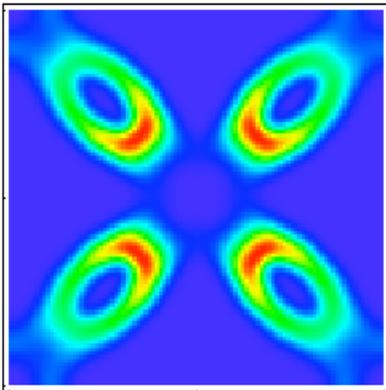
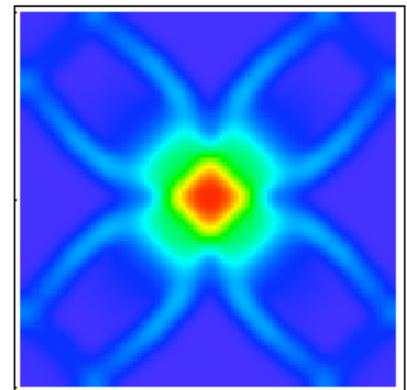


Magnetic Excitations of Stripes



E. W. Carlson
D. X. Yao
D. K. Campbell



Stripes: Why?

HTSC Dilemmas

Superconductivity from a **non-Fermi liquid**

High pairing scale despite **strong repulsion**

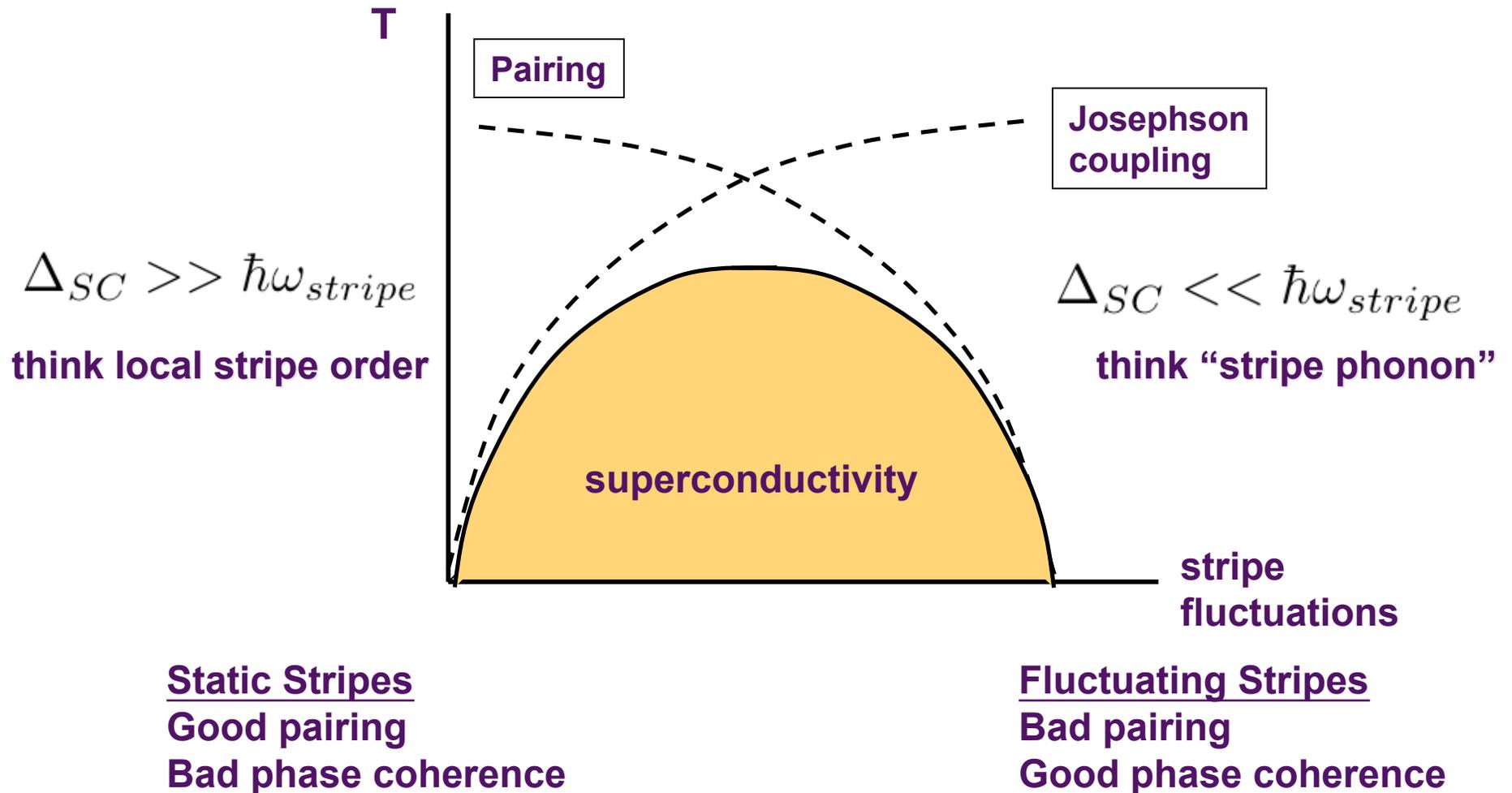
Metallic Charge Stripes: Spin-Charge Separation

Non-Fermi liquid normal state (Luttinger liquid)

Pair the spin degrees of freedom,
and avoid the Coulomb repulsion.

EC, V. Emery, S. Kivelson, D. Orgad
in "Physics of Unconventional Superconductors"
ed. Bennemann and Ketterson, (2004)

Inherent Competition



EC, V. Emery, S. Kivelson, D. Orgad
in “Physics of Unconventional Superconductors”
ed. Bennemann and Ketterson, (2004)

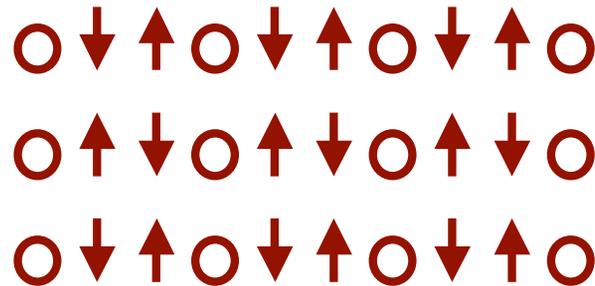
Stripes

Unidirectional modulation in charge and spin

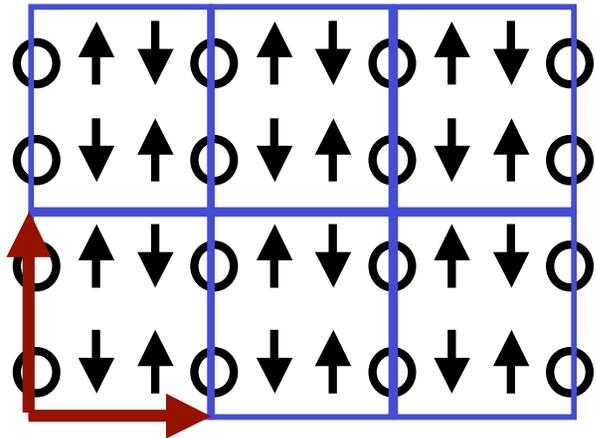


Charge: quasi-one-dimensional (rivers of charge)

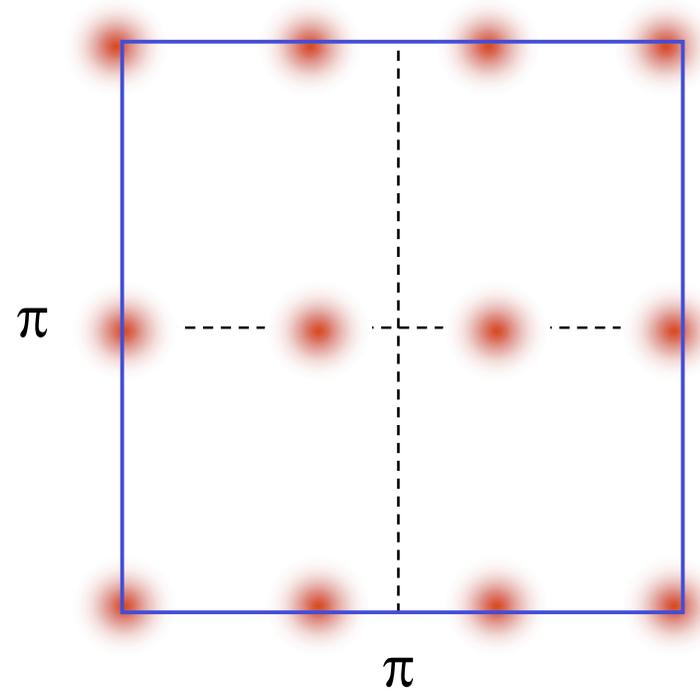
Spin: 2D Magnetic texture



Stripes Have 2D Magnetic Texture



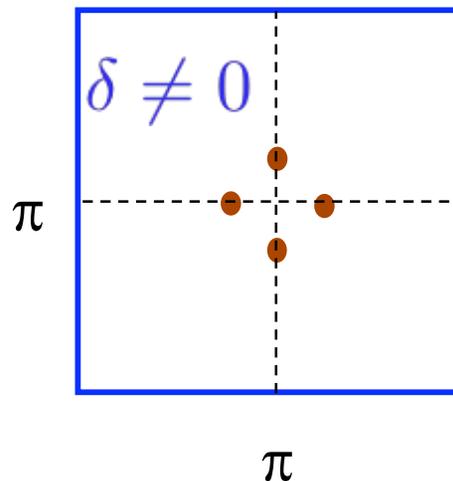
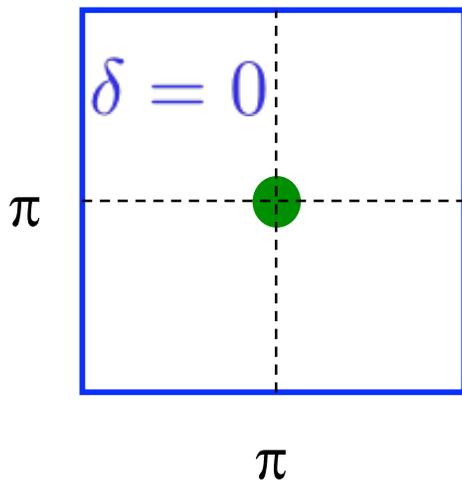
Real Space



Reciprocal Lattice
Vectors

2D spin waves disperse out of the reciprocal lattice vector positions

Neutron Scattering in Cuprates and Nickelates

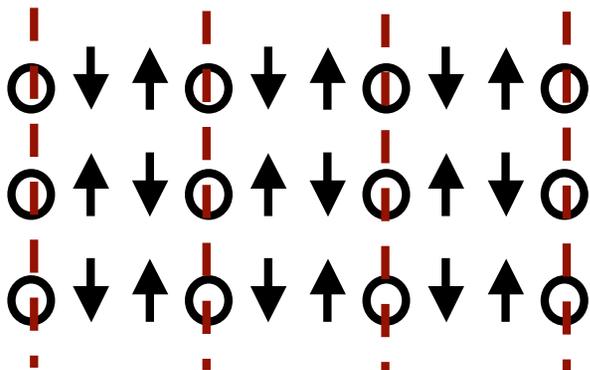


Disappearance of (π, π) peak
with doping

Appearance of satellite
peaks

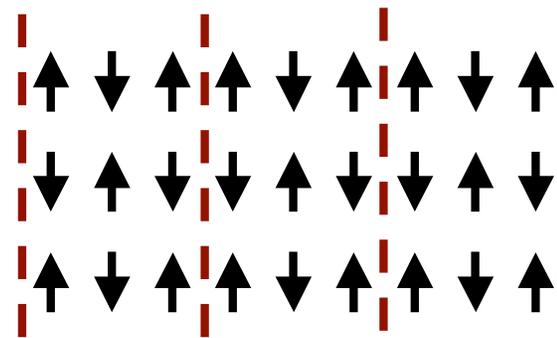
AFM signal averages to zero
antiphase domain walls

site-centered

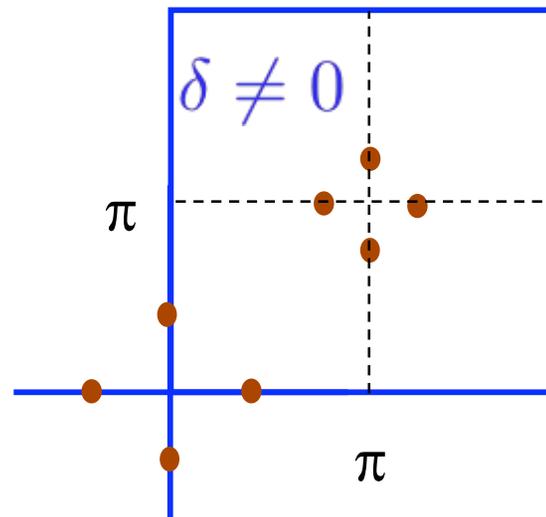


OR

bond-centered

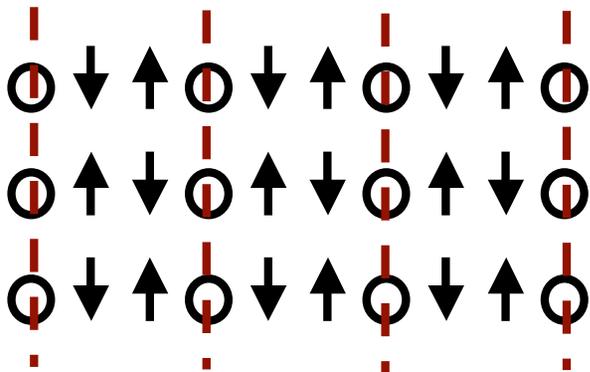


Neutron Scattering in Cuprates and Nickelates



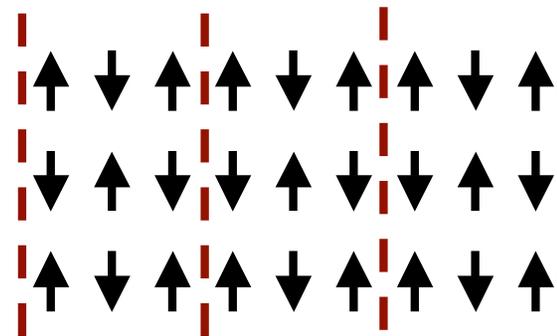
Charge Peaks
related by X2

site-centered

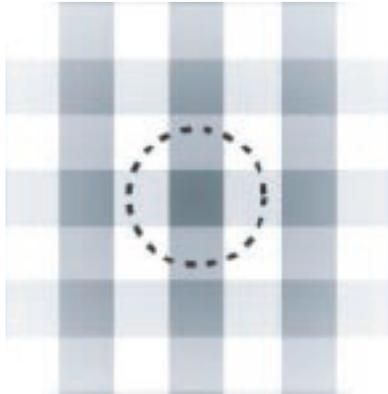


OR

bond-centered

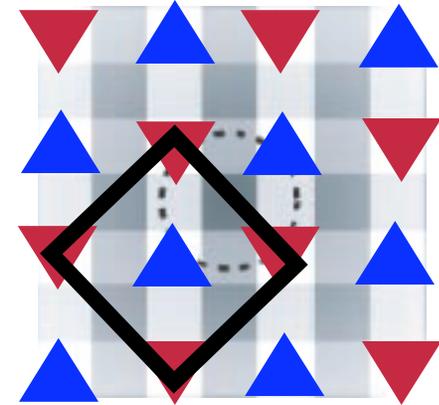


Checkerboards and Plaids?

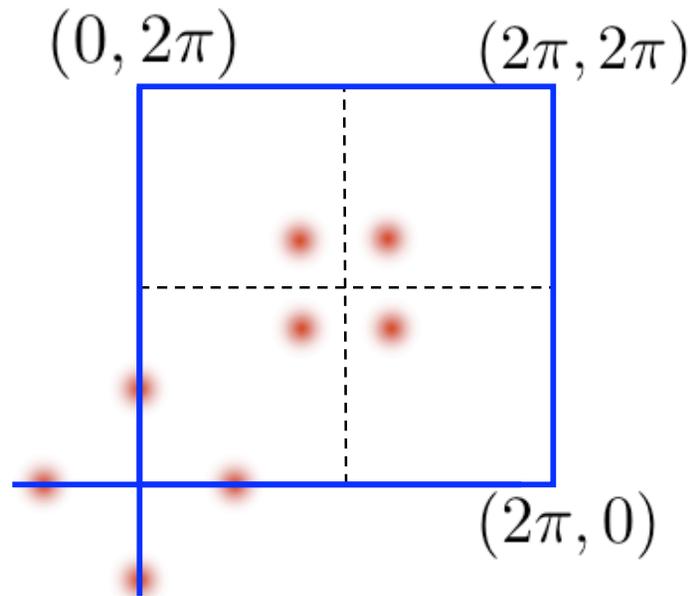


Hoffman *et al.*, Science (2002)
Vershinin *et al.*, Science (2004)

**Antiphase
Domain Walls in
Antiferromagnetism**



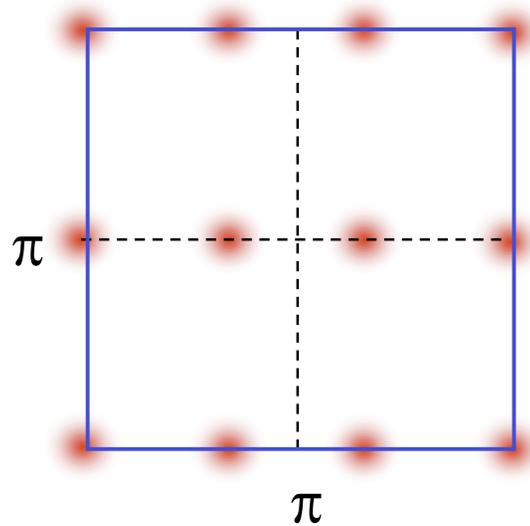
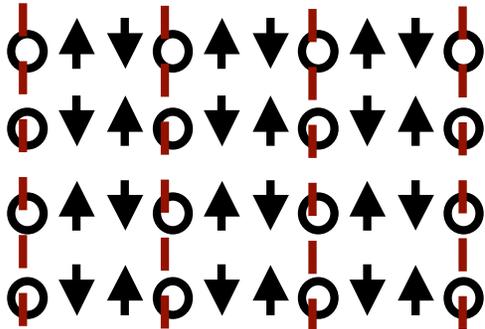
**Charge
Peaks**



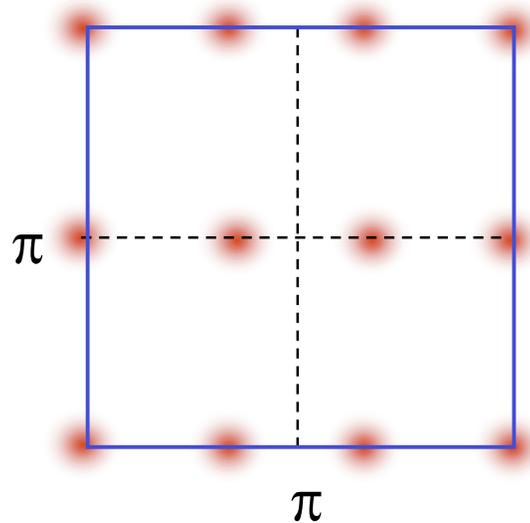
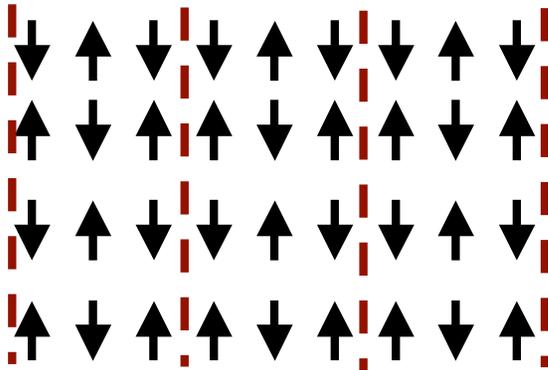
**Spin Peaks in
Wrong Direction!**

Odd Spacing

Site-centered



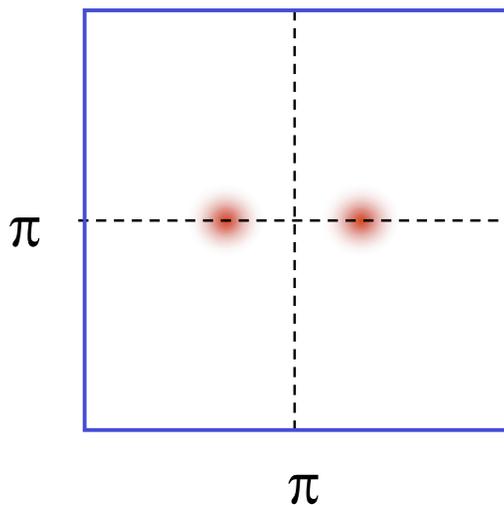
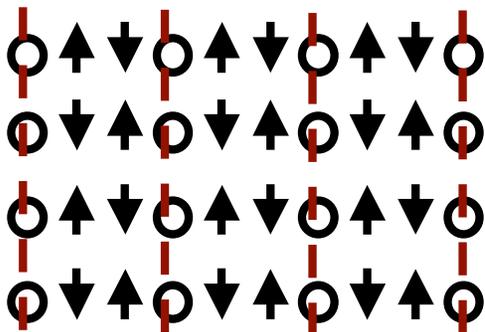
Bond-centered



**Magnetic
Reciprocal
Lattice
Vectors**

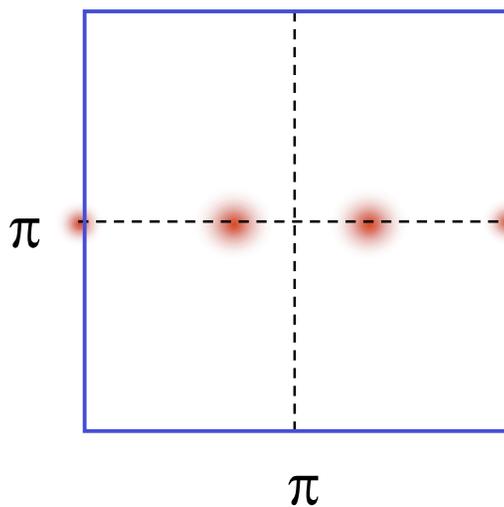
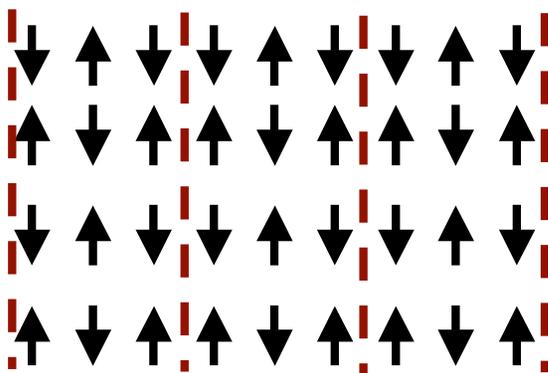
Odd Spacing

Site-centered



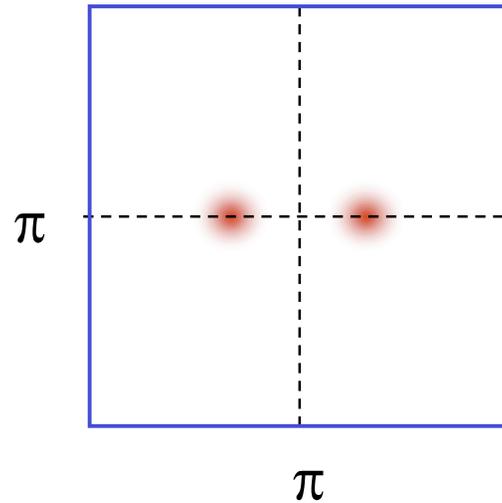
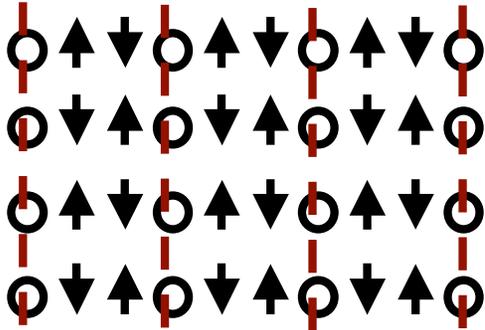
Intensities

Bond-centered

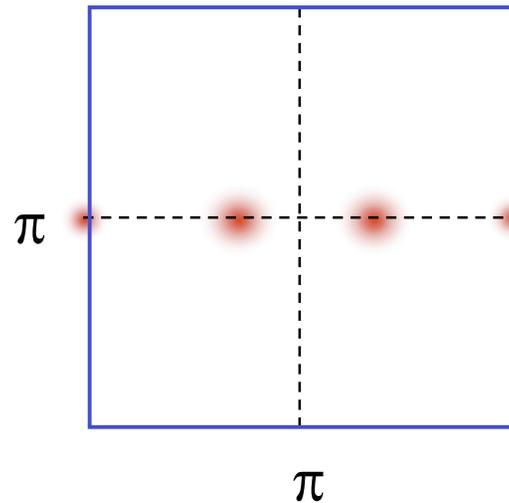
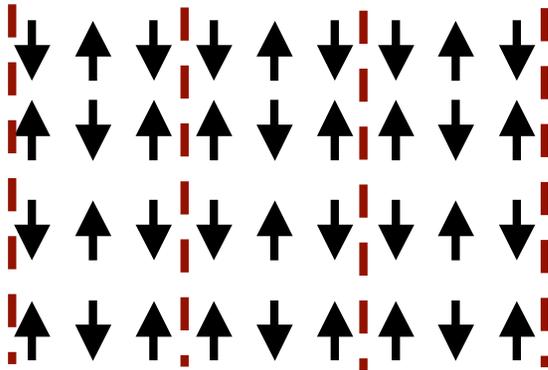


Odd Spacing

Site-centered



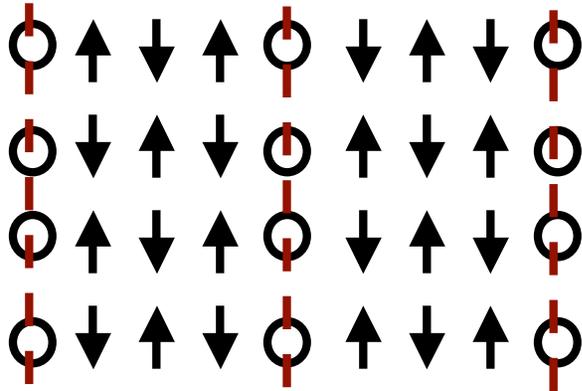
Bond-centered



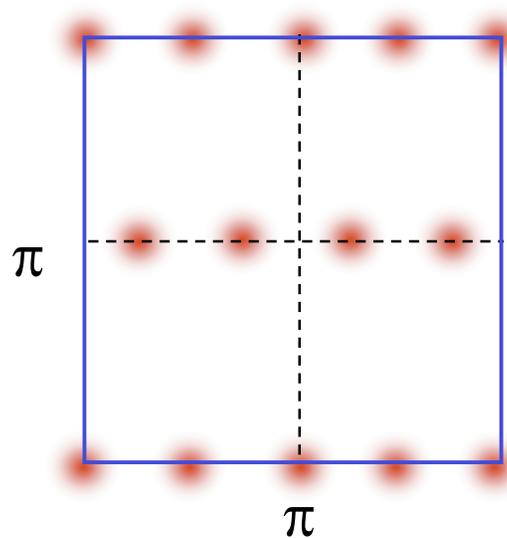
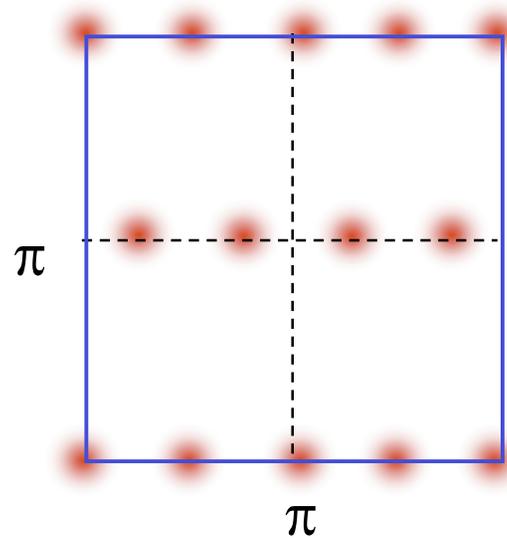
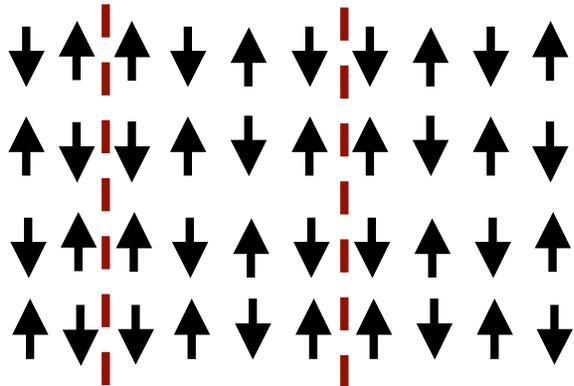
Observing weight here rules out site-centered stripes

Even Spacing

Site-centered



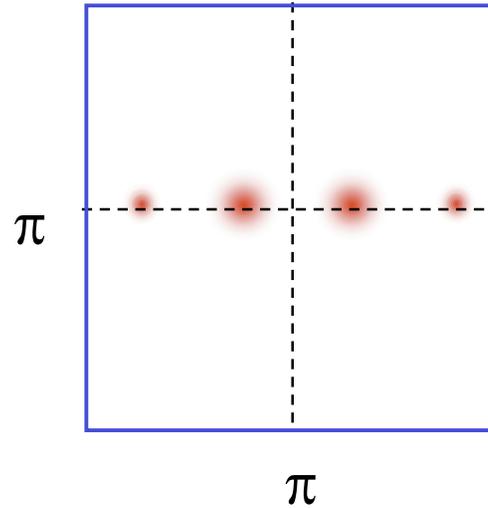
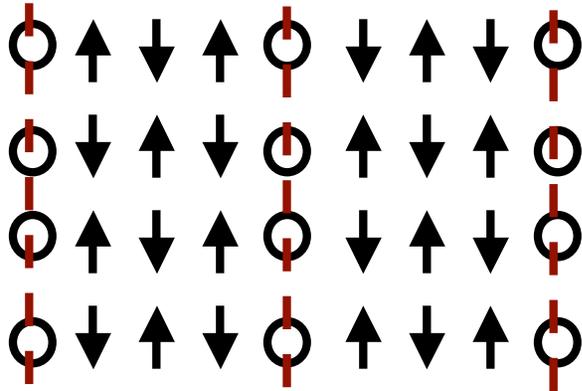
Bond-centered



**Magnetic
Reciprocal
Lattice
Vectors**

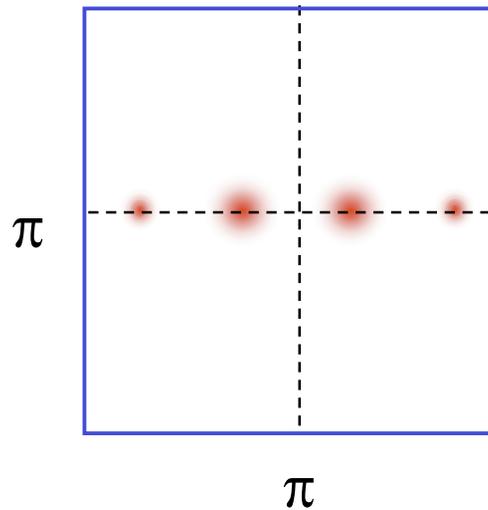
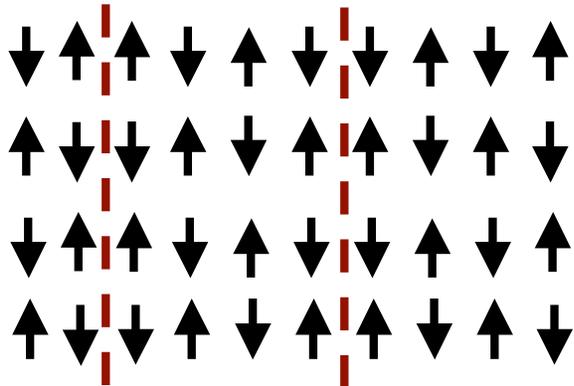
Even Spacing

Site-centered



Intensities

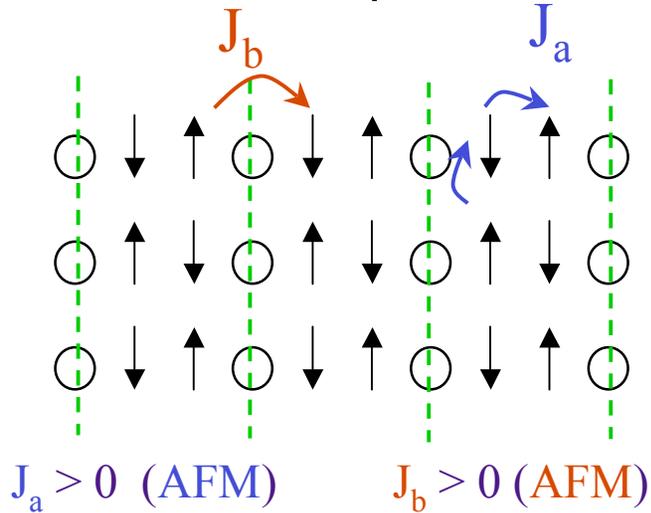
Bond-centered



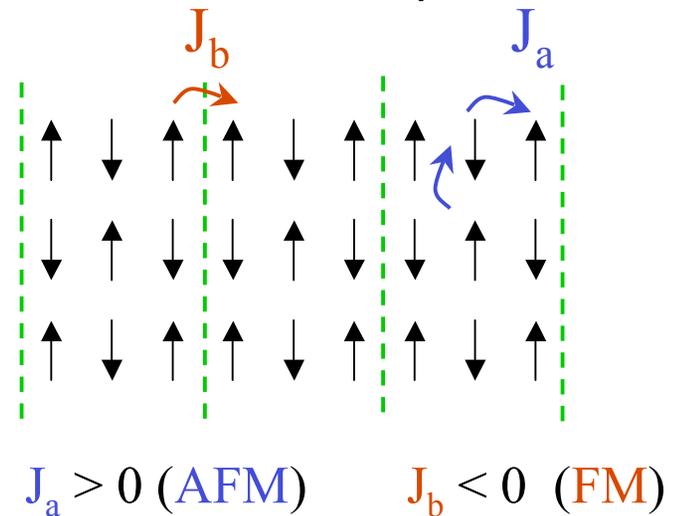
Inelastic Response: Spin Waves

Site or Bond-Centered

Site-centered p=3



Bond-centered p=3

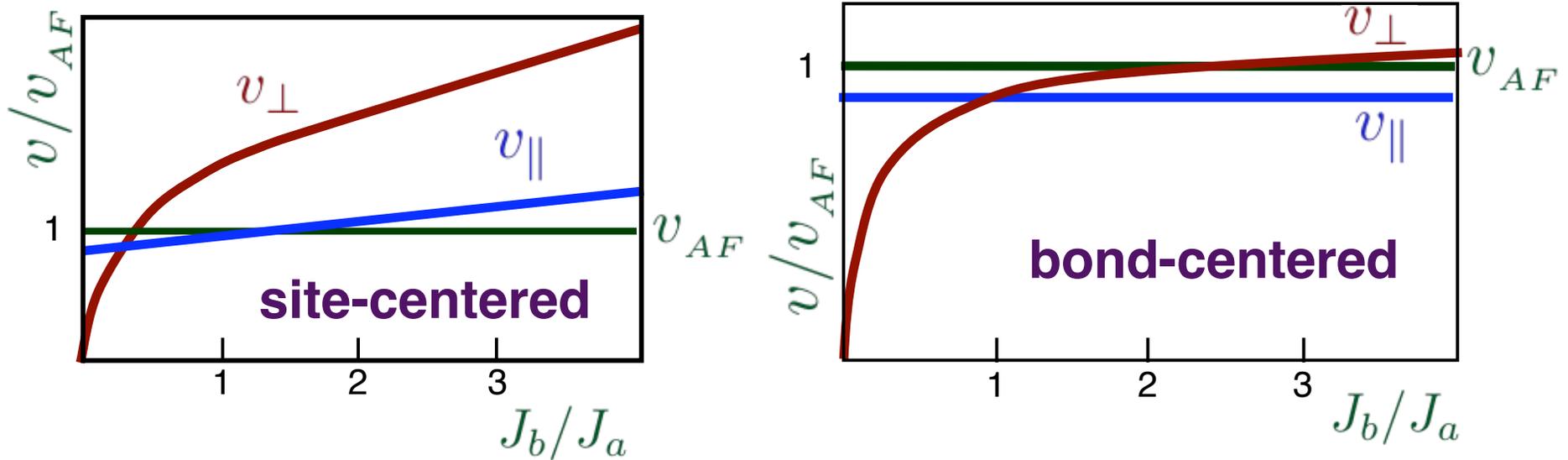


$$H = \frac{1}{2} \sum_{\langle ij \rangle} J_{ij} \vec{S}_i \cdot \vec{S}_j$$

**Semiclassical
Spin Waves**

$$S(\mathbf{k}, \omega)^{in} = \sum_f \sum_{i=x,y,z} | \langle f | S^i(\mathbf{k}) | 0 \rangle |^2 \delta(\omega - \omega_f)$$

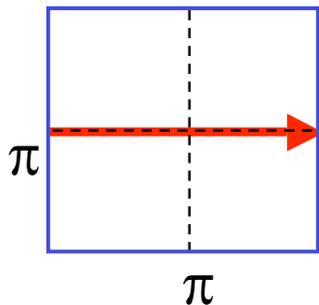
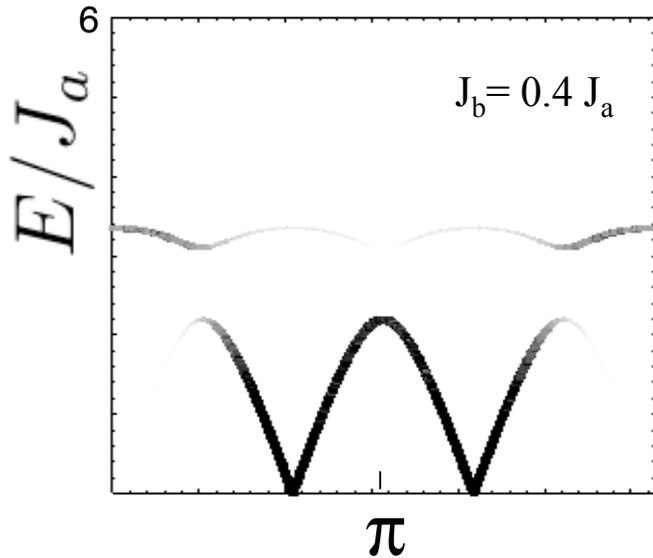
Low Energy Velocities



Spin wave cones may remain rather *isotropic* for bond-centered stripes, despite microscopic anisotropy.

Spin Wave Dispersions

Site-centered, $p=3$

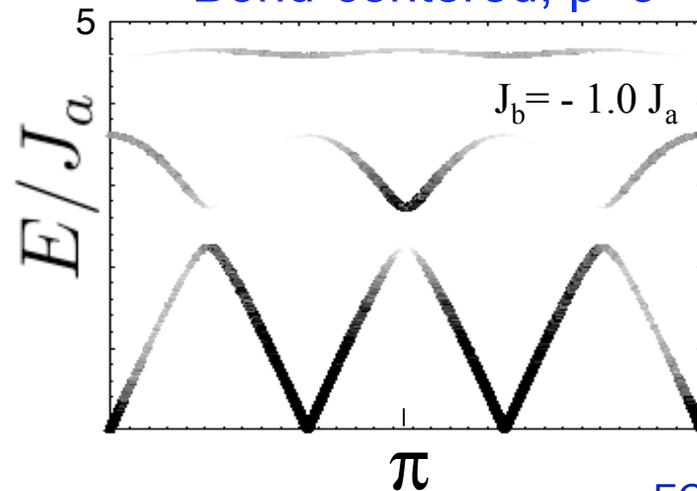


- Bond-centered has one more band
- Bond-centered has weight at $(0, \pi)$
- Bands repel, do not cross

Resonance unlikely from crossings

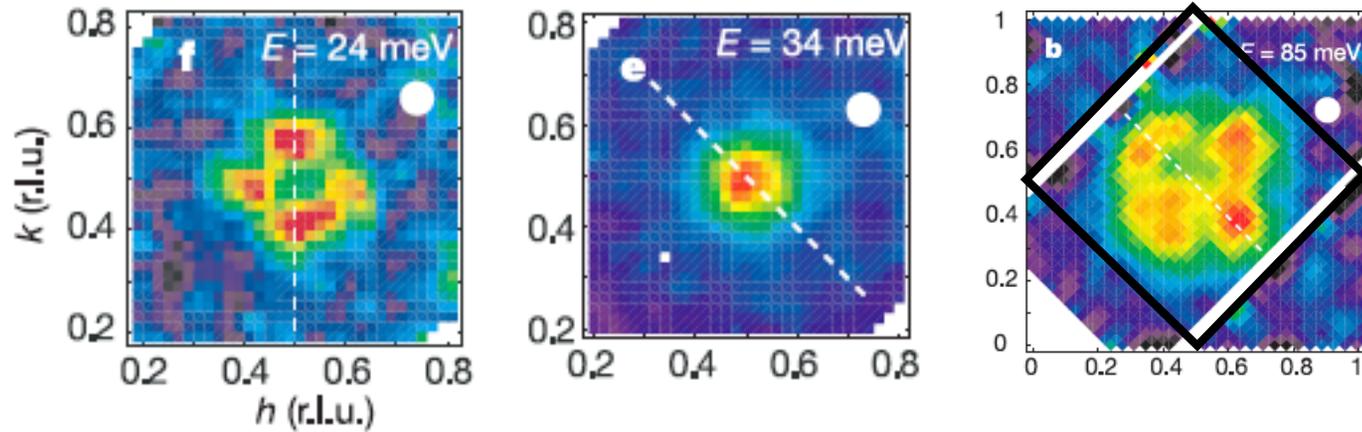
Batista *et al.*, PRB (2001)

Bond-centered, $p=3$

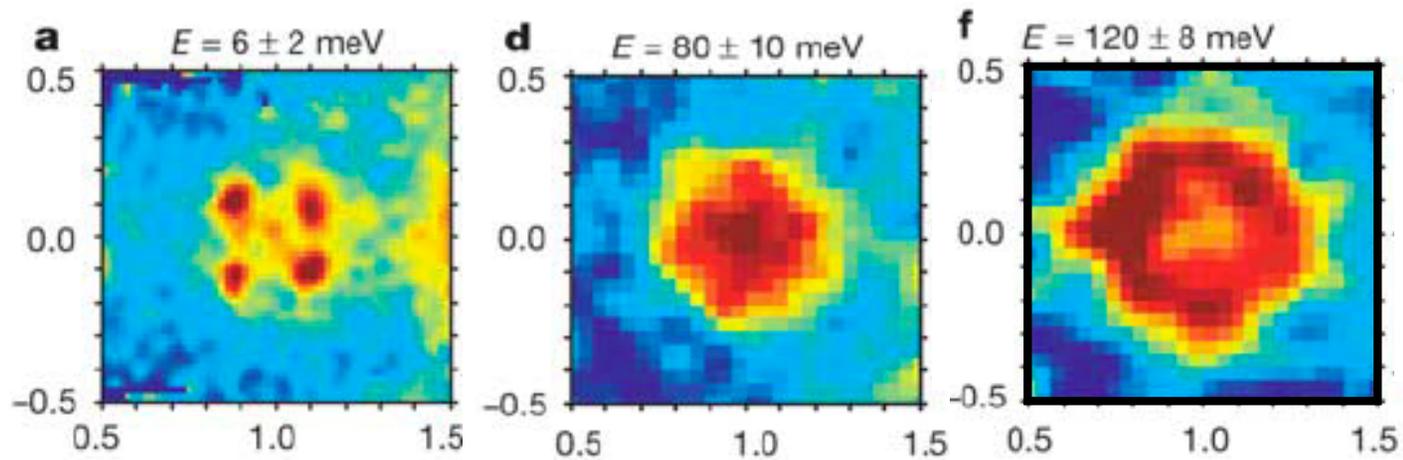


EC, Yao, *et al.*, PRB (2004)

Data

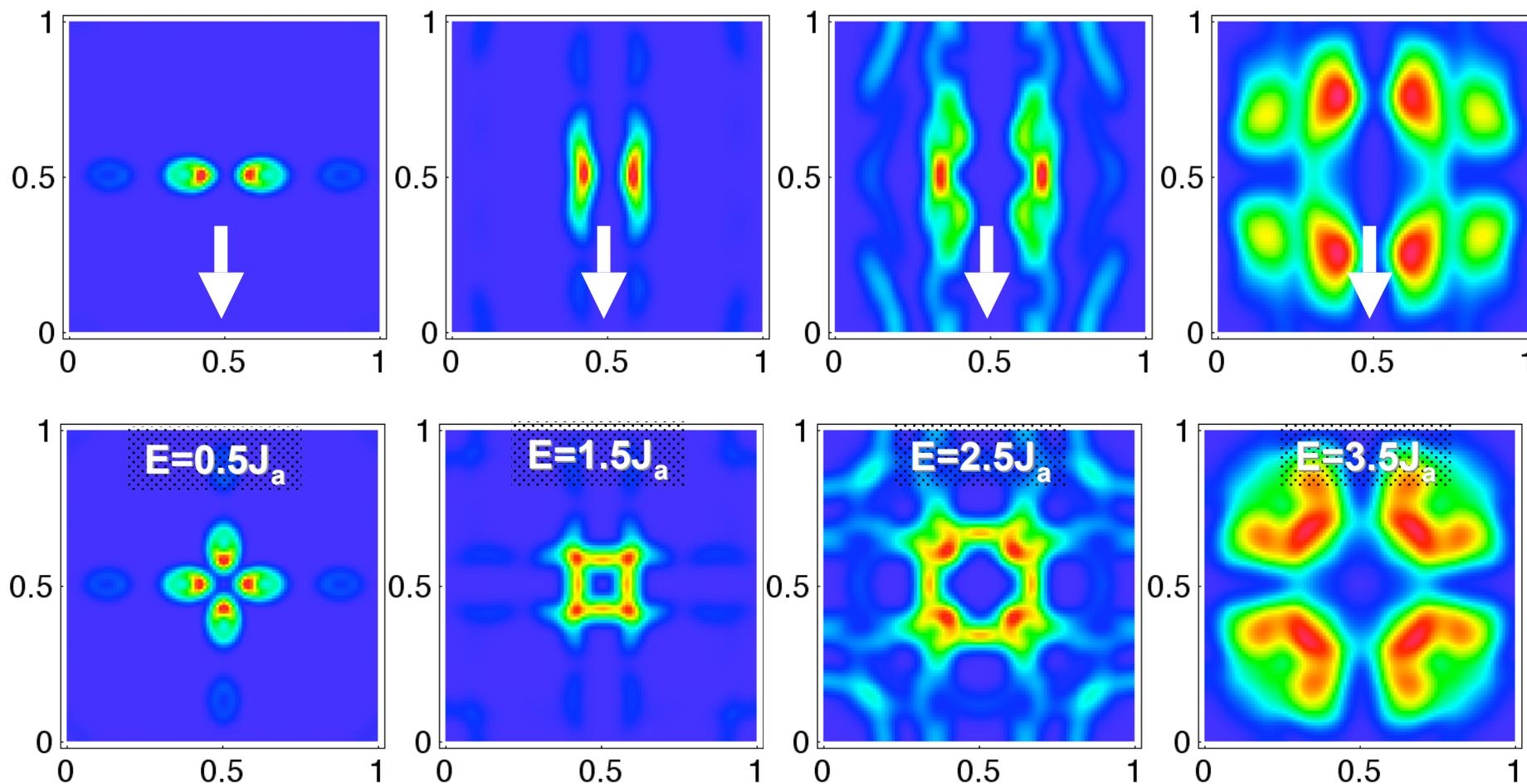
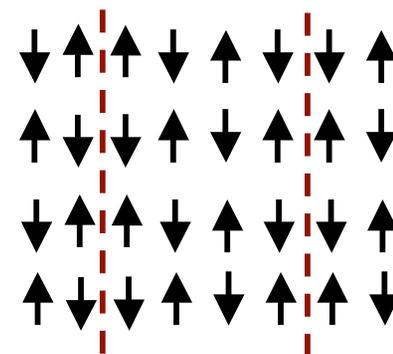


YBCO6.6, S. Hayden *et al.*, Nature 429, 531 (2004)



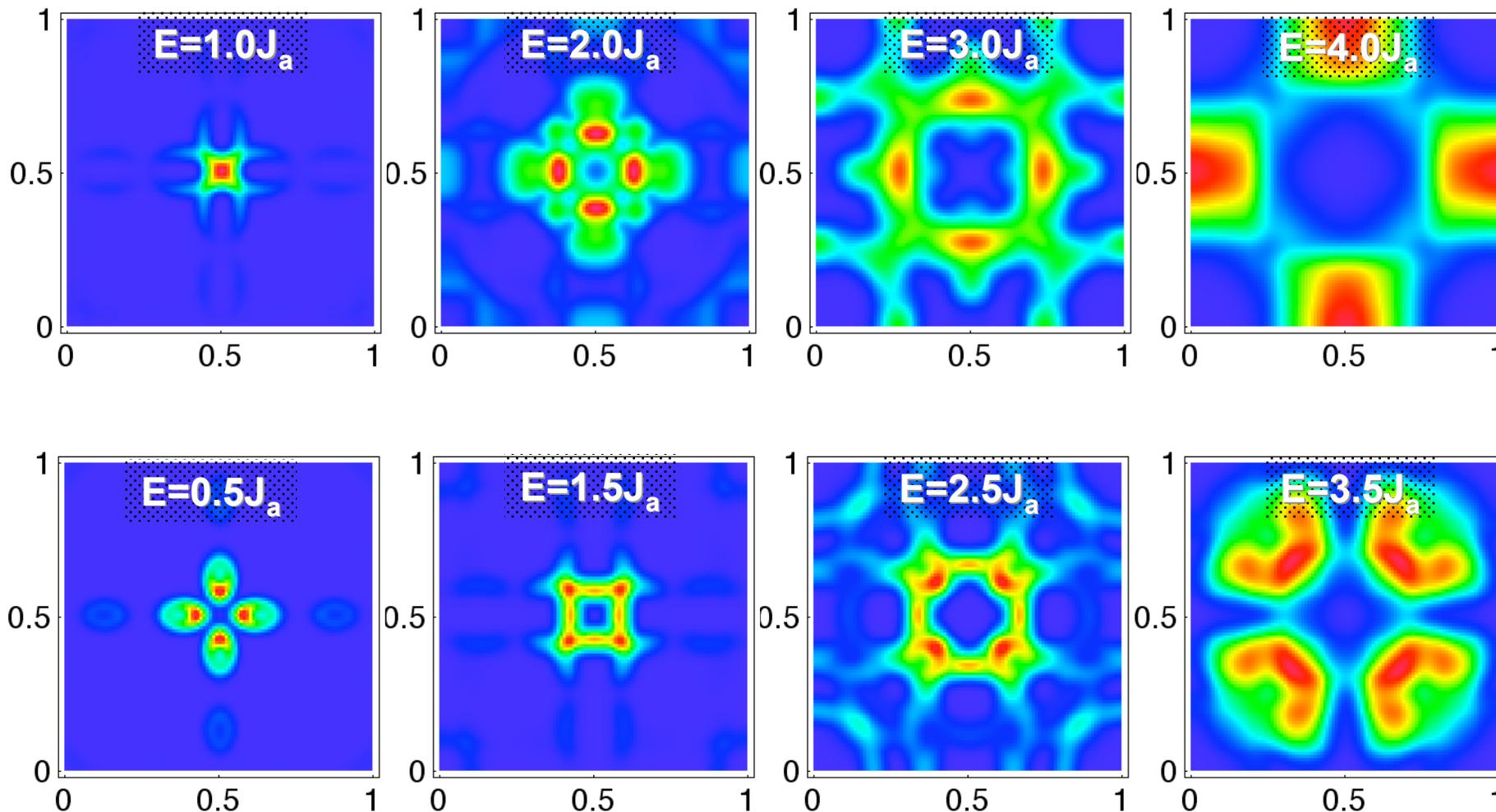
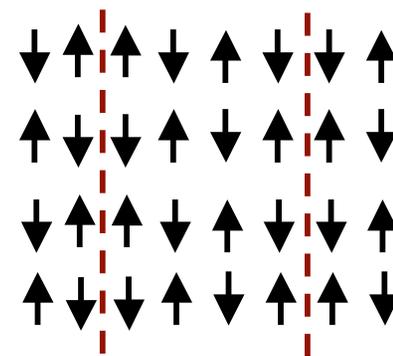
Stripe-ordered LBCO, S. Hayden *et al.*, Nature 429, 534 (2004)

Symmetrize



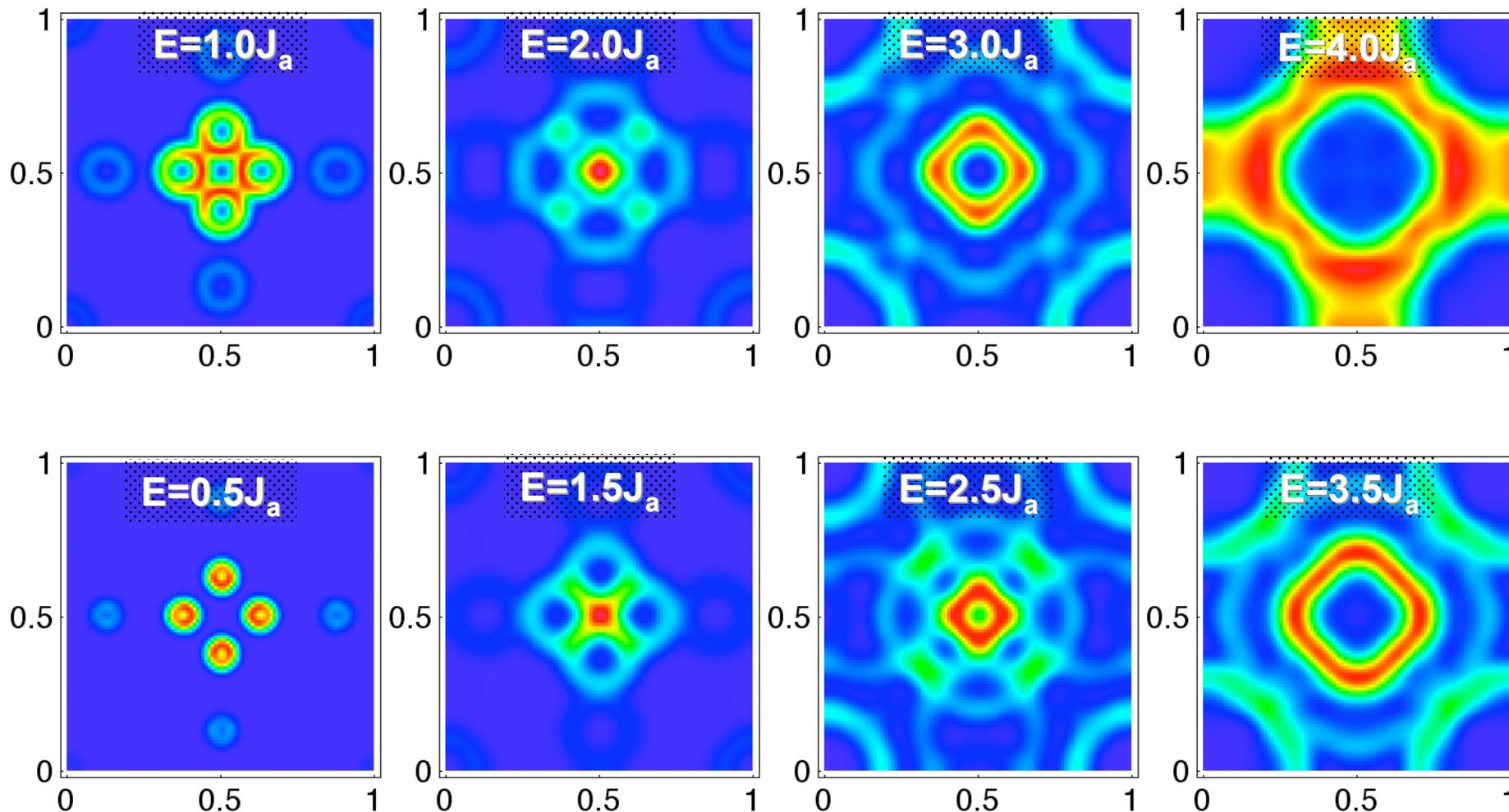
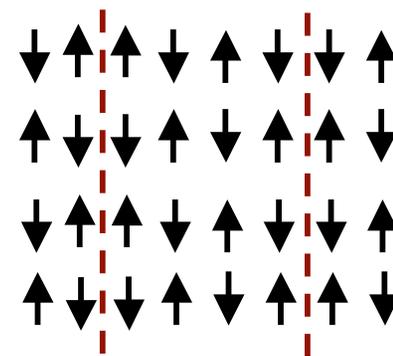
VB4 $J_b = -.1 J_a$

Vertical, Bond-centered, Spacing = 4



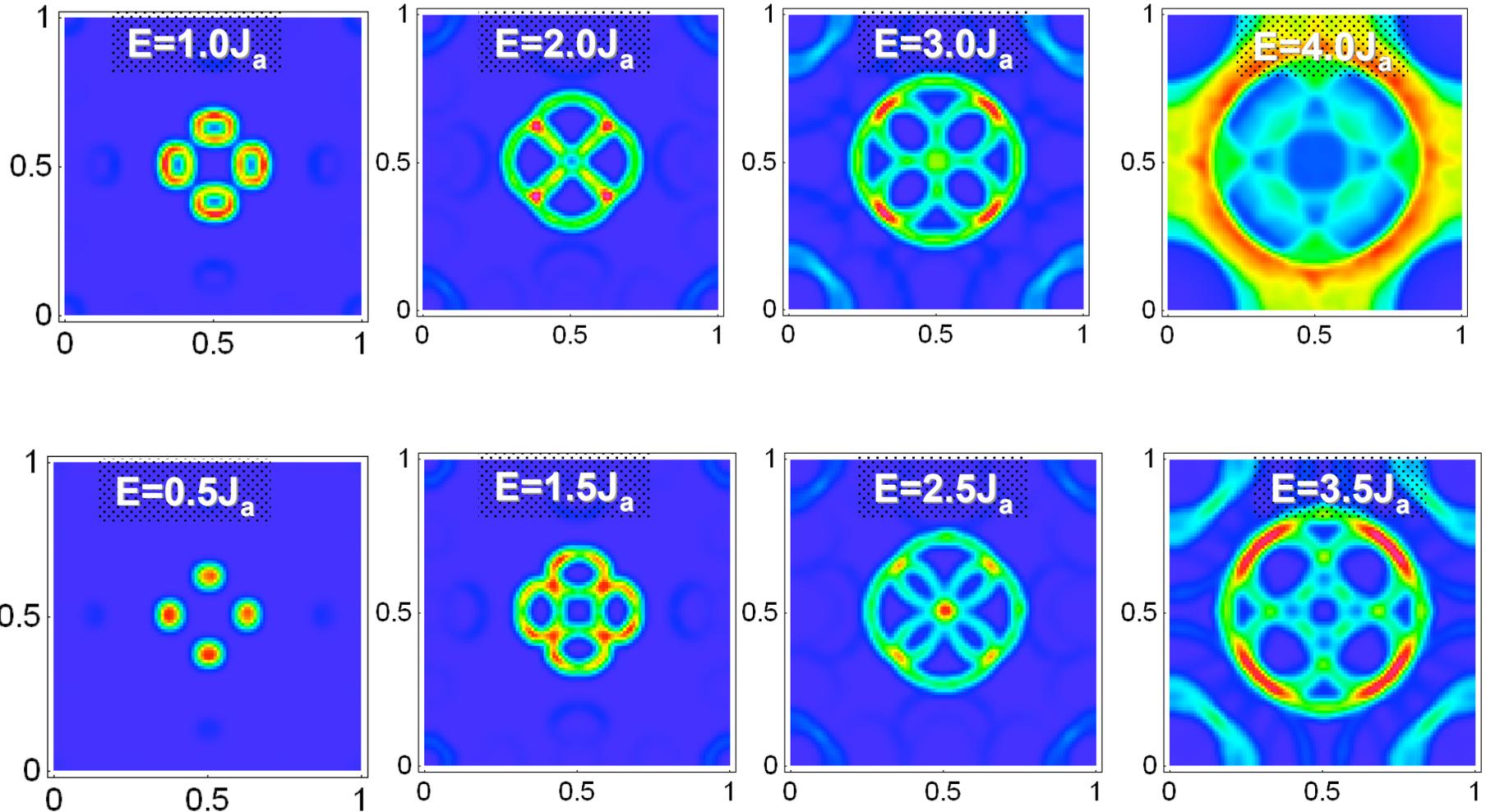
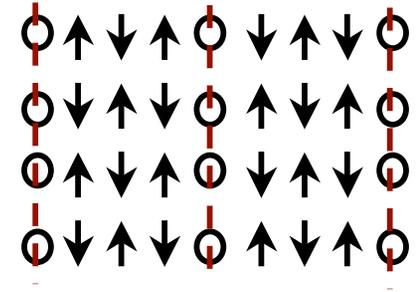
VB4 $J_b = -.56 J_a$

Vertical, Bond-centered, Spacing = 4



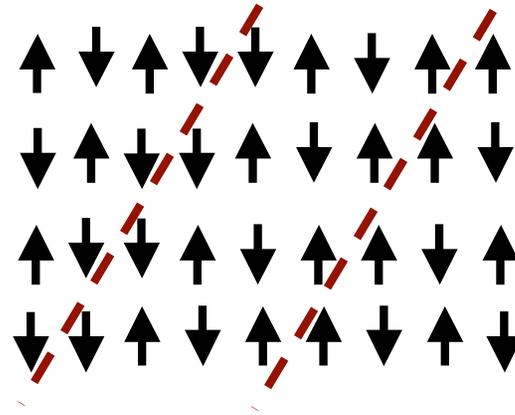
VS4 $J_b = J_a$

Vertical, Site-centered, Spacing = 4



Other Stripe Patterns

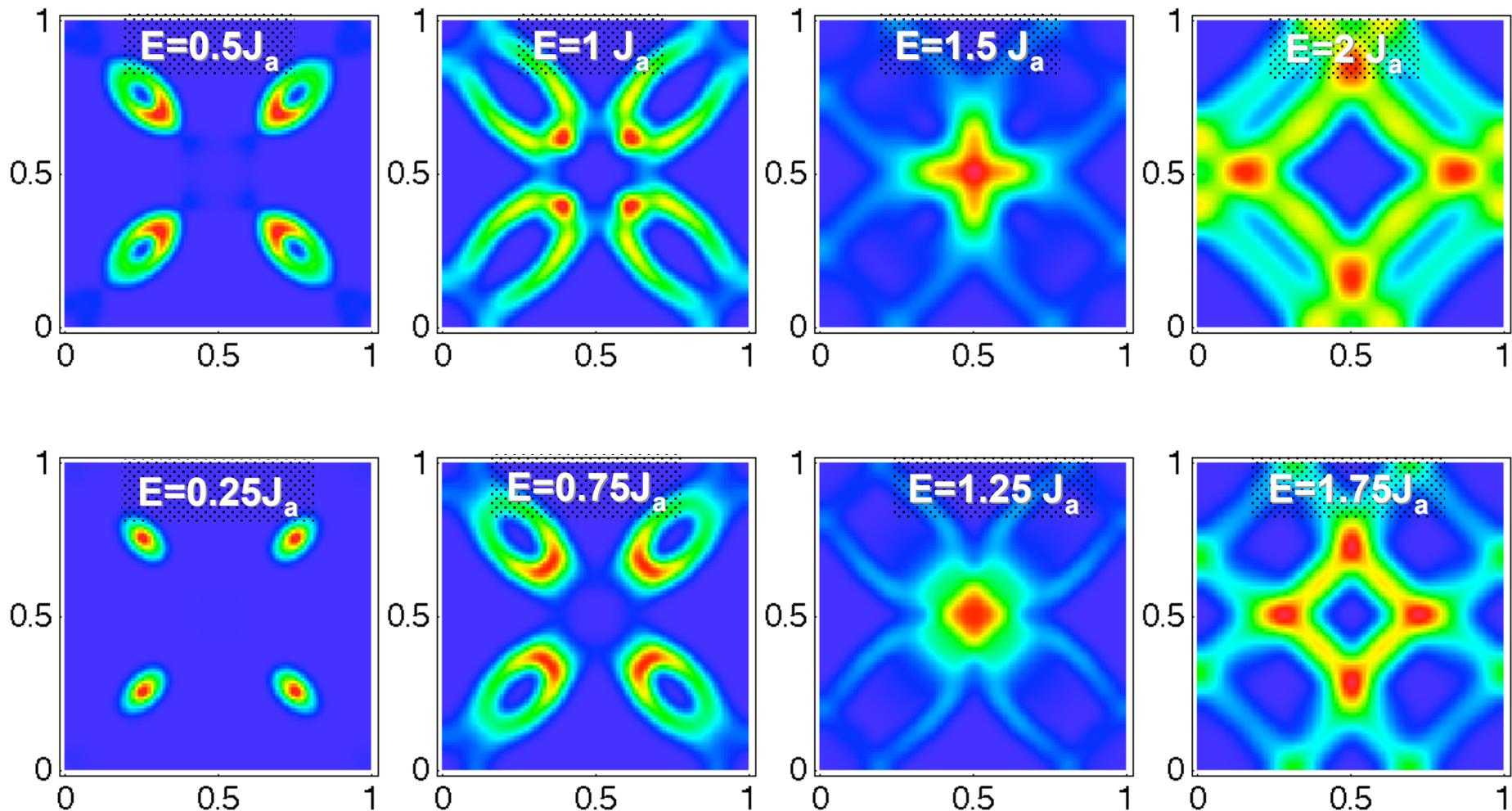
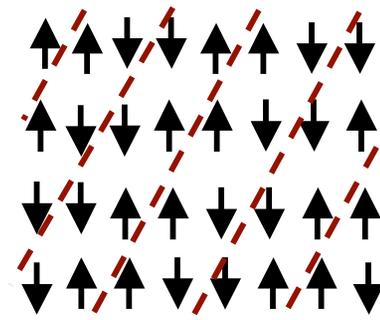
Diagonal



“DB4”

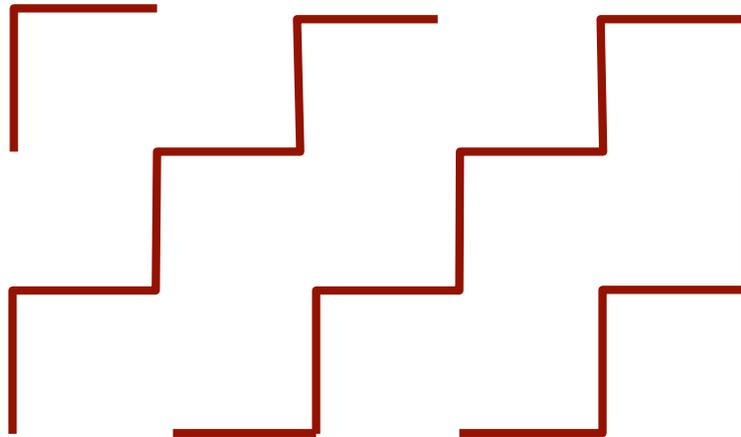
DB2 $J_b = -.1 J_a$

Diagonal, Bond-centered, Spacing = 2



Other Stripe Patterns

Staircase

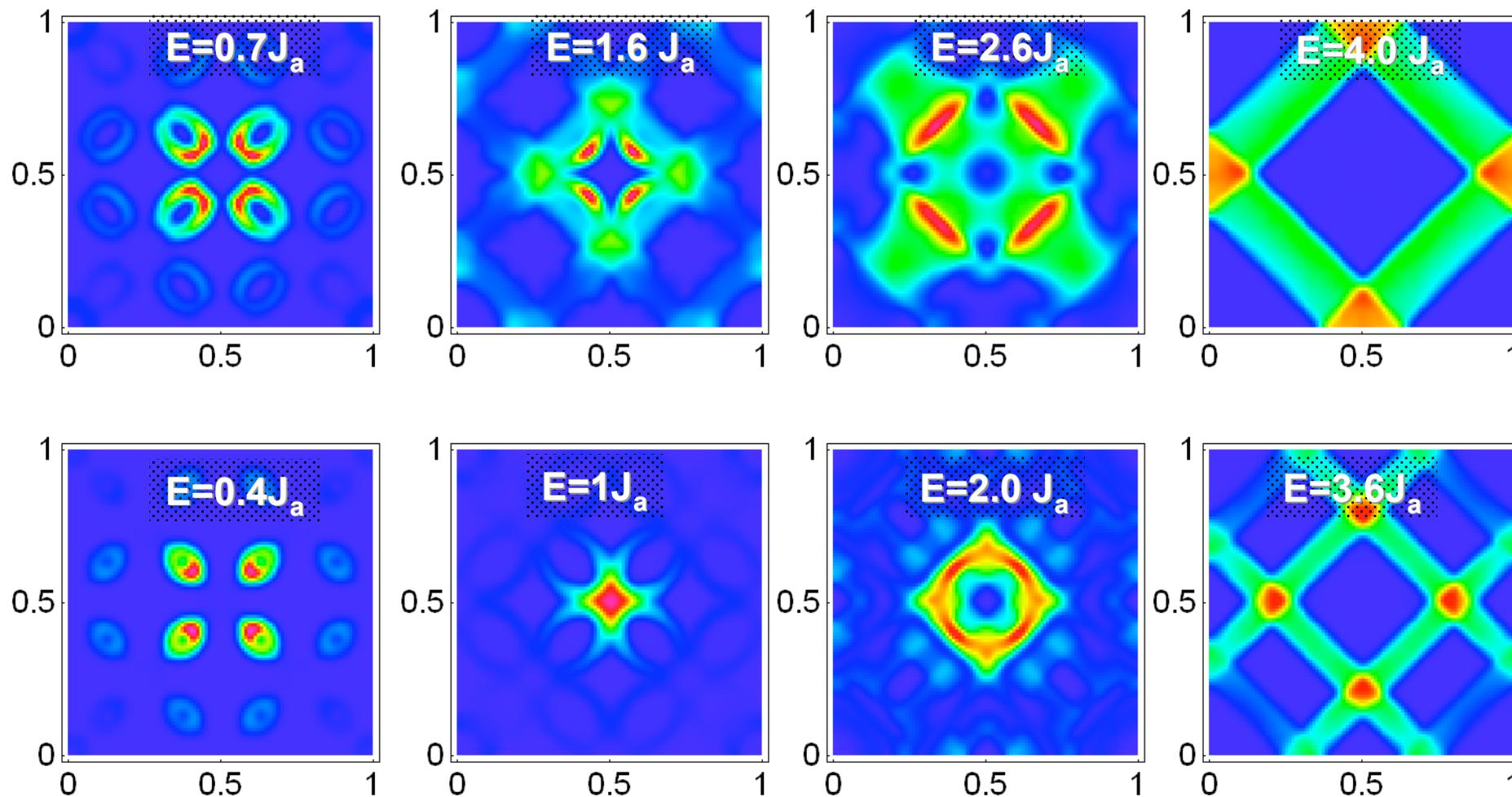
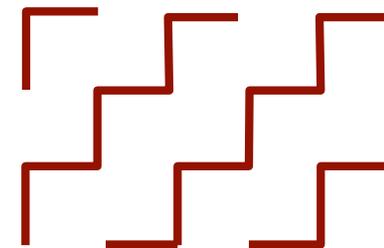


Globally diagonal
Locally vertical
Antiphase domain walls

M. Granath, PRB (2004)
Smooth transition from diagonal to vertical peaks
Fermi Surface Arcs

SB2 $J_b = -.1 J_a$

Staircase, Bond-centered, Spacing = 2



Conclusions

2D magnetic texture

- Stripes produce 2D spin waves.
- Finite energy weight at (π, π) is natural from stripes, but not from a pure antiferromagnet.

Resonance peak

- Unlikely from crossing (**bands repel**)

Bond-centered stripes:

- Ferromagnetic coupling across domain wall
- One more band than site-centered
- Odd spacing has *new elastic peaks*, forbidden for site-centered stripes
- Isotropic spin wave cones
- “**Legs**” of scattering

Comparison to Recent Cuprate Data

- Low energy could be semiclassical spin waves
- High energy is not

