

Using Disorder to Detect Order: Hysteresis and Noise of Nematic Stripe Domains in High Temperature Superconductors

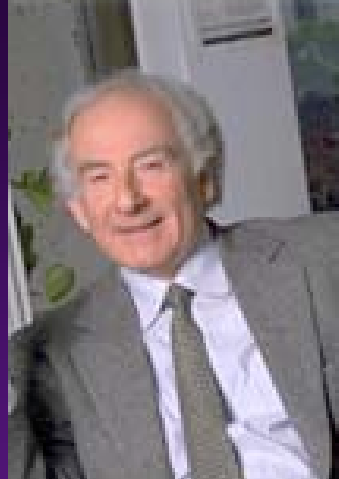
Erica Carlson
Karin Dahmen
Eduardo Fradkin
Steven Kivelson

Dale Van Harlingen
Michael Weissman
Christos Panagopoulos





John Bardeen



Leon Cooper



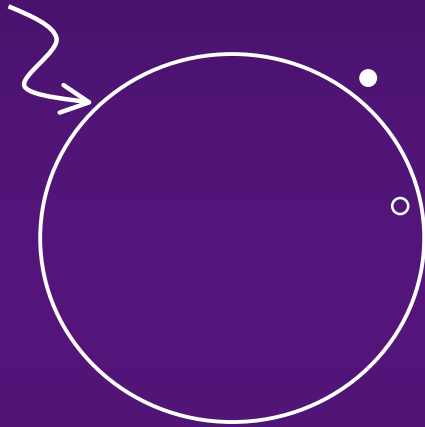
Bob Schrieffer

Conventional Superconductivity

- BCS Theory
- *Instability* of the metallic state

Simple Metals: The Fermi Gas

Fermi Surface

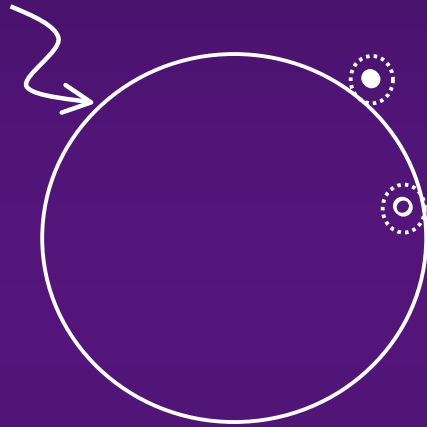


- Free Electrons $E \sim k^2$
- Pauli exclusion principle
- Fill to Fermi level

Adiabatically turn on temperature, most states unaffected
Very dilute gas of excitations: quasiparticles

Simple Metals: The Fermi Liquid

Fermi Surface



- Pauli exclusion principle
- Fill to Fermi level

Adiabatically turn on temperature, most states unaffected
Very dilute gas of excitations: quasiparticles

Fermi Gas + Interactions \rightarrow Fermi Liquid
Quasiparticles = Dressed Electrons

Kinetic Energy
Dominant

Cooper Pairing

- Fermi Liquid Unstable to Pairing
- Pair electrons near Fermi Surface
- Phonon mediated

Retardation is Essential
to overcome
Coulomb repulsion

$$\frac{E_F}{\omega_D} \approx 10^3$$

BCS Haiku:

祢

安

Instability

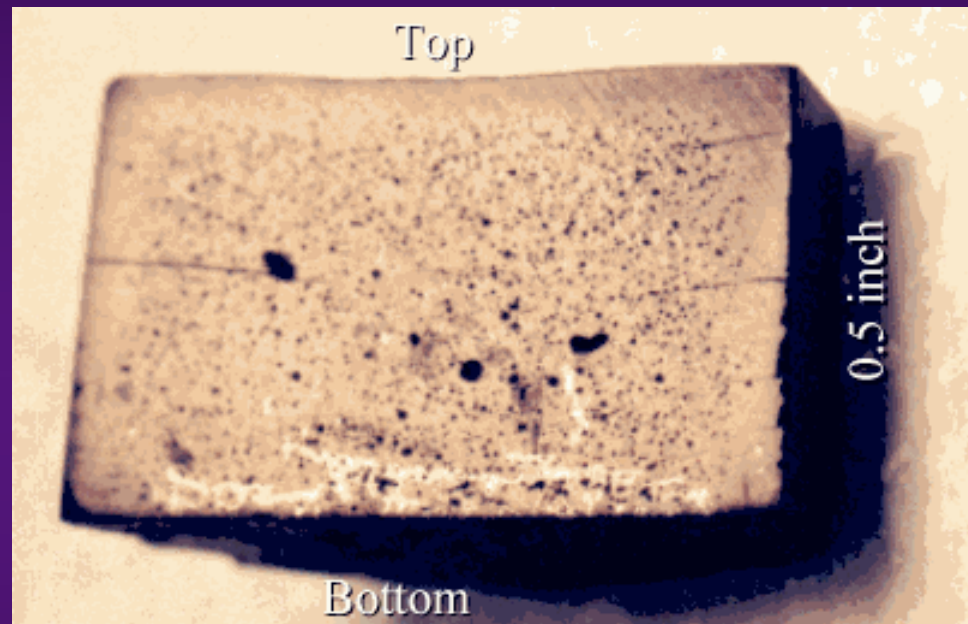
*Of A Tranquil Fermi Sea—
Broken Symmetry*

夢

美

A Ceramic Superconductor?

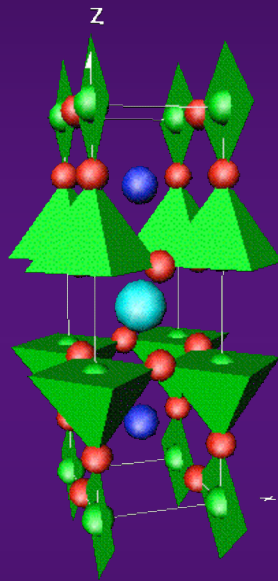
- Brittle
- Ceramic
- Not Shiny
- Not metallic



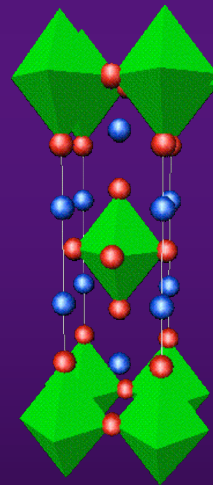
<http://www.superconductivecomp.com/>

- Why do they conduct at all?

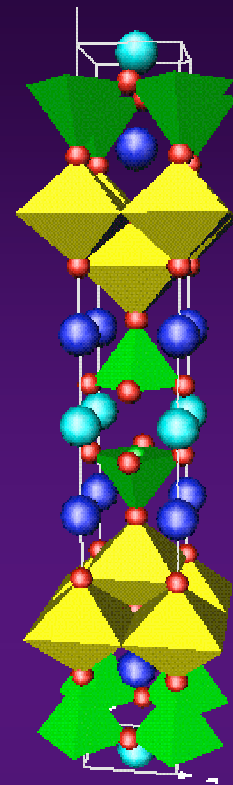
High Temperature Superconductors



YBCO₇

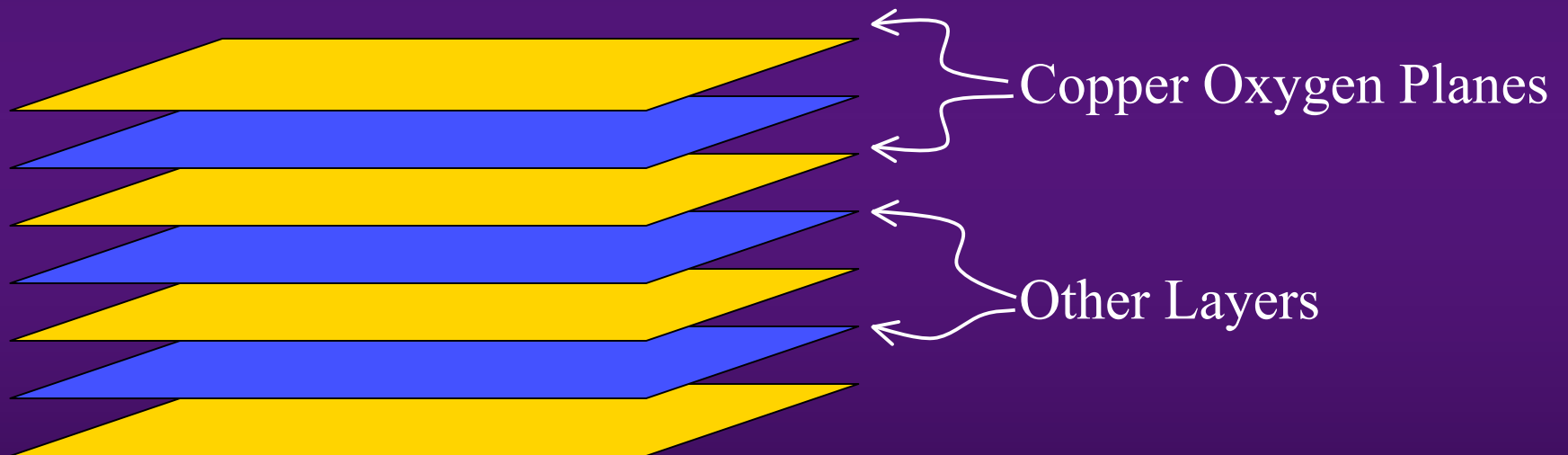


LSCO



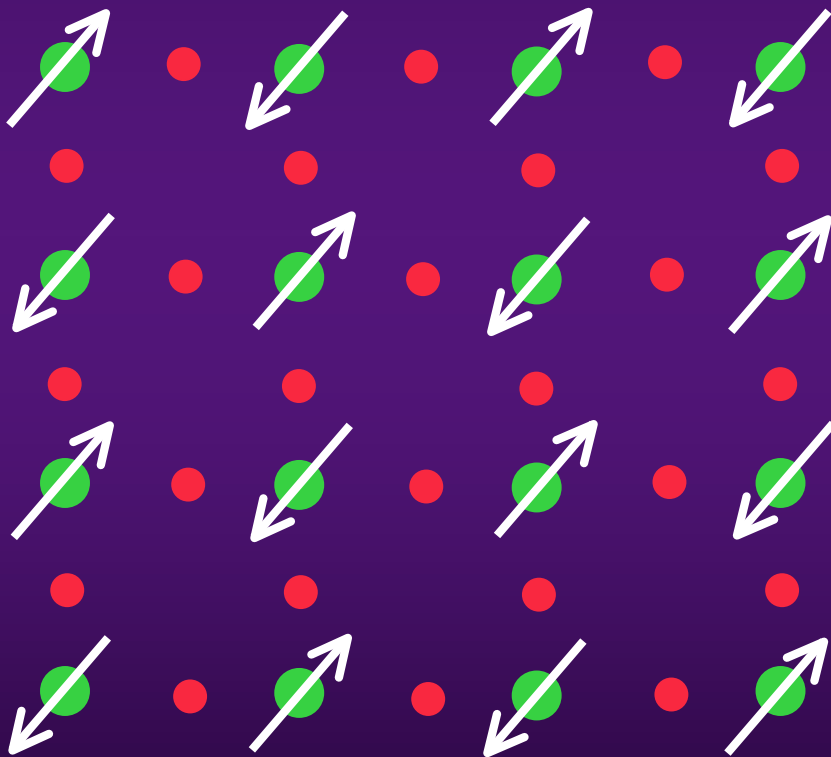
HgCuO

High Temperature Superconductors



Layered structure \rightarrow quasi-2D system

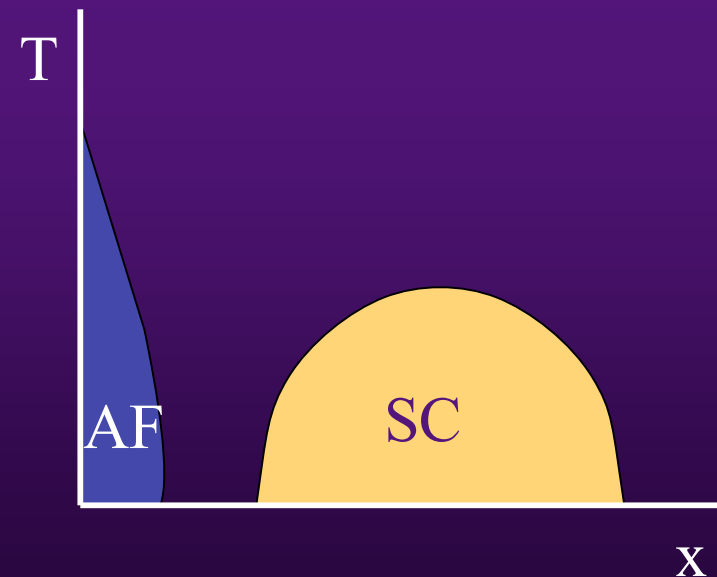
High Temperature Superconductors



● Oxygen ● Copper

Dope with holes

Superconducts at certain dopings



Mysteries of High Temperature Superconductivity

- Ceramic! (Brittle)
- “Non-Fermi liquid” normal state
- Magnetism nearby (antiferromagnetism)
- Make your own (robust)
<http://www.ornl.gov/reports/m/ornlm3063r1/pt7.html>
- Pseudogap
- Phase ordering transition

Two Energy Scales in a Superconductor

Two component order parameter

$$\psi = \Delta e^{i\theta}$$

Amplitude

Pairing
Gap

Phase

Phase Coherence
Superfluid Density

BCS is a mean field theory in which pairing precipitates order

Material	$T_{\text{pair}}[\text{K}]$	$T_c[\text{K}]$	$T_\theta[\text{K}]$
Pb	7.9	7.2	6×10^5
Nb ₃ Sn	18.7	17.8	2×10^4
UBe ₁₃	0.8	0.9	10^2
BaKBiO	17.4	26	5×10^2
K ₃ C ₆₀	26	20	10^2
MgB ₂	15	39	1.4×10^3

Phase Fluctuations
Important in Cuprates



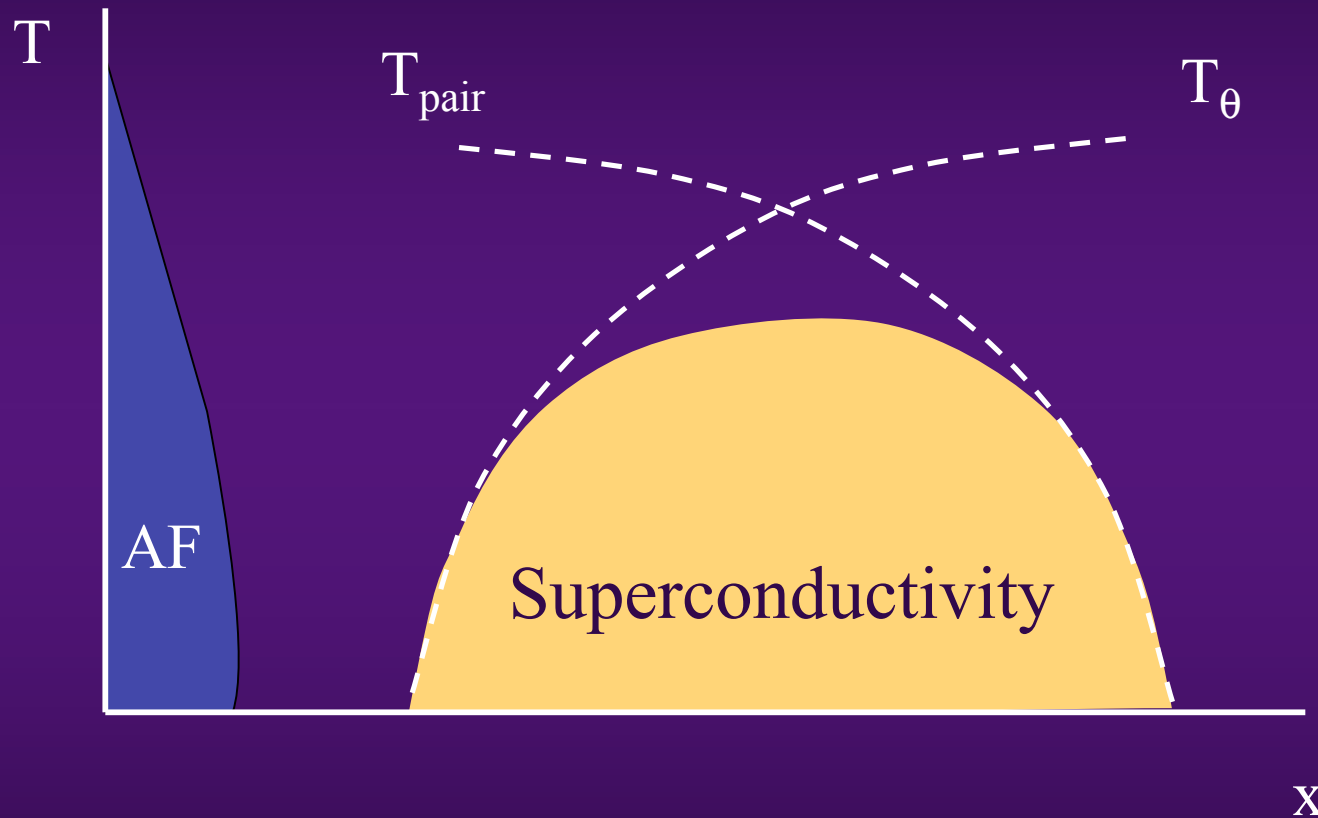
Material	$T_{\text{pair}}[\text{K}]$	$T_c[\text{K}]$	$T_\theta[\text{K}]$
LSCO (ud)	75	30	47
LSCO (op)	58	38	54
LSCO (od)		20	100
Hg-1201 (op)	192	96	180
Hg-1212 (op)	290	108	130
Hg-1223 (op)	435	133	130
Tl-2201 (op)	122	91	
Tl-2201 (od)		80	160
Tl-2201 (od)	26	25	
Bi-2212 (ud)	275	83	
Bi-2212 (op)	220	95	60
Bi-2212 (od)	104	62	
Y-123 (ud)		38	42
Y-123 (op)	116	90	140
Y-123 (od)	55	140	

Emery, Kivelson, Nature, **374**, 434 (1995)

EC, Kivelson, Emery, Manousakis, PRL **83**, 612 (1999)

EC, Emery, Kivelson, Orgad, in The Physics of Superconductors (2004)

T_c and the Energy Scales



BCS:

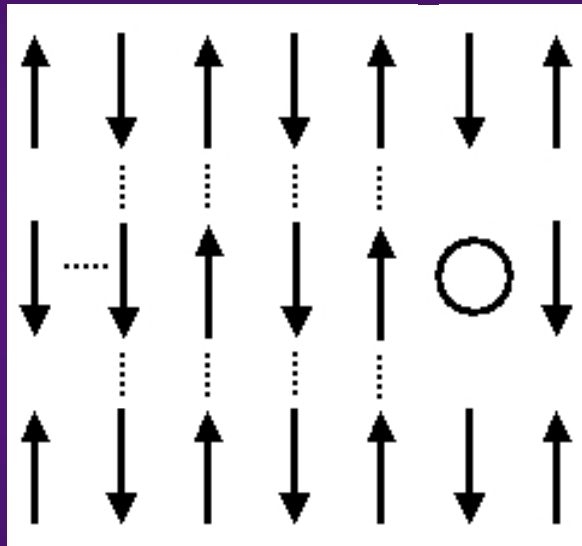
$$T_\theta \sim 1000 T_c$$

Very different from BCS.

HTSC:

$$T_\theta \sim T_c \text{ underdoped}$$

Doped Antiferromagnets



Hole Motion is Frustrated

Doped Antiferromagnets

- Compromise # 1: Phase Separation
- Relieves some KE frustration



The diagram consists of two adjacent rectangular boxes. The left box has a gray and white checkerboard pattern and contains the text 'Pure AF'. The right box is solid white and contains the text 'Hole Rich'.

**Pure
AF**

**Hole
Rich**

Like Salt Crystallizing
From Salt Water,
The Precipitate (AF) is Pure

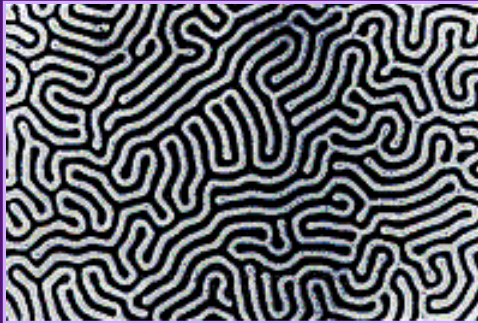
Coulomb Frustrated Phase Separation

- Long range homogeneity
- Short range phase separation
- Compromise # 2: *mesoscale structure*
- Patches interleave
- quasi-1D structure – stripes ?



Competition often produces stripes

Holes want to phase separate (run away), but Coulomb repulsion prevents it. Competition produces local inhomogeneity.



Ferrofluid
confined between
two glass plates
Period $\sim 1\text{cm}$



Ferromagnetic
garnet film
Faraday effect
Period $\sim 10^{-5}\text{ m}$



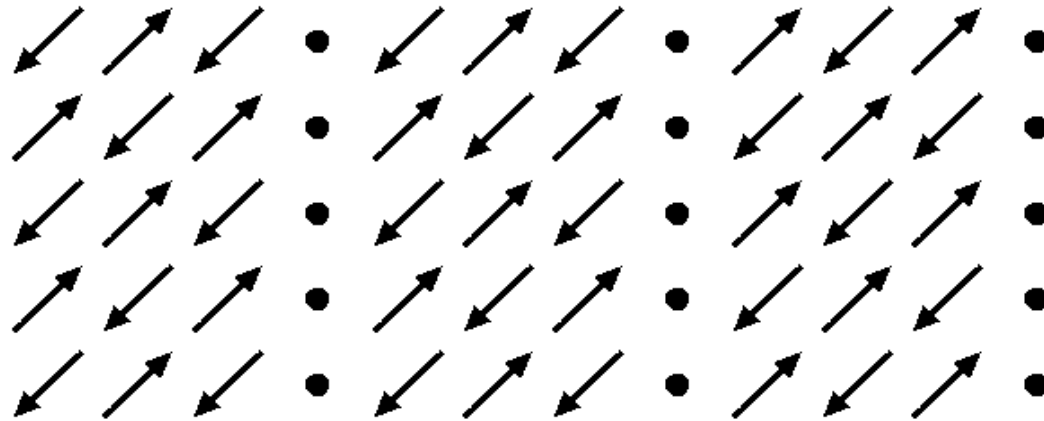
Ferromagnetic
garnet film
Period $\sim 10^{-5}\text{ m}$



Block copolymers
Period $\sim 4 \times 10^{-8}\text{ m}$



What's so special about 1D?



Liquid-like electrons here have new behavior due to 1D

Two types of solitons:

Charge Solitons

Spin Solitons

The electron is no longer a stable many-body excitation

Pair spins directly, no Coulomb repulsion = Pairs at high temperature!

Stripe Issues

Why do we care?

Novel electronic phases: liquid crystals

May shed light on High T_c (route to pairing mechanism)

Issues about stripes in HTSC:

Are they there?

Are they ubiquitous?

What constitutes evidence of them?

Hard to detect!

Disorder (chemical dopants)

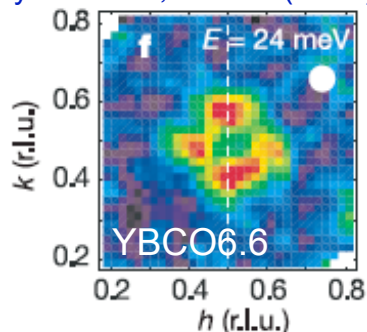
Rounds transitions

Destroys order!

<p>How do we define and detect “order” in the presence of severe disorder effects?</p>
--

Stripes in what probes?

Hayden *et al.*, Nature (2004)

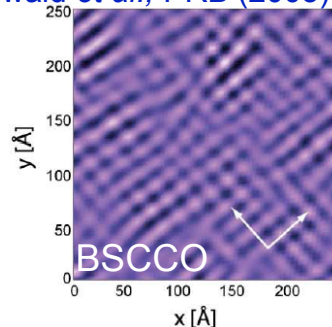


Neutron Scattering

(bulk probe)

LaSrCuO, LaCuO, YBaCuO (not BiSrCaCuO)

Howald *et al.*, PRB (2003)

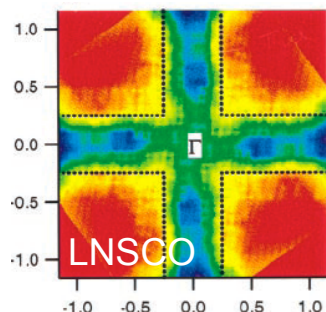


Scanning Tunneling Microscopy

(surface probe)

BiSrCaCuO

Zhou *et al.*, Science (1999)



Angle-Resolved Photoemission Spectroscopy

(surface probe)

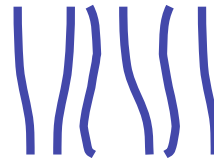
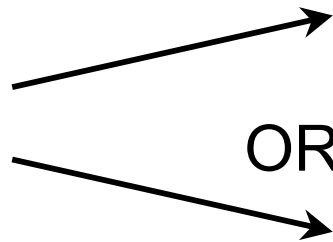
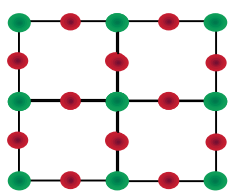
BiSrCaCuO, YBaCuO

Data not clear cut. Different probes for different materials.
We propose new ways to look for stripes.

Finding Electronic Stripes: Ising Symmetry

Stripes lock to a crystal direction

Cu-O plane



Horizontal
or
Vertical

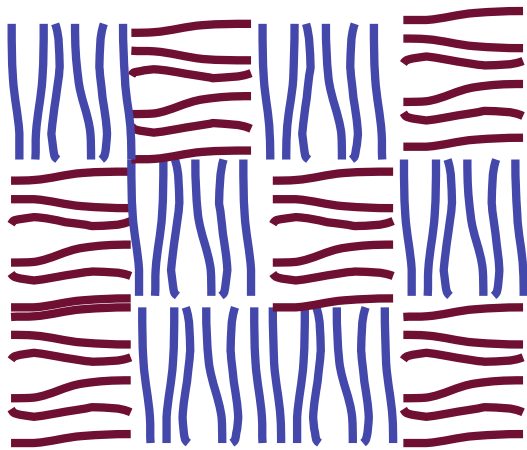
$$H = -J \sum_{\langle i,j \rangle} \sigma_i \sigma_j \quad \text{"Ising Model"}$$

$\sigma = 1$ for horizontal stripe patch

$\sigma = -1$ for vertical stripe patch

Finding Electronic Stripes: Disorder is a Random Field

Disorder favors one direction locally



$$H = -J \sum_{\langle i,j \rangle} \sigma_i \sigma_j - \sum_i (H + h_i) \sigma_i$$

RANDOM FIELD ISING MODEL

Random Field Ising Model in 3D



- Snap: One large, system-size event
- Crackle: Many events at random times, of random sizes.
- Pop: Many small, same-sized events at random times

3D RFIM has phase transition
from “Snap” to “Pop” with “Crackle” at criticality.

Many Things Crackle

Paper



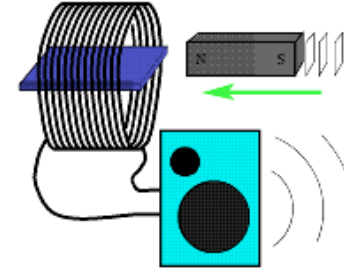
Earthquakes



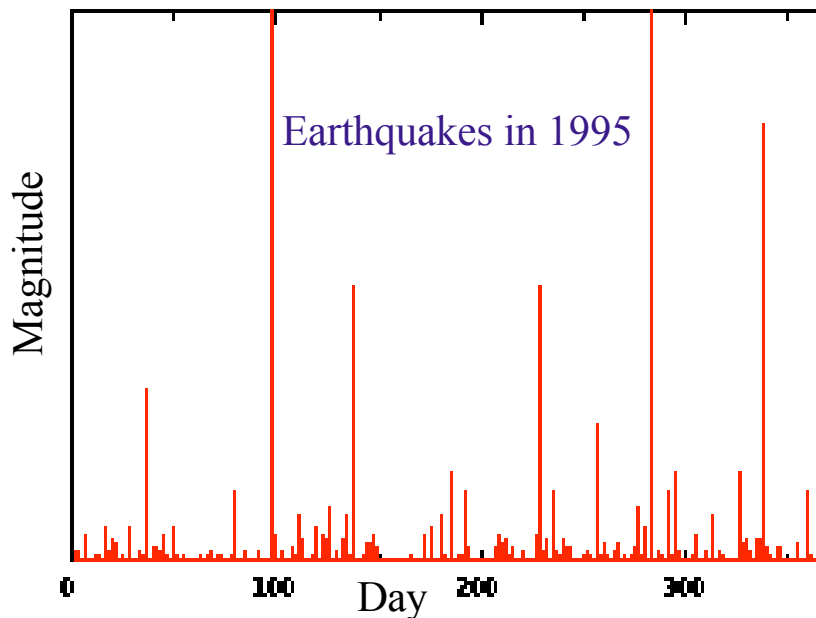
Rice Crispies



Magnets

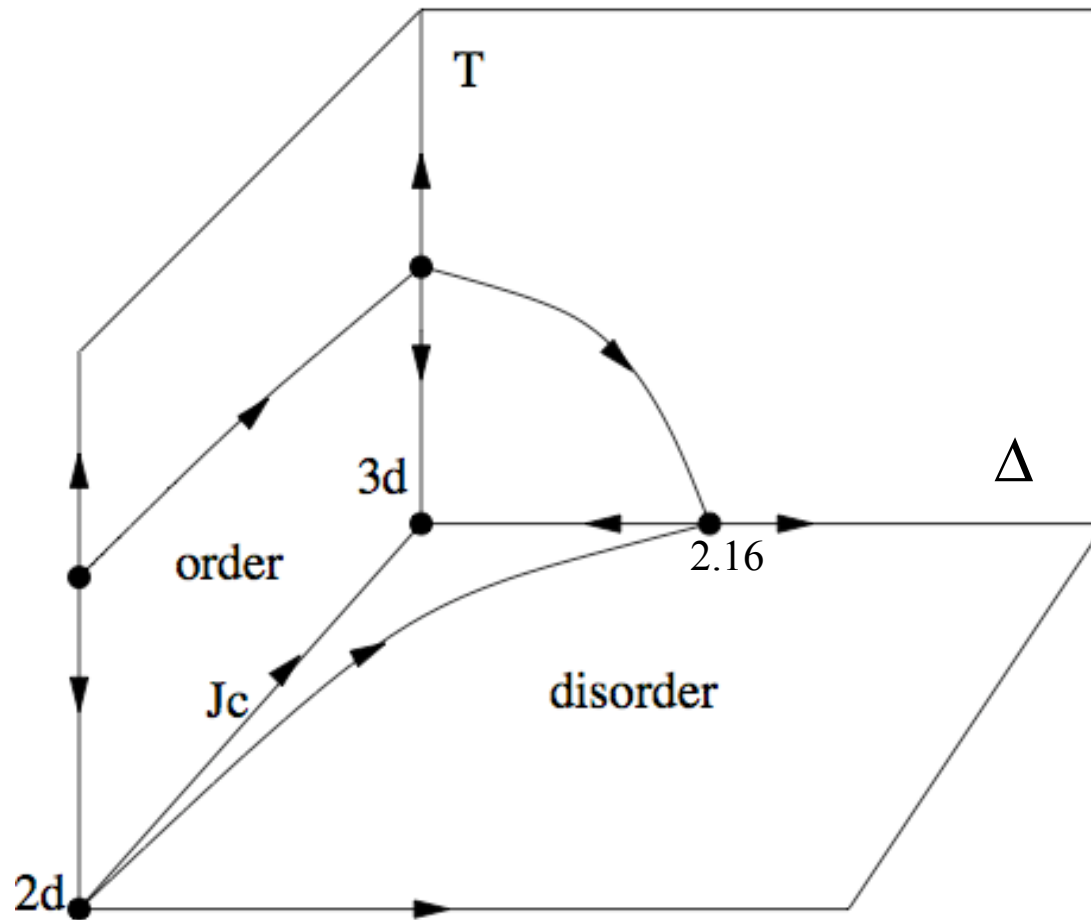


Crackling: Random times, random sizes.

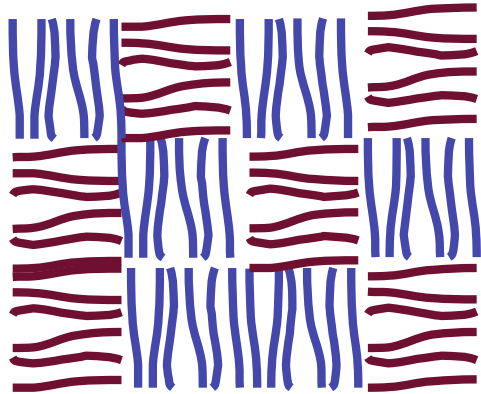


Large critical region in 3D RFIM
(Perkovic, Dahmen, and Sethna, PRL 1995)

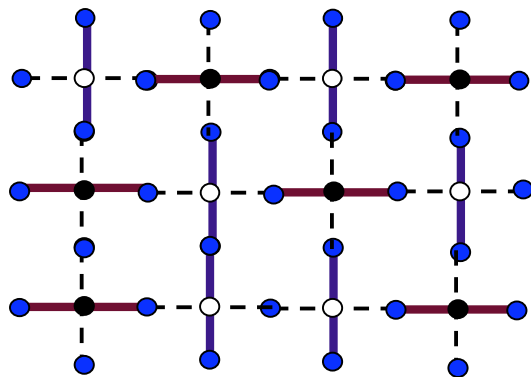
Layered RFIM



Mapping to Random Resistor Network



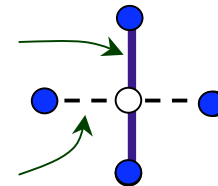
Stripe Patches



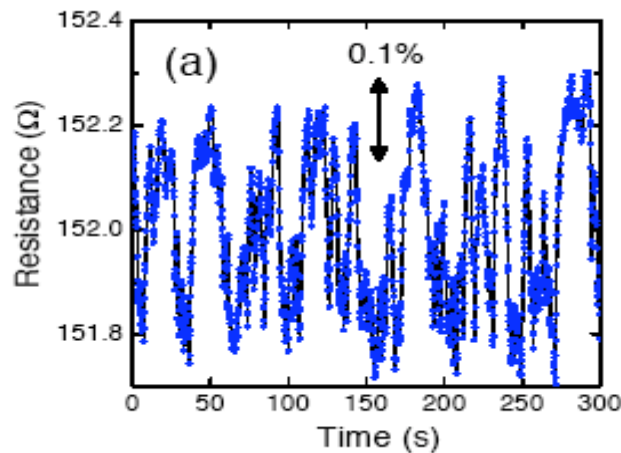
Resistor Network

Easy conduction

Hard conduction



Noise in Resistance

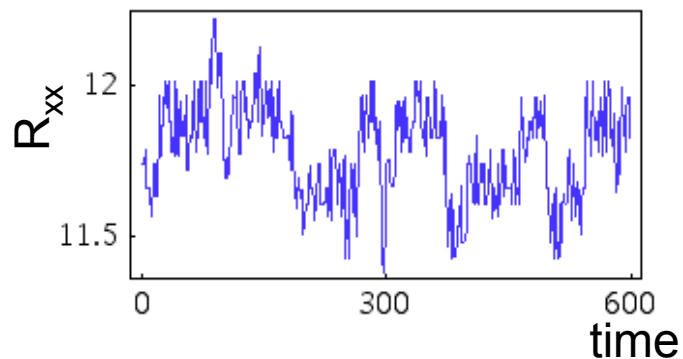


Experiment

YBCO nanowire (underdoped)
 $T=100\text{K}$ $500\text{nm} \times 250\text{nm}$

Bonetti, Caplan, Van Harlingen,
Weissman., Phys. Rev. Lett. 2004

Theory

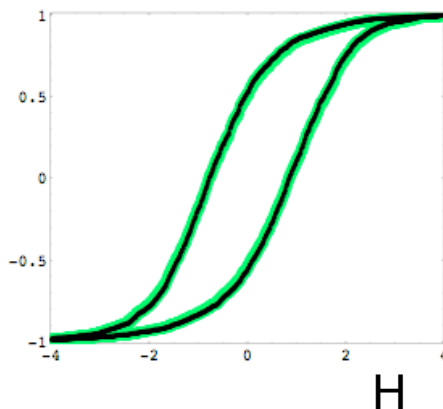
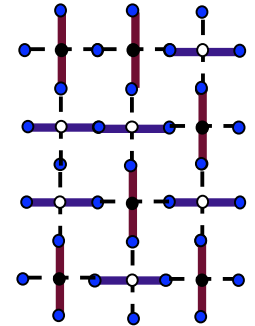


- Local patch anisotropy: 2
- Size: 10×10 patches
- Disorder $R=2.8$ J
- $T = .5$ J
- Dimension = 2
- Stripe correlation length
~ 40nm (from neutron data)

Macroscopic Resistance Anisotropy

Resistance Anisotropy and RFIM Magnetization exhibit hysteresis

“Magnetization” = orientational order

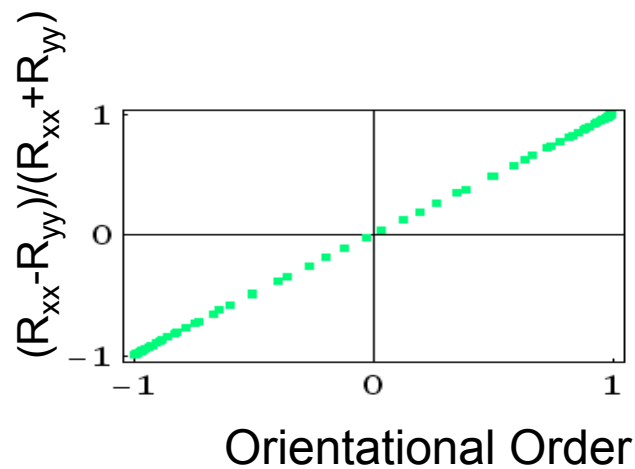


■ Orientational Order

■ $(R_{xx}-R_{yy})/(R_{xx}+R_{yy})$

LXL = 100X100 $R_{\text{large}}/R_{\text{small}} = 2$

T=0; R = 3 J; Dimension = 2

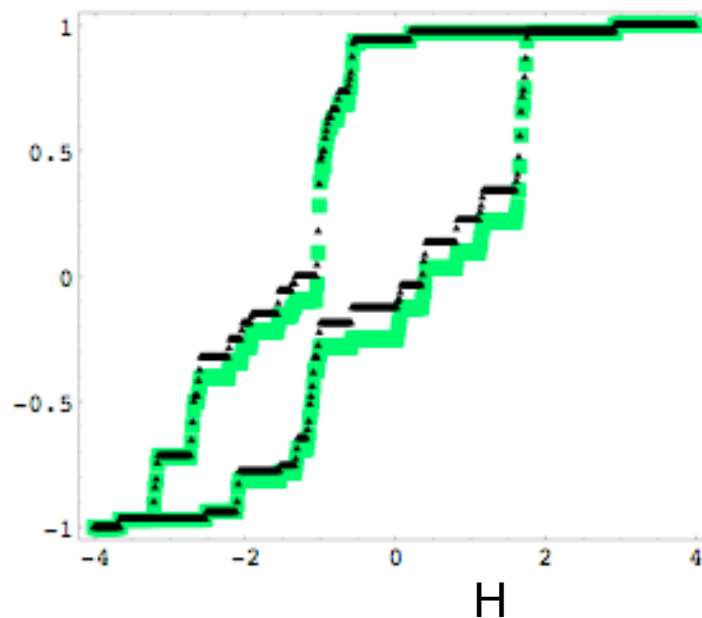
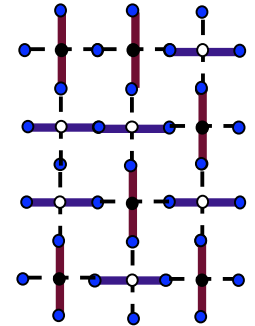


Resistance Anisotropy
 \approx Orientational Order

Macroscopic Resistance Anisotropy

Resistance Anisotropy and RFIM Magnetization exhibit hysteresis

“Magnetization” = orientational order



■ Orientational Order

■ $(R_{xx}-R_{yy})/(R_{xx}+R_{yy})$

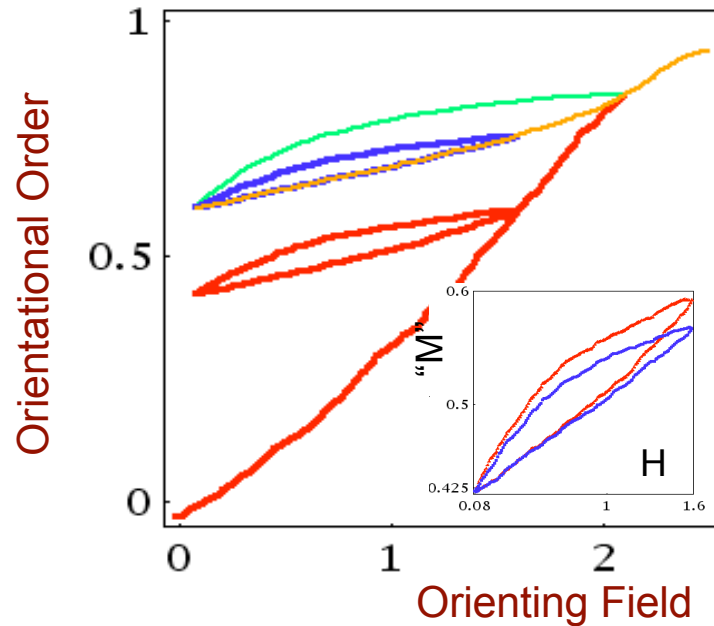
LXL = 8X8

T=0; R = 3 J;

$R_{\text{large}}/R_{\text{small}} = 2$

Smaller system -- more fluctuations.

Hysteresis And Subloops



Theory

- Return Point Memory (subloops close)
- Incongruent Subloops → Interactions important
- Disorder $R=3J$, $T=0$, Size = 100X100

Orientational Order



{ Resistance Anisotropy
Superfluid Anisotropy
Ratio of IC peaks in neutron scattering, STM

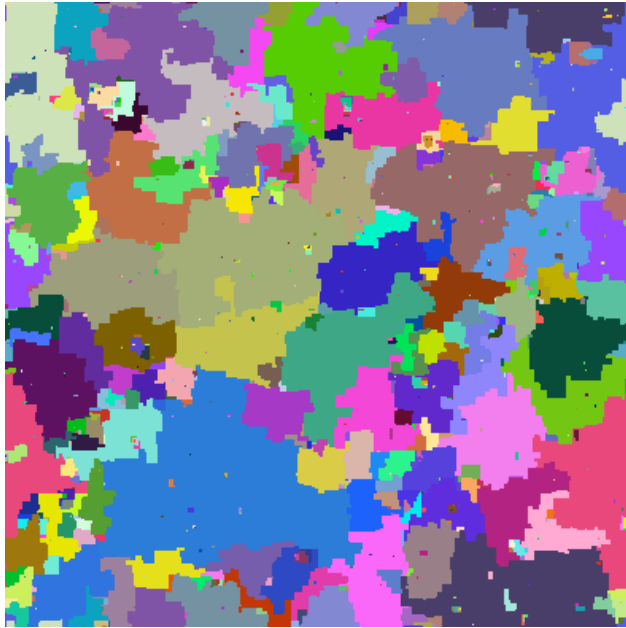
Orienting Field



{ Magnetic Field H^2
Uniaxial Strain
High Current

New STM mode: Scanning Noise Spectroscopy

Map of crackling clusters



Sethna, Dahmen, Perkovic, cond-mat/0406320

Each cluster has characteristic dynamics.
Small clusters flip often,
and large clusters flip much less often.

Position-dependent power spectrum can
map out the cluster pattern.

Conclusions

High Temperature Superconductors: Need a fundamentally different mechanism from BCS

Stripes: 1D System has *spin-charge separation*

Pair spins directly to achieve high pairing scale despite large Coulomb repulsion

Stripes + Host crystal + Disorder = Random Field Ising Model

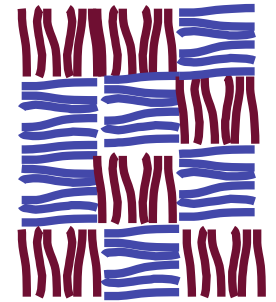
Disorder makes stripes hard to detect -- need new probes. *Noise, Hysteresis*

Transport: Switching noise in small systems in R_{xx}

Orientalional Order measured by $R_{xx}-R_{yy}$

Hysteresis, Return Point Memory at low T

Subloops Incongruent \Rightarrow Interactions important



Scanning Noise Spectroscopy:

Power spectrum of local noise can map out the cluster pattern

Hysteresis:

Resistance Anisotropy

Superfluid Anisotropy

Ratio of IC peaks in neutron scattering, STM

vs.

Magnetic Field H^2

Uniaxial Strain

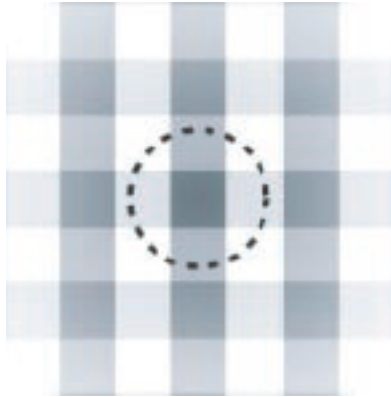
High Current

What's so special about 1D?

→ *solitons*

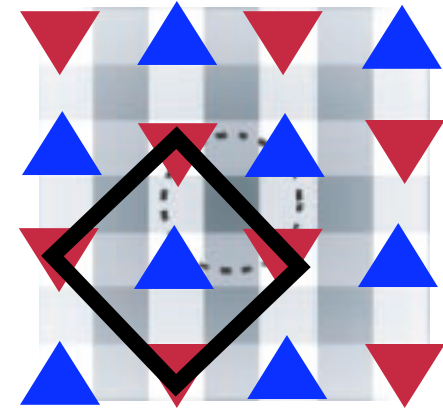
Disturbances in 3D:	dissipate as $\sim 1/R^2$	Like the intensity of light
Disturbances in 2D:	dissipate as $\sim 1/R$	Like a stone thrown in a pond
Disturbances in 1D:	“dissipate” as ~ 1	Like a wave in a canal

Checkerboards and Plaids?

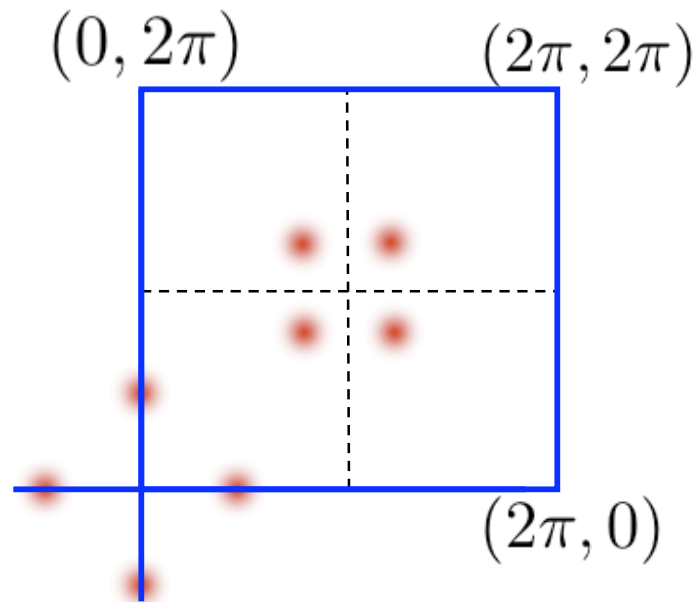


Hoffman *et al.*, Science (2002)
Vershinin *et al.*, Science (2004)

**Antiphase
Domain Walls in
Antiferromagnetism**

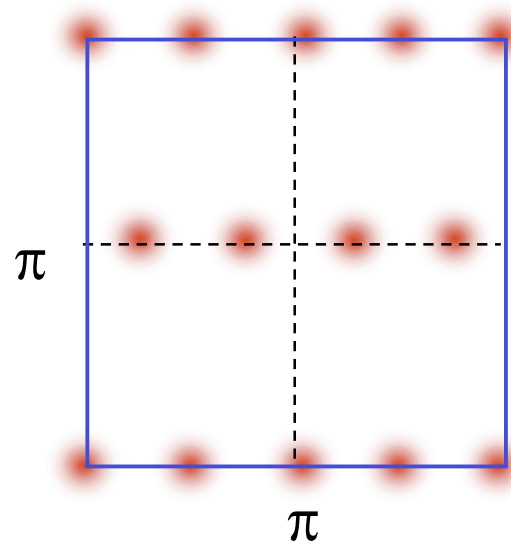
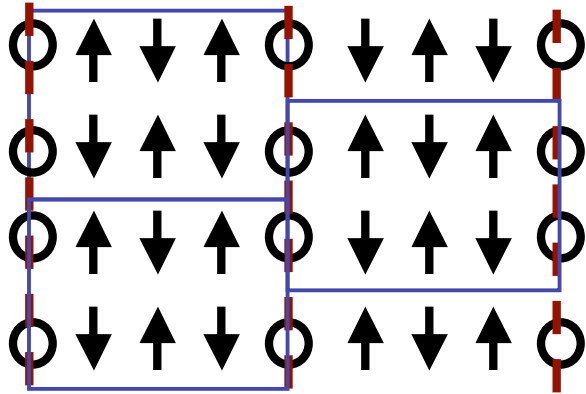


**Charge
Peaks**



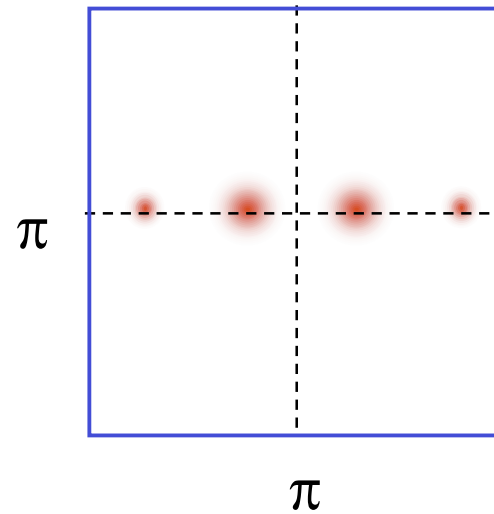
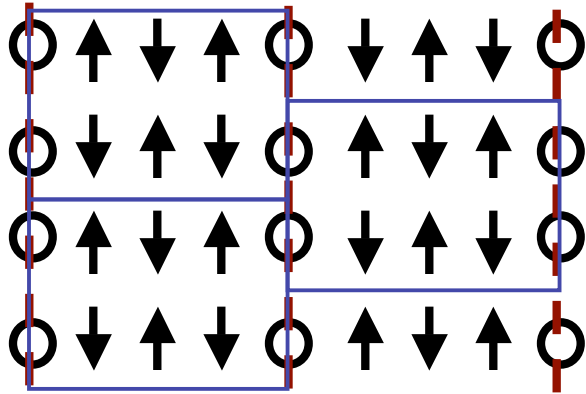
**Spin Peaks in
Wrong Direction!**

Neutron Scattering



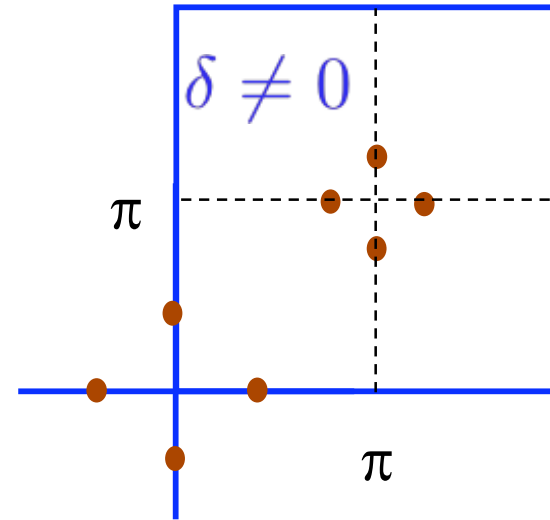
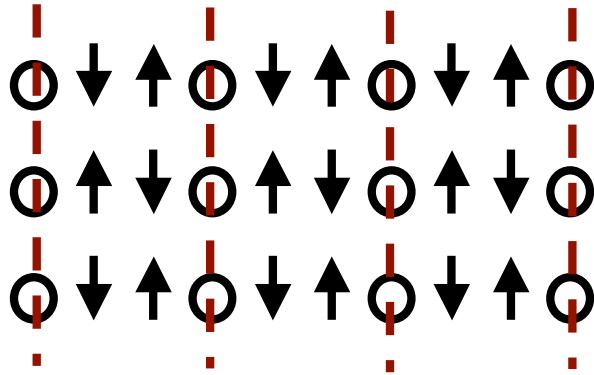
**Magnetic
Reciprocal
Lattice
Vectors**

Neutron Scattering



Intensities

Neutron Scattering in Cuprates



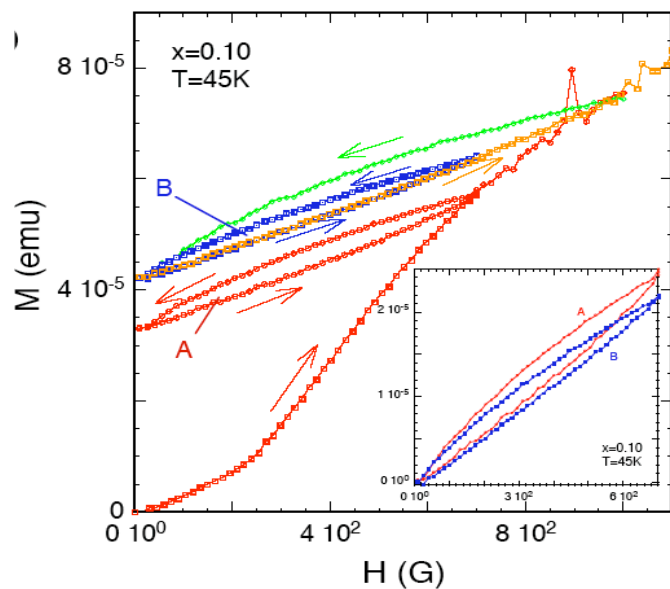
Charge Peaks related by X2

Data is usually twinned due to crystal twinning.

LaSrCuO, LaCuO

YBaCuO

Hysteresis Subloops



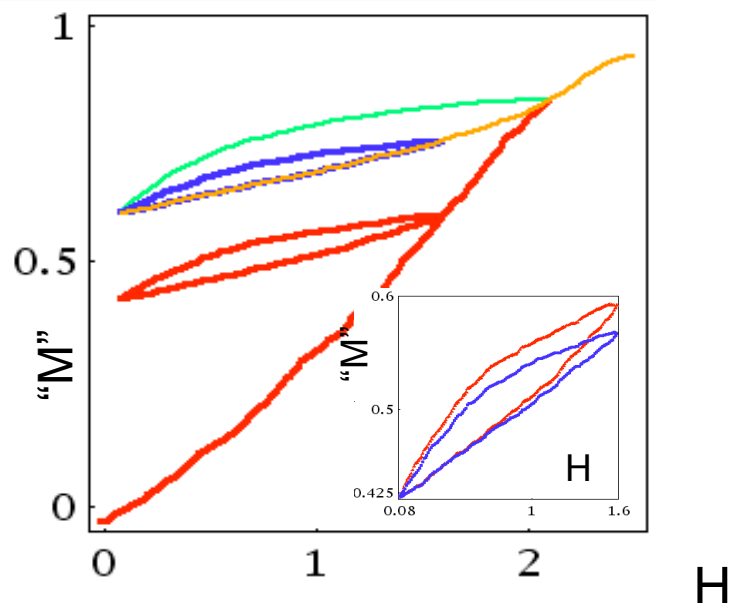
Experiment

LSCO, $X=.10$

ZFC, ZFW

$T=45K$

Panagopoulos *et al.*,
cond-mat/0412570



Theory

- Return Point Memory (subloops close)
- Incongruent Subloops → Interactions important
- Disorder $R=2.8J$, $T=0$,
Size = 100X100

Definitions

$$T_{\text{pair}} = \Delta/2 \quad (\Delta = \text{single particle gap})$$

$$T_{\theta} = \frac{1}{2} A \frac{\hbar^2 n_s}{m^*} L^{d-2} \quad (n_s = \text{superfluid density})$$

$$L = \sqrt{\pi} \xi_o$$

$$\text{3D:} \quad A = 2.2 \quad \frac{n_s}{2m^*} = \frac{c^2}{8\pi e^2 \lambda^2}$$

$$\text{2D:} \quad A = 0.9 \quad \frac{n_s}{2m^*} = \frac{c^2 L}{8\pi e^2 \lambda^2}$$

