

Physics 22000
General Physics
 Lecture 4 – Applying Newton's Laws

Fall 2016 Semester
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1

Review of Lectures 1, 2 and 3

- Algebraic description of linear motion with constant acceleration:

$$x(t) = x_0 + v_{0x}t + \frac{1}{2}a_x t^2$$

$$v_x(t) = v_{0x} + a_x t$$

- Newton's Laws:
 - In an inertial reference frame, the motion of an object remains unchanged when there is no net force acting on it.
 - Acceleration is proportional to the net force and inversely proportional to the mass of an object.
 - Forces come in pairs, but act on different objects.

2

Review of Lectures 1,2 and 3

- We can relate velocity, distance and acceleration at any point in time:

$$2 a_x (x - x_0) = v_x^2 - v_{0x}^2$$

- Average acceleration:

$$a_x = \frac{v_x^2 - v_{0x}^2}{2(x - x_0)}$$

- The force acting on an object of mass m that will result in this acceleration is $F_x = ma_x$.

3

Example

- You are approaching a red light. You slow down from 50 km/h to rest over a distance of 100 m.
- If your mass is 80 kg, what force do you feel?
 - You are the system object
 - The seat and the seat belt apply the force

$$F = \frac{(80 \text{ kg}) \left(0 - \left[\frac{(50 \text{ km/h})(1000 \text{ m/km})}{3600 \text{ s/h}} \right]^2 \right)}{2(100 \text{ m} - 0)} = 77 \text{ N}$$

4

Motion and Forces in More than One Dimension

- So far we have mainly considered motion in only one dimension.
- We picked a coordinate axis (with an origin and a direction) to define the observer's reference frame.
- Newton's second law for the *components* along the x-axis:

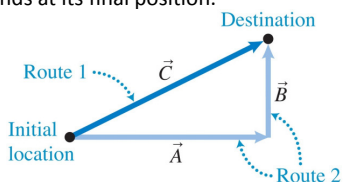
$$a_x = \frac{\sum F_x}{m}$$

- We can analyze motion and forces in more than one dimension by considering each component along different coordinate axes separately.

5

Displacement in Two Dimensions

- Displacement starts from an object's initial position and ends at its final position.

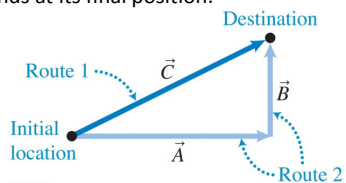


- Route 1 is a direct path represented by a displacement vector.
 - Its tail represents your initial location and its head represents your final destination.

6

Displacement in Two Dimensions

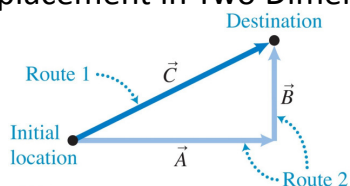
- Displacement starts from an object's initial position and ends at its final position.



- Route 2 goes along two roads.
 - You first travel along A, then along B.
- You end at the same final destination with either route.**

7

Displacement in Two Dimensions

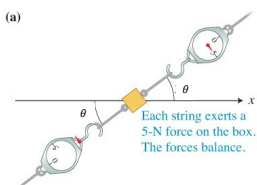


- Route 1 has the same displacement as route 2, showing how to add vectors graphically.
 - $\vec{A} + \vec{B} = \vec{C}$
 - $\vec{A}$ and $\vec{B}$ are perpendicular to each other.
- The key to breaking a vector into its components is to pick vectors perpendicular to each other that, when added, are equivalent to the original vector.*

8

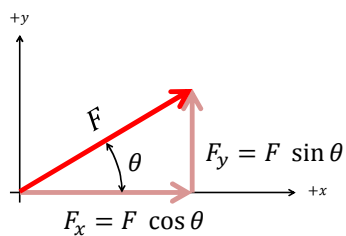
Forces in Two Dimensions

- A small box is being pulled by two springs scales.
- Each scale is at an angle θ with respect to the x-axis.
- How can we replace one scale with two scales that lie along the x- and y-axes?



9

Basic Trigonometry

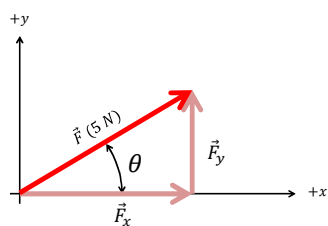


Pythagoras' Theorem: $F^2 = F_x^2 + F_y^2$ } $F = \sqrt{F_x^2 + F_y^2}$

10

Forces in Two Dimensions

- We need to find the lengths of the perpendicular sides of the triangle:



11

Forces in Two Dimensions

Suppose $\theta = 37^\circ$...

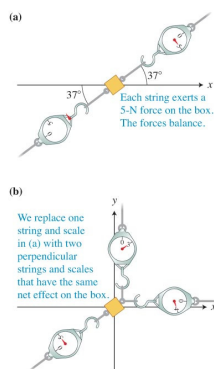
$$F = 5 \text{ N}$$

$$F_x = (5 \text{ N}) \cos 37^\circ = 4 \text{ N}$$

$$F_y = (5 \text{ N}) \sin 37^\circ = 3 \text{ N}$$

It works out nicely because this is a 3-4-5 triangle.

The net force is the same!
(ZERO)

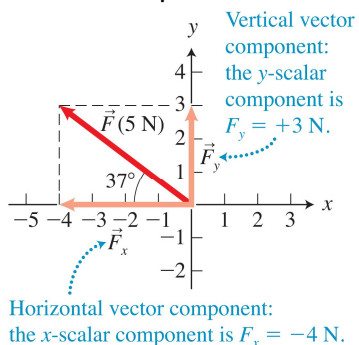


Breaking Forces into Scalar Components

- We can replace any force $\vec{F}$ into two perpendicular forces along the x- and y-axes, so long as they add graphically to equal $\vec{F}$.
- We represent these two forces by scalar components:
 F_x is the component along the x-axis
 F_y is the component along the y-axis
- Components can be positive or negative, depending on whether they point in the + or - direction.

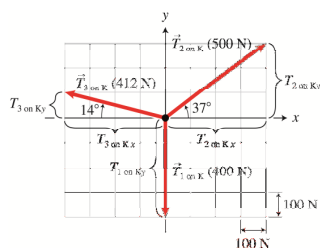
13

Breaking Forces into Scalar Components



14

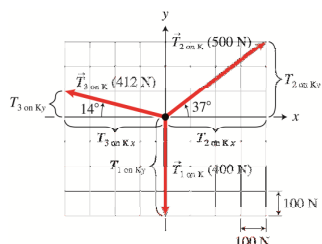
Newton's Second Law in Two Dimensions



- We can apply Newton's second law to situations where the forces are not along only one axis.
- First, find the scalar components of the forces.
- The sum of the scalar components of the force along the **x-axis** equals *mass times acceleration* along the **x-axis**.

15

Newton's Second Law in Two Dimensions



- We can apply Newton's second law to situations where the forces are not along only one axis.
- First, find the scalar components of the forces.
- The sum of the scalar components of the force along the **y-axis** equals *mass times acceleration* along the **y-axis**.

16

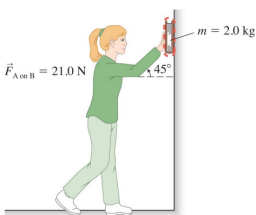
Newton's Second Law in Two Dimensions

- If possible, we might pick the direction of the x-axis to be in the direction of the acceleration.
- Then the component of the acceleration along the other axis will be zero.
- This would simplify the problem, but might not always be possible.
- *Think carefully about which choice of geometry makes the problem easier to analyze!*

17

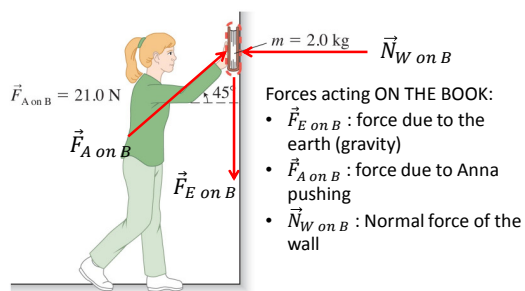
Example: Determining Forces and Acceleration

- Princess Anna Arkadievna Karenina pushes a 2.0 kg book onto a slippery wall, exerting a force of 21.0 N at an angle of 45° above the horizontal.
- What is the normal force of the wall on the book?
- Does the book slide up or down the wall?



18

Determining Forces and Acceleration



- These are the forces at this particular instant in time... at a later time, the angle might change...

19

Determining Forces and Acceleration

- The acceleration in the x-direction is zero
 - the book can only slide up and down the wall
$$a_{B,x} = \frac{\sum F_x}{m_B} = \frac{F_{A \text{ on } B,x} + N_{W \text{ on } B,x} + F_{E \text{ on } B,x}}{m_B} = 0$$
- But $F_{E \text{ on } B,x} = 0$ because gravity only has a component in the vertical direction.

$$F_{A \text{ on } B,x} + N_{W \text{ on } B,x} = 0$$

$$F_{A \text{ on } B,x} = (21 \text{ N}) \cos 45^\circ = 14.8 \text{ N}$$

$$N_{W \text{ on } B,x} = -14.8 \text{ N}$$
 (it points in the $-x$ direction)

20

Determining Forces and Acceleration

- What is the acceleration in the y-direction?

$$a_{B,y} = \frac{F_{A \text{ on } B,y} + N_{W \text{ on } B,y} + F_{E \text{ on } B,y}}{m_B}$$
- There is no vertical component from the normal force:

$$N_{W \text{ on } B,y} = 0.$$
- Gravity exerts a force in the $-y$ direction:

$$F_{E \text{ on } B,y} = -(2.0 \text{ kg})(9.8 \text{ N/kg}) = -19.6 \text{ N}$$
- Vertical component due to Anna:

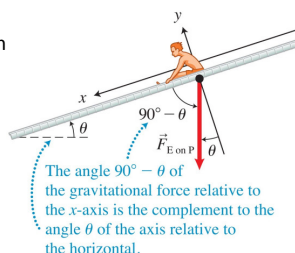
$$F_{A \text{ on } B,y} = (21 \text{ N}) \sin 45^\circ = 14.8 \text{ N}$$
- Acceleration:

$$a_{B,y} = \frac{-19.6 \text{ N} + 14.8 \text{ N}}{2.0 \text{ kg}} = -2.4 \text{ m/s}^2$$
- The book slides *down* the wall.

21

Incline Planes

- Gravity is always in the downward vertical direction
- The normal force is always perpendicular to a surface
- The motion is along the surface of the plane
- Sometimes it is easier to align the x-axis with the direction of motion rather than the usual horizontal direction:

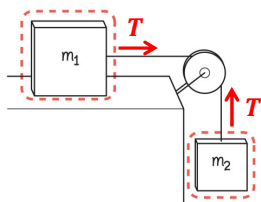


$$a_x = \frac{\sum F_x}{m} = \frac{(mg) \sin \theta}{m} = g \sin \theta$$

22

Tension in Strings

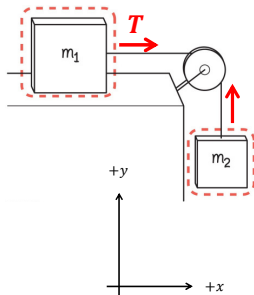
- We assume that strings will not stretch
 - Their length remains constant
- Strings can only pull... they can't push.
- The tension in a string, T , is the same everywhere.



23

Tension in Strings

- m_1 accelerates in the +x direction.
- m_2 accelerates in the -y direction.
- The magnitudes of the acceleration are equal because the string can't stretch.



24

Tension in Strings

- $a_1 = T/m_1$
- $a_1 = -a_2 = \frac{T - F_E \text{ on } m_2}{m_2}$

$$= \frac{T - m_2 g}{m_2} = -\frac{T}{m_1}$$

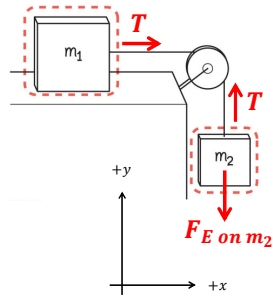
- Solve for the tension:

$$T \left(\frac{1}{m_2} + \frac{1}{m_1} \right) = g$$

$$T = g \left(\frac{m_1 m_2}{m_1 + m_2} \right)$$

- Substitute it in to solve for a :

$$a_1 = \frac{T}{m_1} = g \left(\frac{m_2}{m_1 + m_2} \right) = -a_2$$



25
