

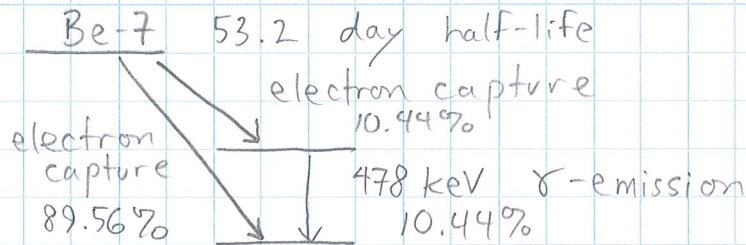
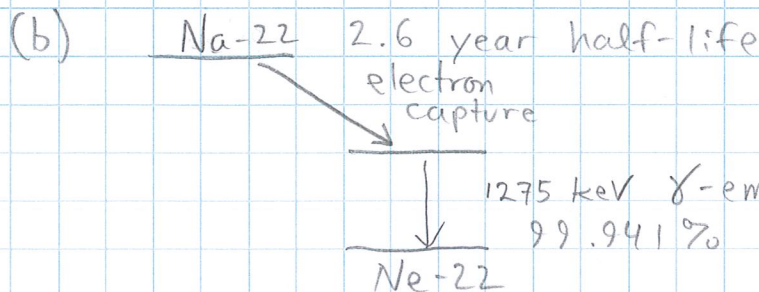
Physics 56400 Assignment # 1

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1 (a) The surface area of the gamma ray detector is $a = \pi r^2$ where $r = 3 \text{ cm}$. The surface area of a sphere of radius $R = 23 \text{ cm}$ is $A = 4\pi R^2$.

The acceptance of the detector is then

$$E = a/A = \frac{1}{4} r^2 / R^2 = \frac{(3 \text{ cm})^2}{4(23 \text{ cm})^2} = 0.0043$$



(c) The total decay rate is the measured rate divided by the acceptance,

$$R = \frac{1.79 \text{ s}^{-1}}{0.0043} = 416.3 \text{ s}^{-1}$$

If the sample was irradiated 266 days before it was analyzed then the original activity was

$$R_0 = R \cdot 2^{t/t_{1/2}}$$

where $t_{1/2} = (2.6 \text{ years})(365.25 \text{ days/year}) = 949.7 \text{ days}$.

Hence, $t/t_{1/2} = 0.28$ and

$$R_0 = (416.3 \text{ s}^{-1}) \cdot 2^{0.28}$$

$$= 505.5 \text{ s}^{-1}$$

(d) Just after the irradiation was complete, the activity was 505.5 s^{-1} . This is related to the number of Na-22 atoms present by

$$R_0 = -\frac{dN}{dt} = \frac{N_0}{\tau}$$

where $\tau = \frac{t_{1/2}}{\log 2}$.

Hence, $N_0 = R_0 \tau$

$$= \frac{(505.5 \text{ s}^{-1})(949.7 \text{ days})(86400 \text{ sec/day})}{\log 2}$$

$$= 59.8 \times 10^9$$

The probability that one proton makes an Na-22 atom is

$P = \frac{N\sigma}{A}$ where N is the number of target nuclei in a sample with area A .

But $N = \frac{t \cdot A \cdot \rho}{m} \cdot N_A$

where ρ is the density of aluminum, t is the thickness of the sample and m is the molecular mass.

Hence, $P = \frac{t \cdot p \cdot \sigma}{m} N_A$

Given that $\sigma = 15 \times 10^{-3}$ barn

$t = 0.025$ mm

$p = 2.7$ g \cdot cm⁻³

$m = 26.98$ g \cdot mol⁻¹

$N_A = 6.02 \times 10^{23}$ mol⁻¹

$$P = \frac{(2.5 \times 10^{-3} \text{ cm})(2.7 \text{ g} \cdot \text{cm}^{-3})(15 \times 10^{-27} \text{ cm}^2)(6.02 \times 10^{23} \text{ mol}^{-1})}{26.98 \text{ g/mol}}$$

$$= 2.26 \times 10^{-6}$$

Therefore, if there were 59.8×10^9 Na-22 atoms produced, then the number of protons on target was

$$N_{\text{POT}} = \frac{59.8 \times 10^9}{2.26 \times 10^{-6}} = 26.5 \times 10^{15}$$

(e) The number of Be-7 atoms produced by the proton beam can be calculated by scaling the number of Na-22 atoms by the ratio of the cross sections.

$$N_{\text{Be7}} = N_{\text{Na-22}} \cdot \frac{\sigma_{\text{Be7}}}{\sigma_{\text{Na22}}} = \frac{(59.8 \times 10^9)(6.4 \text{ mb})}{(15 \text{ mb})} = 25.5 \times 10^9$$

The Be-7 decay rate is

$$\frac{1}{\tau_{\text{Be7}}} = \frac{\log 2}{(53.2 \text{ days})(86400 \text{ s/day})} = 0.151 \times 10^{-6} \text{ s}^{-1}$$

Hence, the Be-7 activity just after irradiation was

$$R_{\text{Be7}} = \frac{N_{\text{Be7}}}{\tau_{\text{Be7}}} = (25.5 \times 10^9) (0.151 \times 10^{-6} \text{ s}^{-1})$$

$$= 3.85 \times 10^3 \text{ s}^{-1}$$

After 266 days the activity will be

$$R'_{\text{Be7}} = R_{\text{Be7}} \cdot \left(\frac{1}{2}\right)^{t/t_{1/2}}$$

$$= (3.85 \times 10^3 \text{ s}^{-1}) \left(\frac{1}{2}\right)^{266/53.2}$$

$$= 120 \text{ s}^{-1} .$$

However, the branching fraction for Be-7 to produce a γ is only 10.44% and the detector acceptance is only 0.0043. Therefore the observed Be-7 counting rate is only

$$R = (120 \text{ s}^{-1}) (0.1044) (0.0043)$$

$$= 0.054 \text{ s}^{-1} .$$