \text{ MeV} = 1.5 \times 10^{-10} \text{ J}$
- But there are 2.5×10^{21} atoms in 1 gram of U-235.
- There are also other fission processes but they are similar.

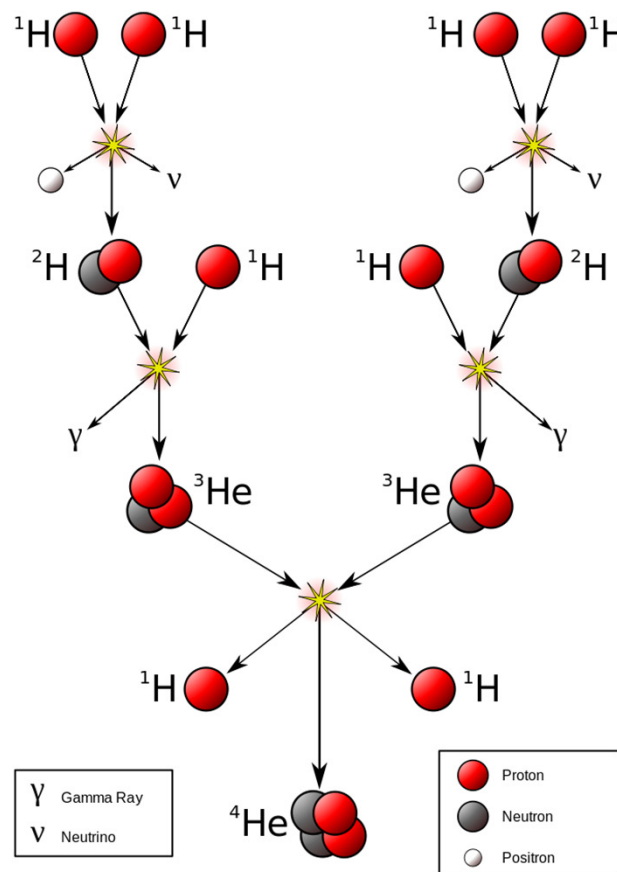
Modern Nuclear Reactors



- Nuclear fusion generates heat, just like burning coal.
 - 1 kg of coal produces 8 kWh of energy
 - 1 kg of U-235 produces 24,000,000 kWh of energy
- There are some engineering, safety, and waste disposal challenges though...

Solar Energy

- The sun converts hydrogen to heavier elements through the process of nuclear fusion.



- The total energy released is 26.22 MeV.
- The first step is very slow which is why stars burn for billions of years
- Protons usually just bounce off each other and don't fuse to form deuterium.

Semester Summary

Six BIG ideas

- Electrostatic Force - Coulomb's Law (1785)
- Induced emf - Faraday's Law (1830)
- Electromagnetic Waves - Maxwell (1865)
- Quantized Energy States - Planck, Einstein, Bohr (1900-1910)
- Particles behave like Waves - de Broglie (1923), Schrödinger (1926)
- *Relativity - Einstein (1905)*

We have covered five of these six BIG ideas. You should now have a general appreciation for why they are important.

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