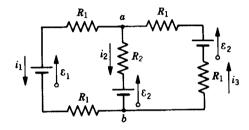
## PHYSICS 271 ELECTRICITY AND MAGNETISM SECOND EXAMINATION

19 November 1999

**INSTRUCTIONS:** Answer all questions on the answer sheet provided, it will be the only paper that is collected. This is a closed book exam.

(25 pts) 1.) For the circuit drawn below:



1.a.) What does the junction rule yield?

$$\mathbf{a)} \quad \mathcal{E}_1 + 2 \, \mathcal{E}_2 = 0$$

c) 
$$i_1 + i_2 = i_3$$

**b)** 
$$i_1 + i_2 + i_3 = 0$$
  
 $2i_1R_1 + i_2R_2 = \mathcal{E}_1 + \mathcal{E}_2$   
 $i_2R_2 + 2i_3R_1 = 0$ 

**d)** 
$$i_1 + i_2 = i_3$$
  
 $-2i_1R_1 + i_2R_2 = \mathcal{E}_1 - \mathcal{E}_2$   
 $i_2R_2 + 2i_3R_1 = 0$ 

1.b.) What does the loop rule yield?

**a)** 
$$i_1 + i_2 = i_3$$

c) 
$$-2i_1R_1 + i_2R_2 = \mathcal{E}_1 - \mathcal{E}_2$$
  
 $i_2R_2 + 2i_3R_1 = 0$ 

**b)** 
$$i_1 + i_2 + i_3 = 0$$
  
 $2i_1R_1 + i_2R_2 = \mathcal{E}_1 + \mathcal{E}_2$   
 $i_2R_2 + 2i_3R_1 = 0$ 

**d)** 
$$2i_{1}R_{1} + i_{2}R_{2} = \mathcal{E}_{1} + \mathcal{E}_{2}$$
  
 $i_{2}R_{2} + 2i_{3}R_{1} = 0$ 

1.c.) What is the current through the source of emf in the left branch?

**a)** 
$$i_1 = \frac{(2R_1 + R_2)(\mathcal{E}_2 - \mathcal{E}_1)}{4R_1(R_1 + R_2)}$$
 **c)**  $i_1 = \frac{(2R_1 + R_2)(\mathcal{E}_1 - \mathcal{E}_2)}{4R_1(R_1 + R_2)}$ 

**c)** 
$$i_1 = \frac{(2R_1 + R_2)(\mathcal{E}_1 - \mathcal{E}_2)}{4R_1(R_1 + R_2)}$$

**b)** 
$$i_1 = \frac{(\mathcal{E}_2 - \mathcal{E}_1)}{2(R_1 + R_2)}$$

**d)** 
$$i_1 = \frac{(2R_1 + R_2)(\mathcal{E}_1 + \mathcal{E}_2)}{4R_1(R_1 + R_2)}$$

1.d.) What is the current through the source of emf in the right branch?

**a)** 
$$i_3 = \frac{R_2(\mathcal{E}_1 - \mathcal{E}_2)}{4R_1(R_1 + R_2)}$$

c) 
$$i_3 = \frac{(2R_1 + R_2)(\mathcal{E}_1 - \mathcal{E}_2)}{4R_1(R_1 + R_2)}$$

**b)** 
$$i_3 = \frac{(\mathcal{E}_1 - \mathcal{E}_2)}{2(R_1 + R_2)}$$

**d)** 
$$i_3 = \frac{R_2(\mathcal{E}_2 - \mathcal{E}_1)}{4R_1(R_1 + R_2)}$$

1.e.) What is the current through the source of emf in the center branch?

**a)** 
$$i_2 = \frac{(2R_1 + R_2)(\mathcal{E}_2 - \mathcal{E}_1)}{4R_1(R_1 + R_2)}$$
 **c)**  $i_2 = \frac{(\mathcal{E}_1 - \mathcal{E}_2)}{2(R_1 + R_2)}$ 

$$c) i_2 = \frac{\left(\mathcal{E}_1 - \mathcal{E}_2\right)}{2\left(R_1 + R_2\right)}$$

$$\mathbf{b)} \quad i_2 = \frac{\left(\mathcal{E}_2 - \mathcal{E}_1\right)}{2\left(R_1 + R_2\right)}$$

**d)** 
$$i_2 = \frac{(2R_1 + R_2)(\mathcal{E}_1 + \mathcal{E}_2)}{4R_1(R_1 + R_2)}$$

**1.f.**) The potential difference  $V_a$ - $V_b$  is equal to

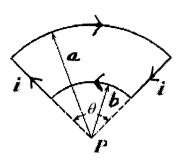
$$a) V_a - V_b = iR_{eq}$$

c) 
$$V_a - V_b = \frac{(2R_1 + R_2) \mathcal{E}_2 + R_2 \mathcal{E}_1}{2(R_1 + R_2)}$$

**b)** 
$$V_a - V_b = \frac{\mathcal{E}_2}{2(R_1 + R_2)}$$

**b)** 
$$V_a - V_b = \frac{\mathcal{E}_2}{2(R_1 + R_2)}$$
 **d)**  $V_a - V_b = \frac{-\mathcal{E}_2}{2(R_1 + R_2)}$ 

2.) Consider the circuit drawn below. The curved segments are arcs of circles of radii a (25 pts) and b. The straight segments are along the radii. Assume current i flows in the circuit.

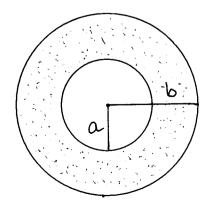


- **2.a.)** The direction of the magnetic field at P is
- a) B points up
- c) B points to the right
- e) B points into the page

- **b) B** points down
- d) B points to the left
- f) B points out of the page

**g)** 
$$B = 0$$

- **2.b.)** The magnitude of the magnetic field at P is
- **a)**  $B = \frac{\mu_0}{4\pi} i \frac{1}{2} \left( \frac{1}{a} + \frac{1}{b} \right)$
- c) B = 0, since P is outside the loop
- **b)**  $B = \frac{\mu_0}{4\pi} i\theta \left(\frac{1}{h} \frac{1}{a}\right)$
- $\mathbf{d)} \ B = \frac{\mu_0 i}{\left[ (a-b) + \theta (a+b) \right]}$
- **2.c.**) The magnetic dipole moment  $\mu$  of the above current loop is
- a)  $i\pi(a^2-b^2)$ , into the page
- c)  $\mu = 0$ , since P is outside the loop
- **b)**  $\frac{\mu_0}{4\pi}i\left(a^2-b^2\right)$ , into the page **d)**  $i\theta\frac{1}{2}(a^2-b^2)$ , into the page
- 3.) Below is drawn a cross section of a hollow cylindrical conductor of radii a and b, (25 pts) carrying a uniformly distributed current i flowing out of the page.



**3.a.)** Determine the magnetic field for radius r>b.

- a)  $B = \frac{\mu_0 i}{4\pi r}$ , tangent to circles in CCW direction
- **b)**  $B = \frac{\mu_0 i}{4\pi r}$ , out of the page
- c)  $B = \frac{\mu_0 i}{2\pi r}$ , tangent to circles in the CCW direction
- **d)**  $B = \frac{\mu_0 i}{2\pi r}$ , out of the page

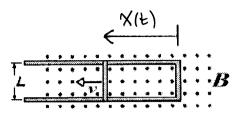
**3.b.)** Determine the magnetic field for radius r < a.

- a)  $B = \frac{\mu_0 i}{4\pi a}$ , tangent to circles in CCW direction
- **b)** B = 0
- c)  $B = \frac{\mu_0 i}{4\pi r}$ , tangent to circles in the CCW direction
- **d)**  $B = \frac{\mu_0 i}{4\pi r}$ , out of the page

**3.c.)** Determine the magnetic field for radius a < r < b.

- a)  $B = \frac{\mu_0 i}{2\pi r} \frac{(r^2 a^2)}{(b^2 a^2)}$ , tangent to circles in CCW direction
- **b)**  $B = \frac{\mu_0 i}{2\pi r} \frac{(r^2 a^2)}{(b^2 a^2)}$ , out of the page
- c)  $B = \frac{\mu_0 i}{4\pi r} \frac{(r^2 a^2)}{(b^2 a^2)}$ , tangent to circles in the CCW direction
- **d)**  $B = \frac{\mu_0 i}{4\pi r} \frac{(r^2 a^2)}{(b^2 a^2)}$ , out of the page

(25 pts) 4.) A rod lies across frictionless rails in a uniform magnetic field B, as shown. The rod moves to the left with constant speed v and at t=0 its position is  $x(t=0)=x_0$ .



**4.a.)** In order for the emf around the circuit to be zero, the magnitude of the magnetic field should

a) not change

- d) increase quadratically with time
- b) increase linearly with time
- e) decrease quadratically with time
- c) decrease inversely with time

**4.b.)** A rod with resistance R lies across frictionless conducting rails in a constant uniform magnetic field B, as drawn above. Assume the rails have negligible resistance. The force that must be applied by a person to pull the rod to the left at constant speed v is

**a)** 0

 $\mathbf{d)} \; \frac{B^2 L^2 v}{R}$ 

**b)** *BLv* 

 $e) \frac{B^2 L x v}{R}$ 

c)  $\frac{BLv}{R}$ 

## Physics 271 Electricity and Magnetism Examination 2: Equation Sheet

$$i=rac{dq}{dt} \hspace{0.5cm} ; \hspace{0.5cm} ec{j}=Nqec{v_d} \hspace{0.5cm} ; \hspace{0.5cm} i=\int_{S}ec{j}\cdot dec{A} \hspace{0.5cm} (1)$$

$$\int_{V} \frac{\partial \rho}{\partial t} dV + \oint_{S} \vec{j} \cdot d\vec{A} = 0$$
 (2)

$$ec{j}=\sigmaec{E}$$
 ;  $V=iR$  ;  $R=rac{
ho L}{A}$  (3)

$$P = iV ; P = i^2 R = \frac{V^2}{R} (4)$$

Kirchhoff's First Rule: At any junction, the sum of the currents leaving the junction equals the sum of the currents entering the junction.

Kirchhoff's Second Rule: The algebraic sum of the changes in potential encountered in a complete traversal of any closed circuit is zero.

Parallel Resistors:  $\frac{1}{R_{eq}} = \sum_{i=1}^{N} \frac{1}{\vec{R}_i}$  Series Resistors:  $R_{eq} = \sum_{i=1}^{N} R_i$   $\vec{F} = q \left( \vec{E} + \vec{v} \times \vec{B} \right) \quad ; \qquad \oint_{\vec{G}} \vec{B} \cdot d\vec{A} = 0$  (5)

$$d\vec{F} = id\vec{s} \times \vec{B}$$
 ;  $\vec{F} = i\vec{L} \times \vec{B}$  (6)

$$\vec{\mu} = NiA\hat{n}$$
 ;  $\vec{\tau} = \vec{\mu} \times \vec{B}$  ;  $U = -\vec{\mu} \cdot \vec{B}$  (7)

$$d\vec{B} = \frac{\mu_0}{4\pi} \frac{id\vec{s} \times \vec{r}}{r^3} \qquad ; \qquad \qquad \vec{B} = \frac{\mu_0}{4\pi} \int_C \frac{id\vec{s} \times \vec{r}}{r^3} \tag{8}$$

$$\oint_C \vec{B} \cdot d\vec{s} = \mu_0 i_{\text{enclosed}} \qquad ; \qquad \qquad \mathcal{E} = -\frac{d\Phi_B}{dt} \tag{9}$$

$$\Phi_B = \int_S \vec{B} \cdot d\vec{A} \qquad ; \qquad \qquad \mathcal{E} = \oint_C \vec{E} \cdot d\vec{s} = -\frac{d}{dt} \int_S \vec{B} \cdot d\vec{A}$$
 (10)