PURDUE DEPARTMENT OF PHYSICS

Physics 22000 General Physics

Lecture 6 – Projectile Motion

Fall 2016 Semester Prof. Matthew Jones



Review of Chapter 3

- So far we learned how to add forces as vectors to calculate the net force on an object
 - We used free-body diagrams
 - We added the components of each vector in the xand y-directions
- · We considered several types of forces
 - Force of the earth on an object (gravity)
 - Tension in strings
 - Static and kinetic friction
- So far we still only considered linear motion
 - Motion was constrained to a straight line

Using Newton's laws to explain how static friction helps a car start and stop

- Increasing or decreasing a car's speed involves static friction between the tire's region of contact and the pavement.
 - To move faster, turn the tire faster. The tire then pushes back harder on the pavement, and the pavement pulls forward more on the tire (Newton's third law).

Using Newton's laws to explain how static friction helps a car start and stop (Cont'd) – To slow down, turn the tire more slowly. The tire

 Io slow down, turn the tire more slowly. The tire pulls forward on the pavement, which in turn pushes back on the tire to accelerate the car backward.

(b) The tire is moving to the right and turning faster.



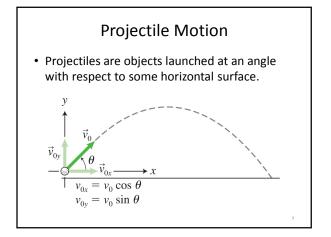


If the tire turns faster, it pushes back harder on the road. The road in turn pushes forward on the tire, causing the car to accelerate to the right.

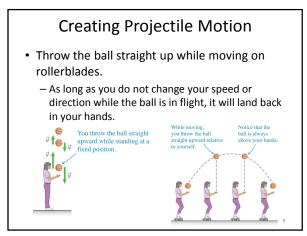


Tip

 Some people think a car's engine exerts a force on the car that starts the car's motion and helps it maintain a constant speed despite air resistance. In fact, the forces the engine exerts on other parts of the car are internal forces. Only external forces exerted by objects in the environment can affect the car's acceleration. The engine rotates the wheels, and the wheels push forward or backward on the ground. It is the ground (an external object) that pushes backward or forward on the wheels, causing the car to slow down or speed up. The force responsible for this backward or forward push is the static friction force that the road exerts on the tires.







Qualitative analysis of projectile motion in the y-axis

- A ball thrown straight up in the air by a person moving horizontally on rollerblades will land back in the person's hand.
- Earth exerts a gravitational force on the ball, so its upward speed decreases until it stops at the highest point, and then its downward speed increases until it returns to your hands.
- With respect to you on the rollerblades, the ball simply moves up and down.

Qualitative analysis of projectile motion in the x-axis

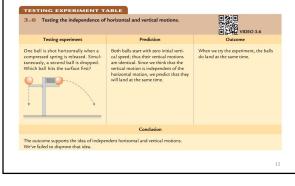
- A ball thrown straight up in the air by a person moving horizontally on rollerblades will land back in the person's hand.
- The ball also moves horizontally.
- No object exerts a horizontal force on the ball. Thus, according to Newton's first law, the ball's horizontal velocity does not change once it is released and is the same as the person's horizontal component of velocity.

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Qualitative analysis of projectile motion in the *x*- and *y*-axes

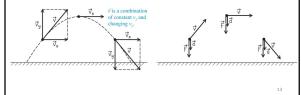
- A ball thrown straight up in the air by a person moving horizontally on rollerblades will land back in the person's hand.
- The ball continues moving horizontally as if it were not thrown upward.
- The ball moves up and down as if it does not move horizontally.
- It seems that the horizontal and vertical motions of the ball are independent of each other. We need to test this pattern!

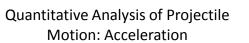
Experiment to Test Independence of Motion in x- and y-directions



Conceptual Exercise: Throwing a Ball

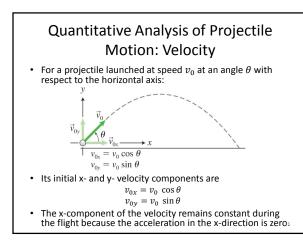
 You throw a tennis ball as a projectile. Arrows represent the ball's instantaneous velocity and acceleration and the force or forces exerted on the ball by other objects when at the three positions shown in the diagram.





- The equations of motion for velocity and constant acceleration are used to analyze projectile motion quantitatively.
- The *x*-component (in the horizontal direction) of a projectile's acceleration is zero.
- The *y*-component (in the vertical direction) of a projectile's acceleration is *-g*.
 - The force is mg—the force of gravity that Earth exerts on the projectile.

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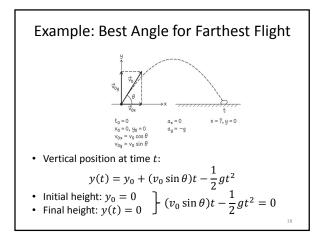
Quantitative Analysis of Projectile Motion: Using Kinematic Equations

 Projectile motion in t 	ne • Projectile motion in the
x-direction:	y-direction:
$(a_x = 0)$	$(a_y = -g)$
$v_x = v_{0x} = v_0 \cos\theta$	$v_y = v_{0y} + a_y t$
$x = x_0 + v_{0x}t$	$= v_0 \sin \theta + (-g)t$
$= x_0 + (v_0 \cos \theta)t$	1
	$y = y_0 + v_{0y}t + \frac{1}{2}a_yt^2$
The y-equations can be used	to 4
determine the time interval f projectile's flight.	For the $= y_0 + (v_0 \sin \theta)t - \frac{1}{2}gt^2$
 The x-equations can be used determine how far the project travels in the horizontal direct during that time integral 	tile
during that time interval.	16



Example: Best angle for farthest flight

- While rioting in down town West Lafayette, you want to throw a rock the farthest possible horizontal distance. You keep the initial speed of the rock constant and find that the horizontal distance it travels depends on the angle at which it leaves your hand.
- What is the angle at which you should throw the rock so that it travels the longest horizontal distance, assuming it is always thrown with the same initial speed?





Example: Best Angle for Farthest Flight

$$(v_0\sin\theta)t - \frac{1}{2}gt^2 =$$

0

- This has two solutions. One is just t = 0.
- The other solution will be when $t \neq 0$, so we can divide by t to obtain:

$$(v_0\sin\theta) - \frac{1}{2}gt = 0$$

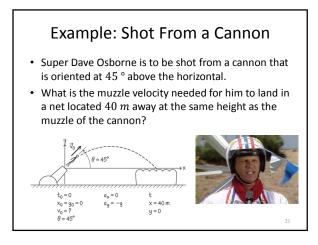
 $t = \frac{2 v_0 \sin \theta}{g}$

Example: Best Angle for Farthest Flight

- Next, substitute *t* into equation for horizontal motion:
 - $x = x_0 + (v_0 \, \cos \theta)t$
- Initial position: $x_0 = 0$
- Final position:
- Trigonometric identity (just google them): $2 \cos \theta \sin \theta = \sin 2\theta$
- This is maximal when $2\theta = 90^{\circ} (\sin 90^{\circ} = 1)$

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- Maximum distance is when $heta=45^\circ$



Example: Shot From a Cannon

Remember, we already worked out that

 $x = (v_0 \, \cos \theta) \left(\frac{2 \, v_0 \, \sin \theta}{g} \right)$

• And we used the trigonometric identity: $2\cos\theta\sin\theta = \sin2\theta$

to obtain:

$$x = \frac{v_0^2 \sin 2\theta}{g}$$

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• But when
$$\theta = 45^{\circ}$$
, sin $2\theta = 1$, so
 $v_0 = \sqrt{x \ g} = \sqrt{(40 \ m)(9.8 \ m/s^2)}$
 $= 20 \ m/s = 71 \ km/h$

Application: The Hippie Jump

- Examples:
 - https://youtu.be/R_C7nMs0bKA
 - <u>https://youtu.be/mhyCCJ3EUcQ</u>
- It is important to jump *straight up*
- If you don't, then Newton's third law says that you exert a force on the skateboard in the horizontal direction.
- This force causes you and the skateboard to accelerate in opposite horizontal directions
- The horizontal velocities are no longer equal and you will miss the skateboard when you land.