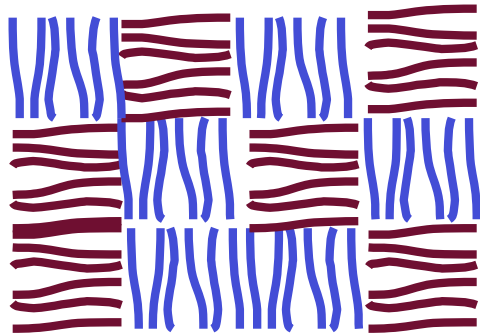


# Electronic Noise Due to Thermal Stripe Switching

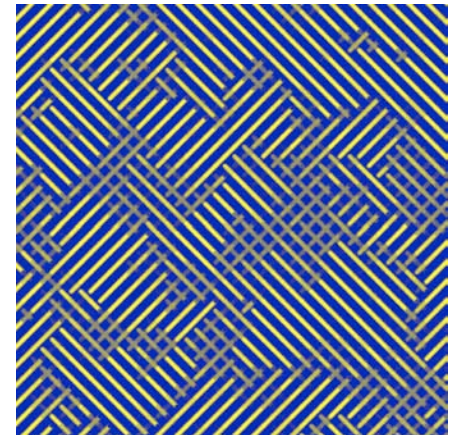


**E. W. Carlson**

B. Phillabaum

Y. L. Loh

D. X. Yao



**Research  
Corporation**

***Solid***

***Liquid***

***Gas***



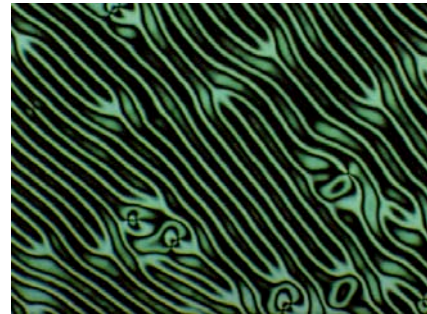
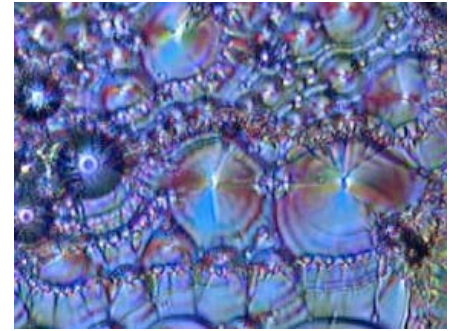


## Crystals Fluids



Crystals  
Fluids

Liquid Crystals

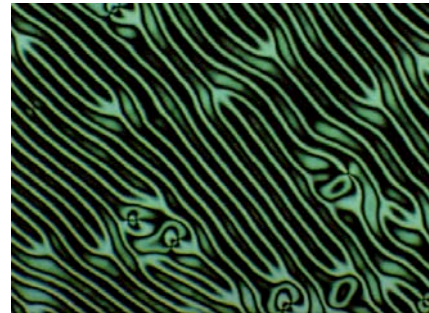
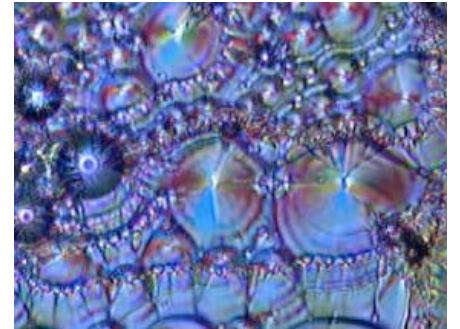


*Smectic*  
*Nematic*  
*Hexatic*  
*Cholesteric...*



Crystals  
Fluids

Liquid Crystals



*Smectic*  
*Nematic*  
*Hexatic*  
*Cholesteric...*



Glass and  
Amorphous solids

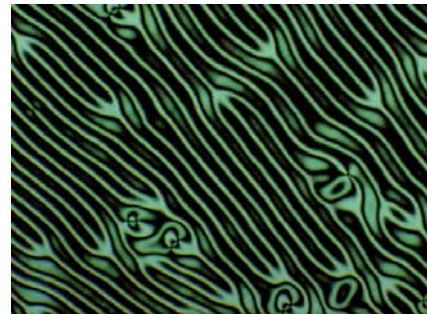
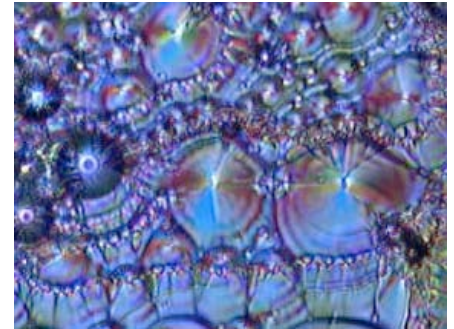
[www.dalechihuly.com](http://www.dalechihuly.com)





## Crystals Fluids

## Liquid Crystals

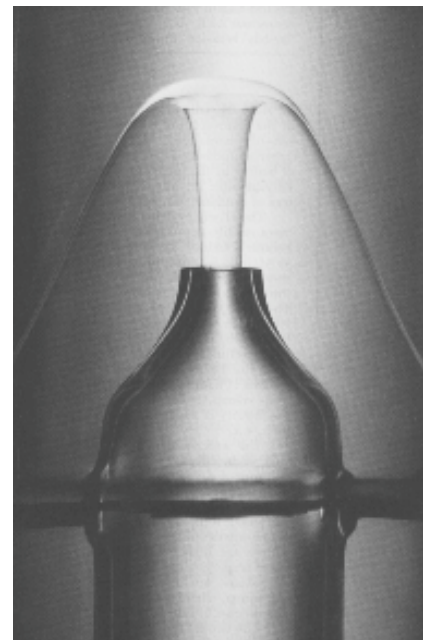


*Smectic*  
*Nematic*  
*Hexatic*  
*Cholesteric...*

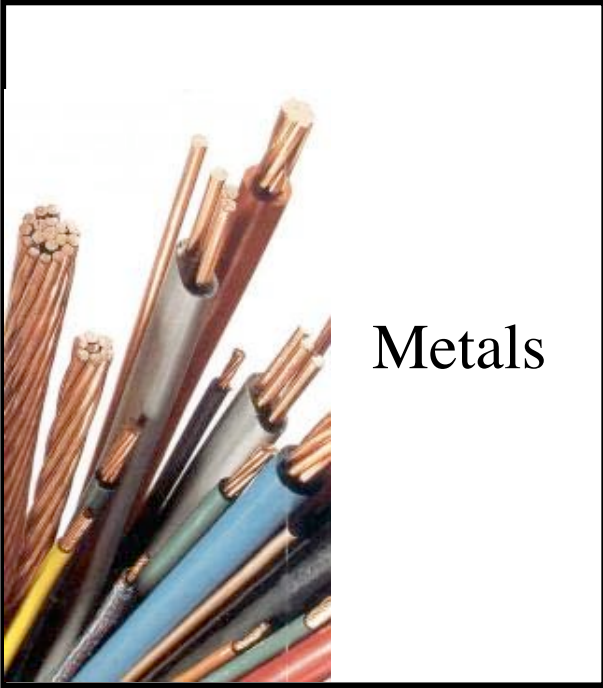


## Glass and Amorphous solids

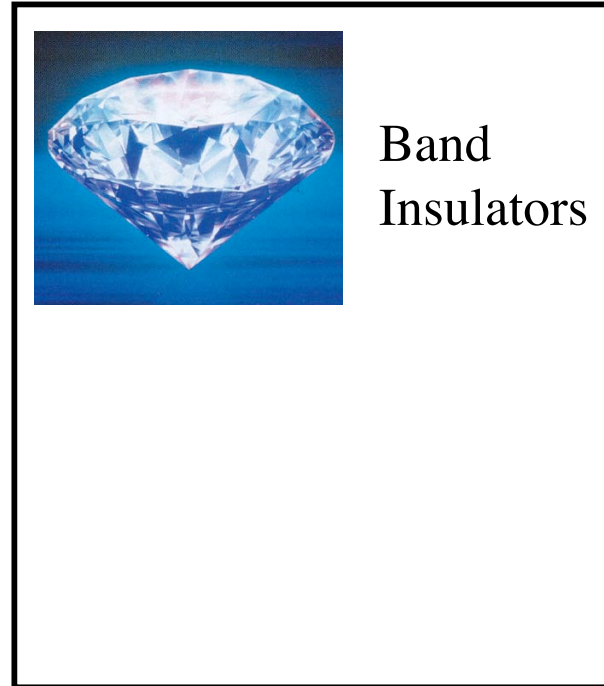
[www.dalechihuly.com](http://www.dalechihuly.com)



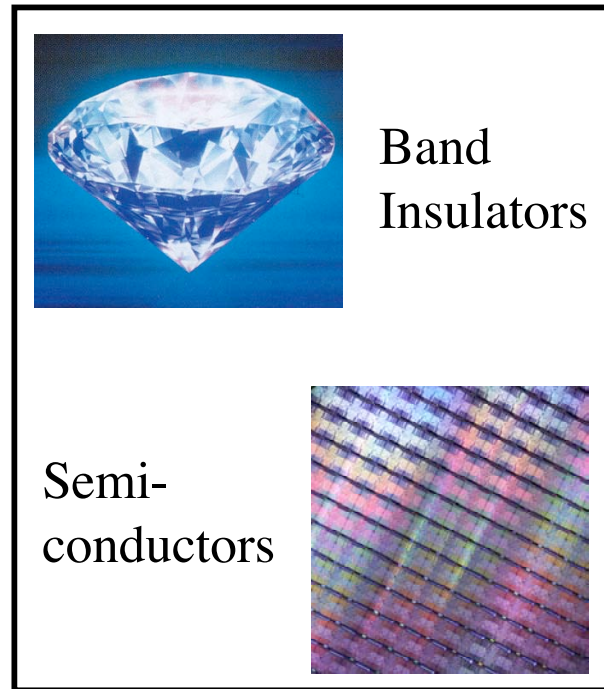
## Superfluid

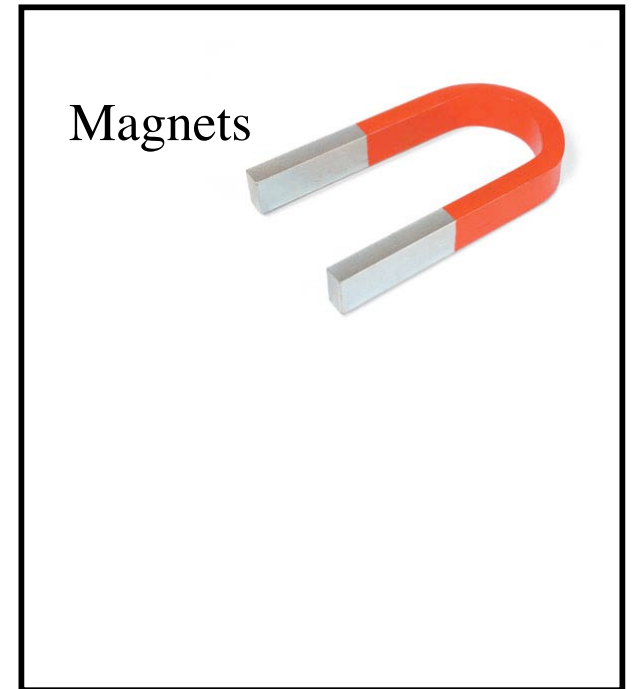
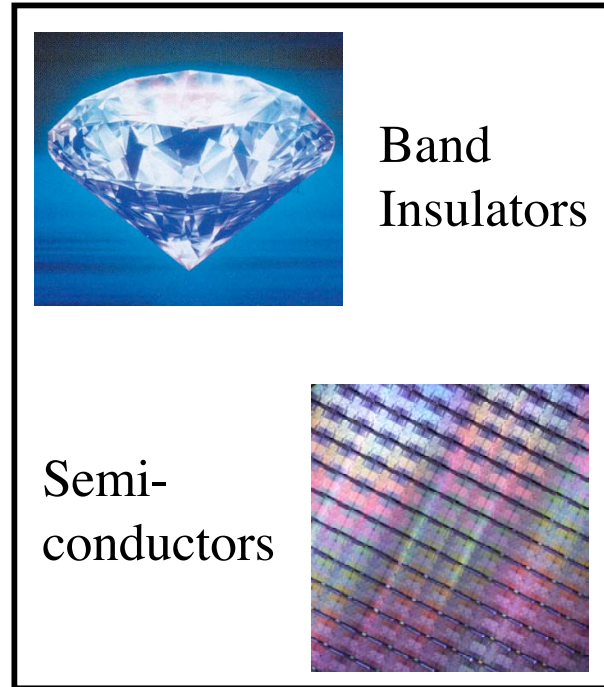


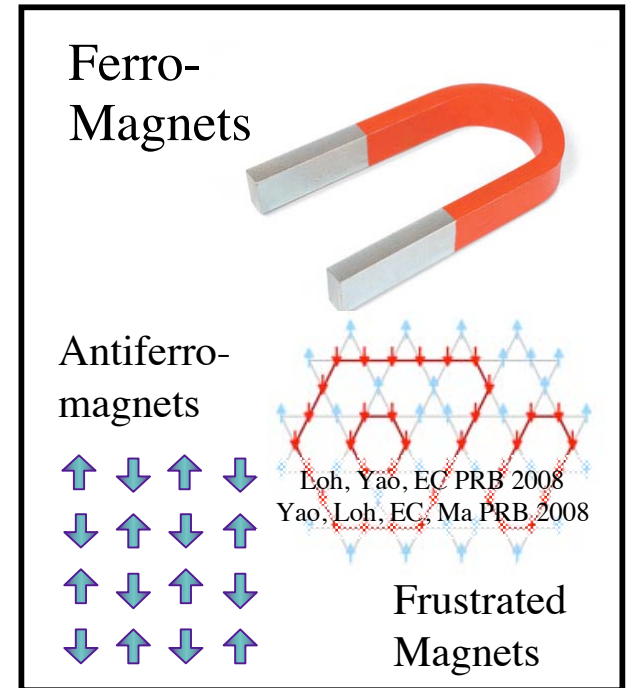
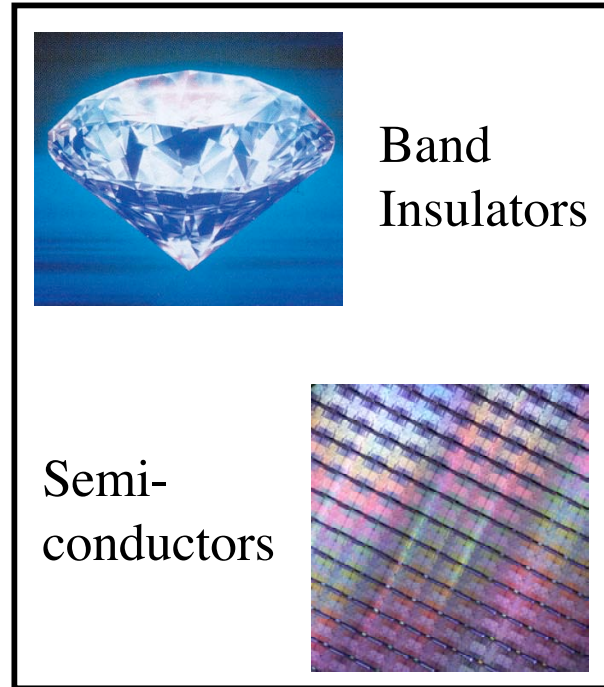
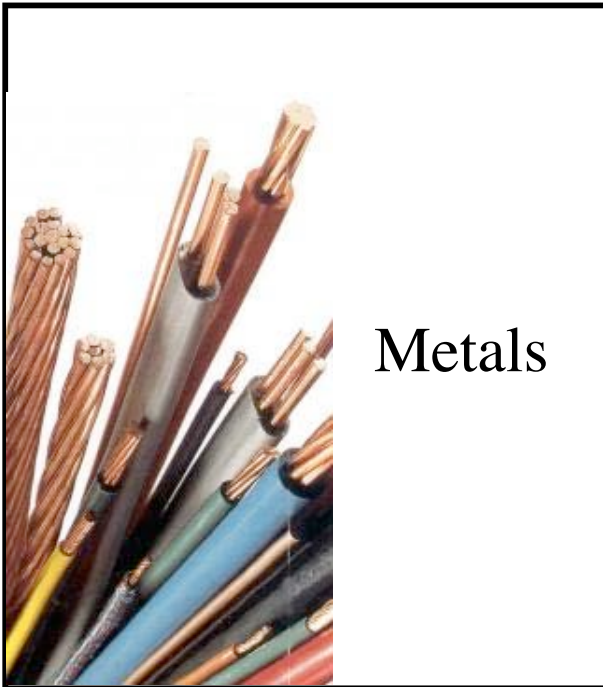
Metals

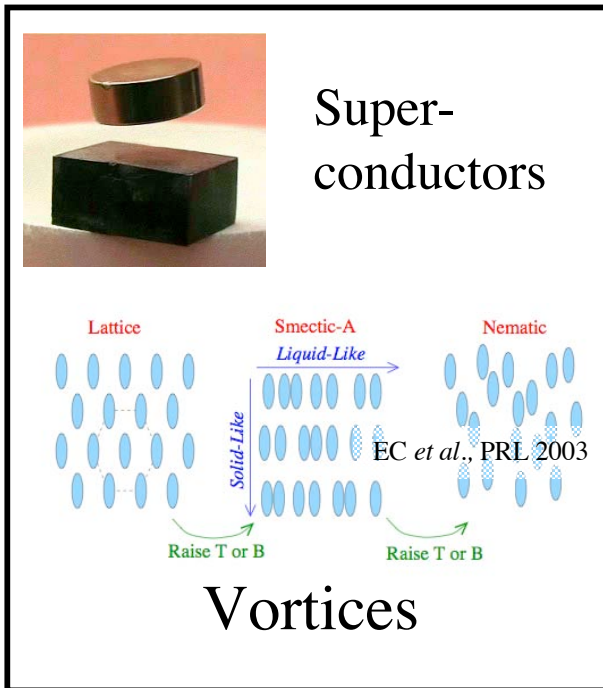
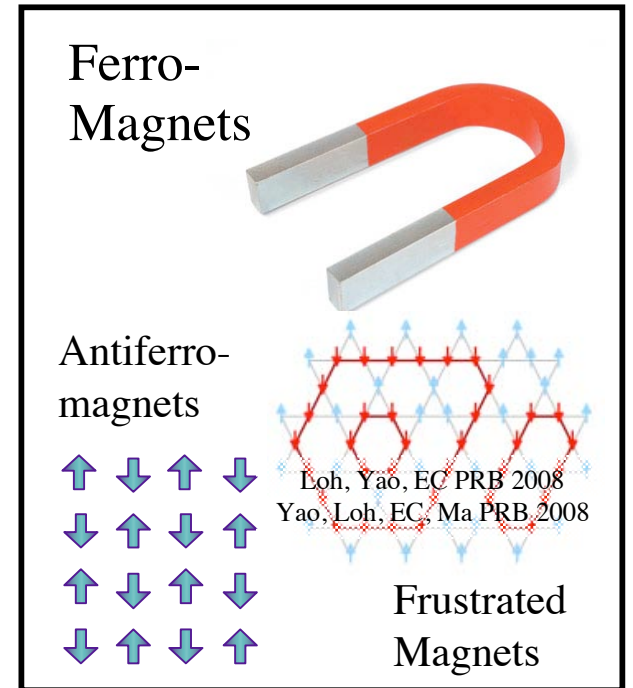
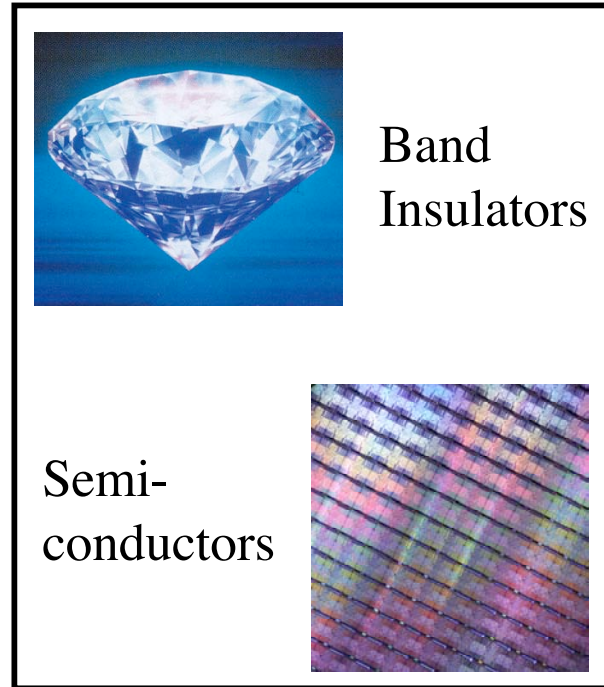
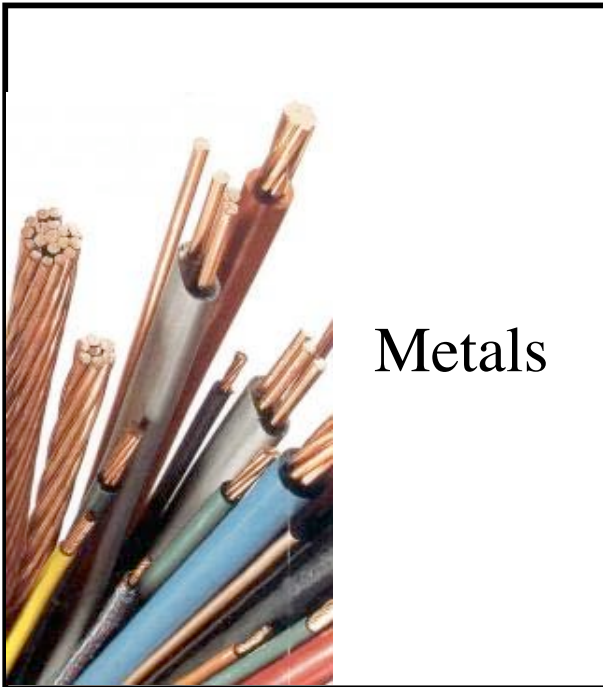




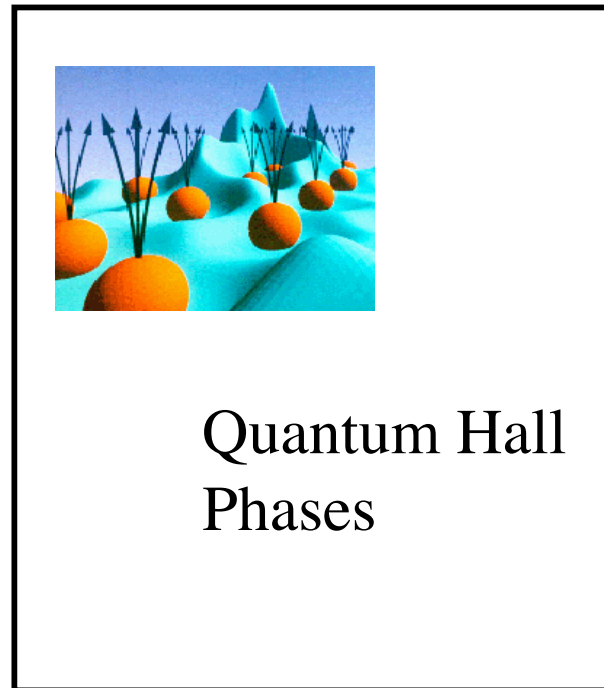
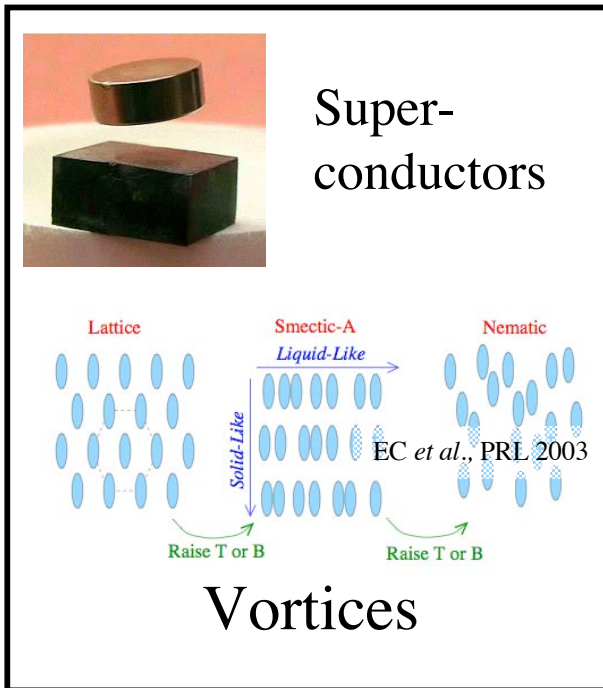
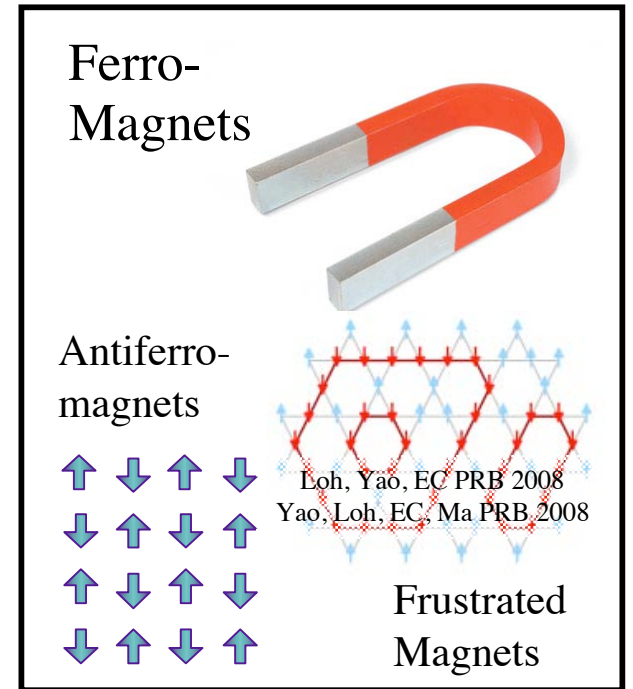
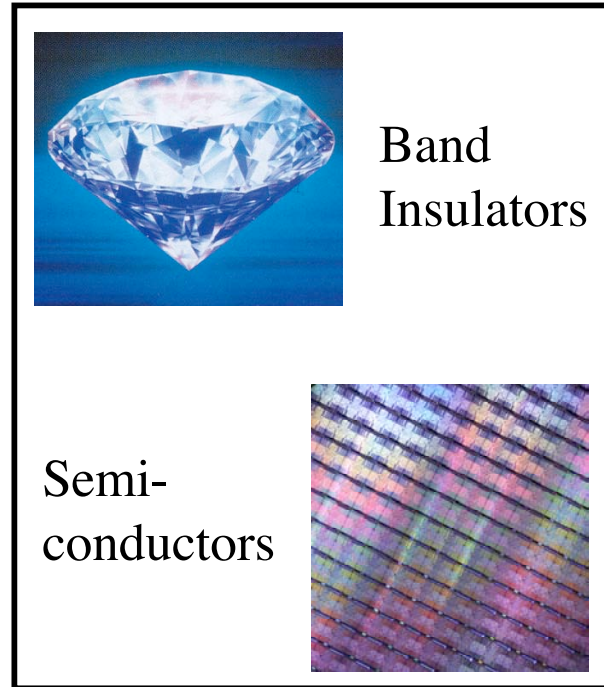
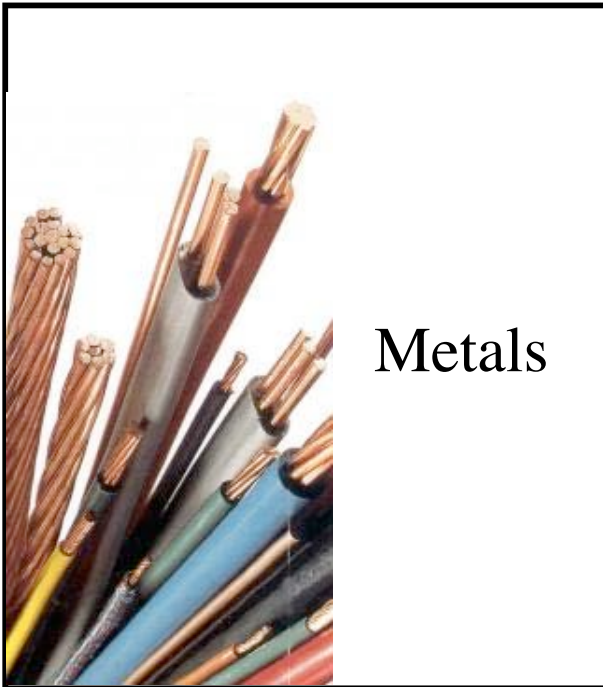


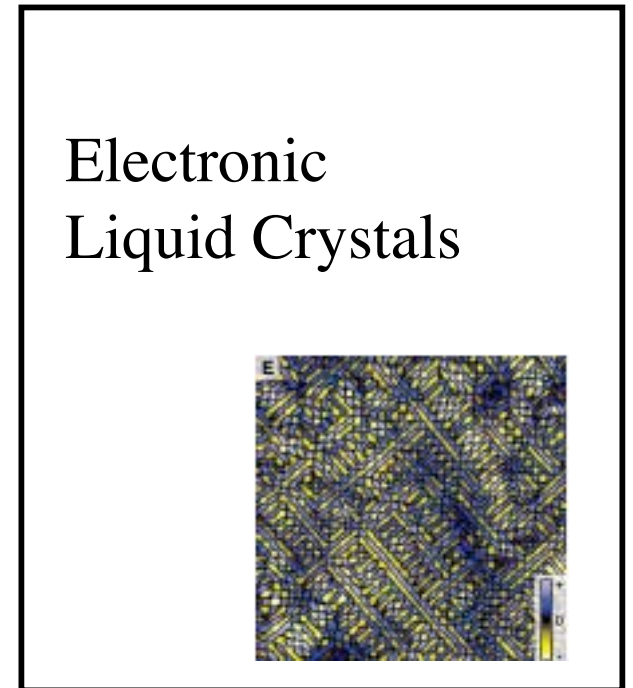
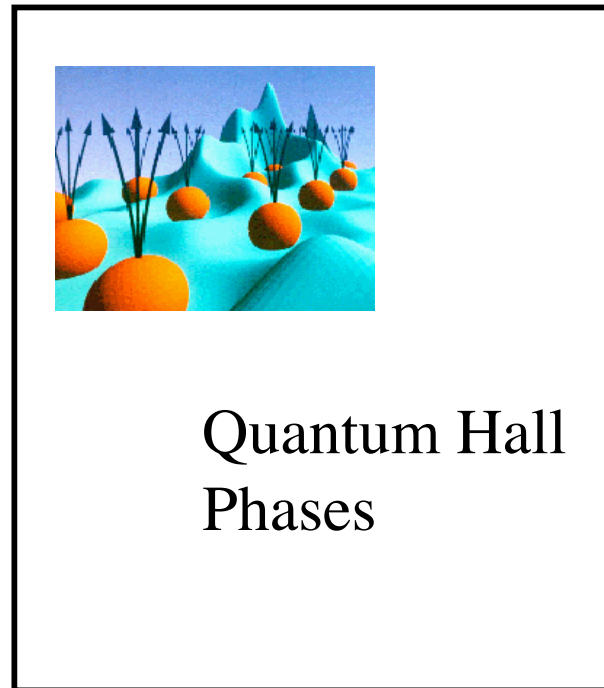
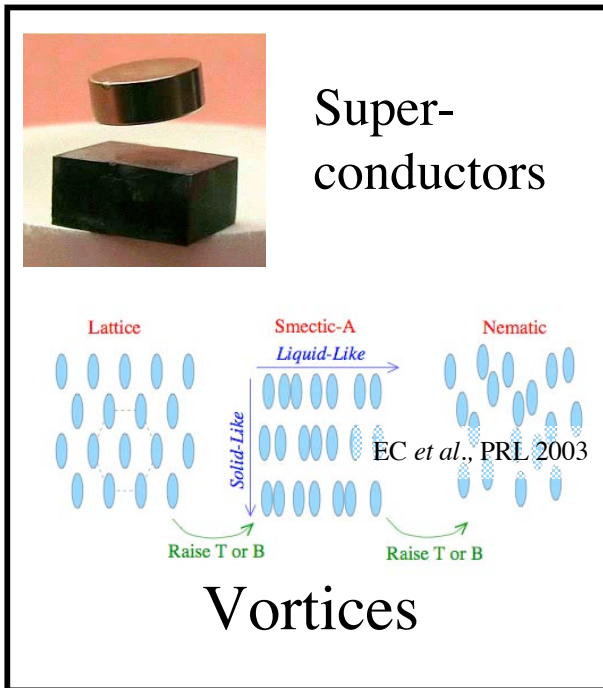
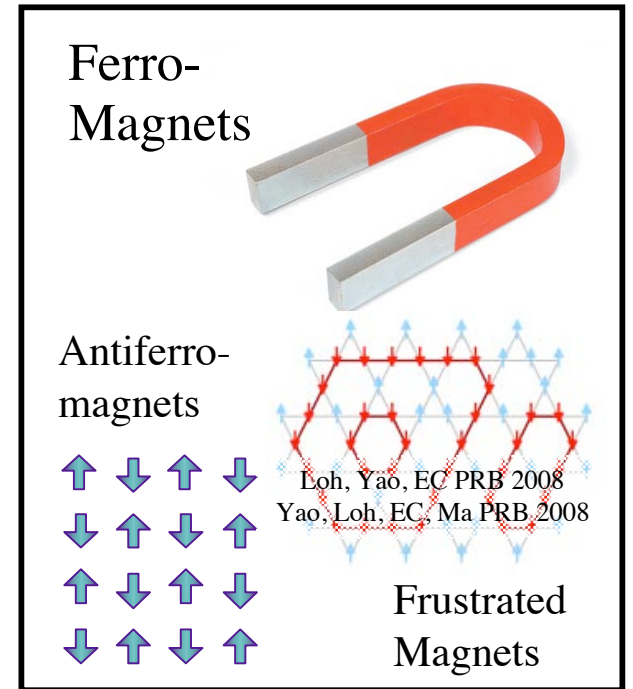
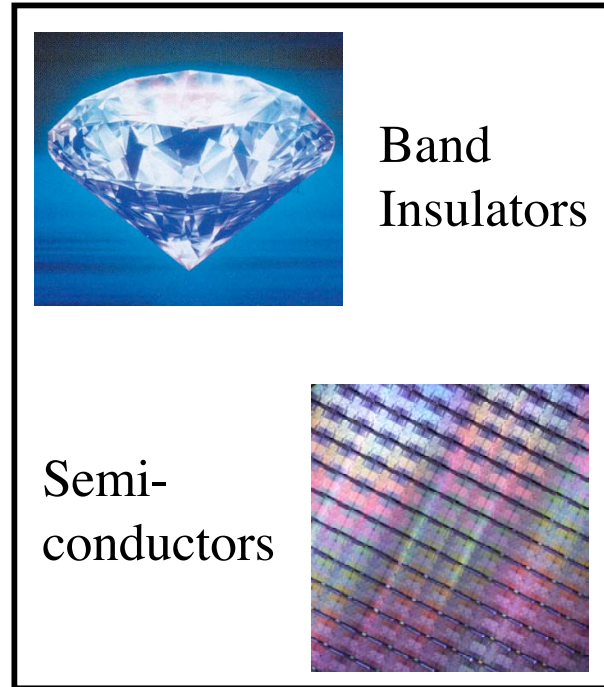
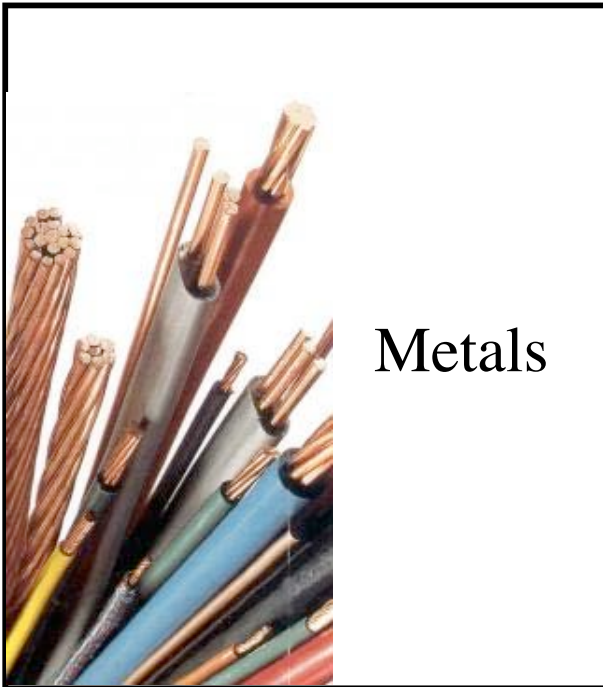










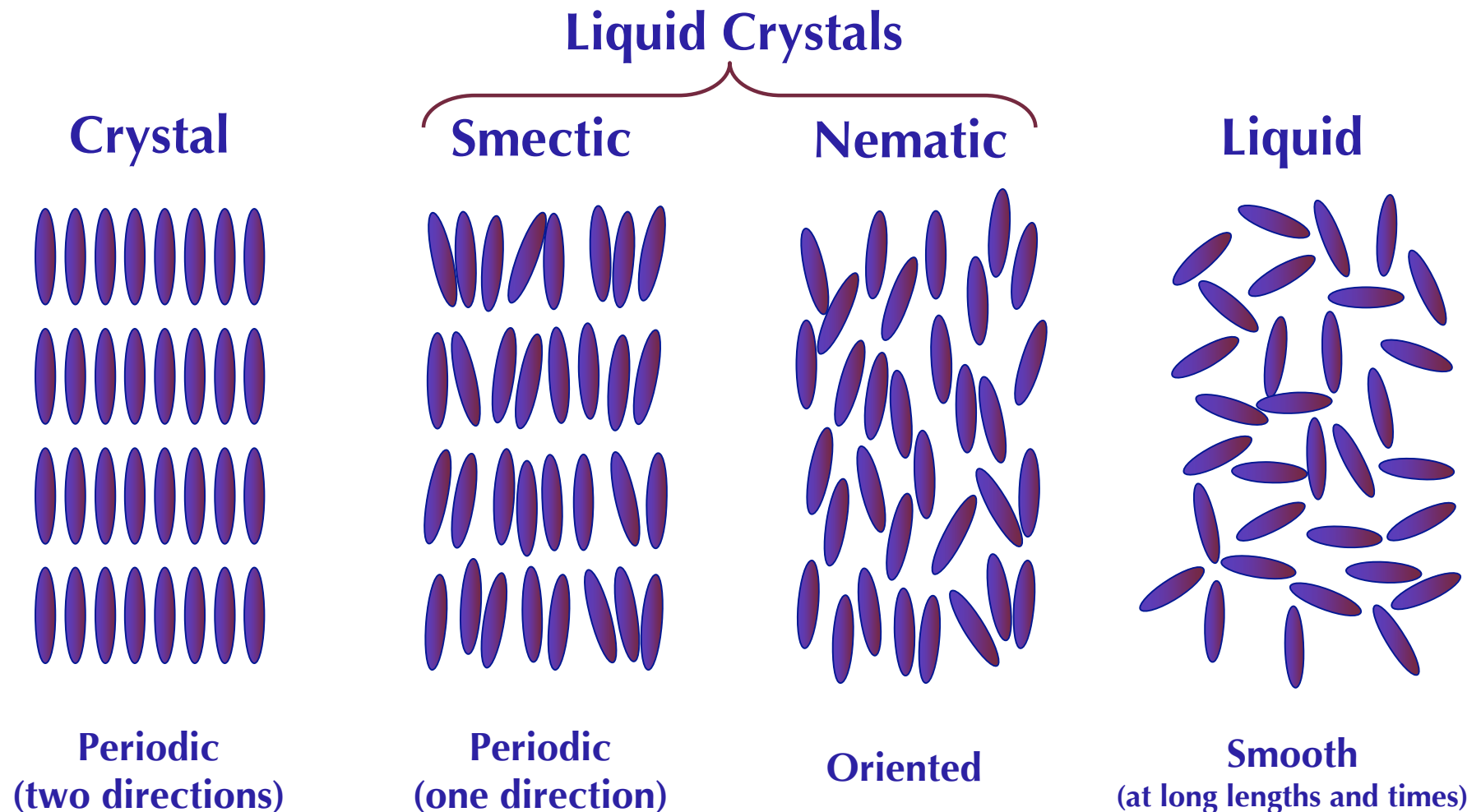




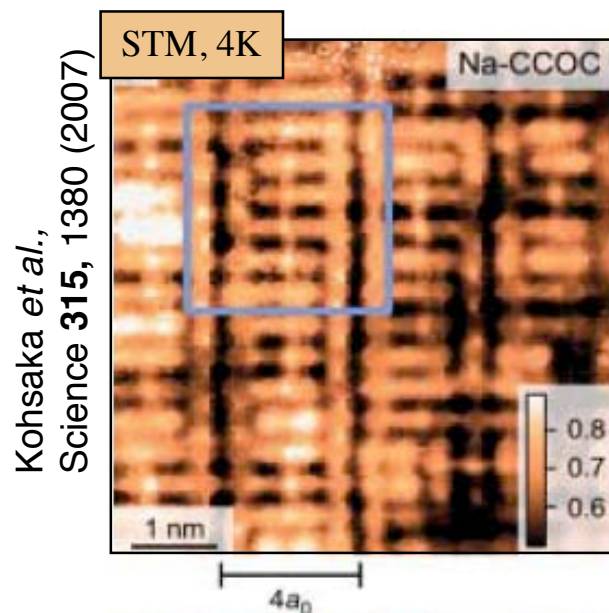
# How we classify phases

---

By the symmetry of long distance and long time properties



# Strong Correlations and Disorder

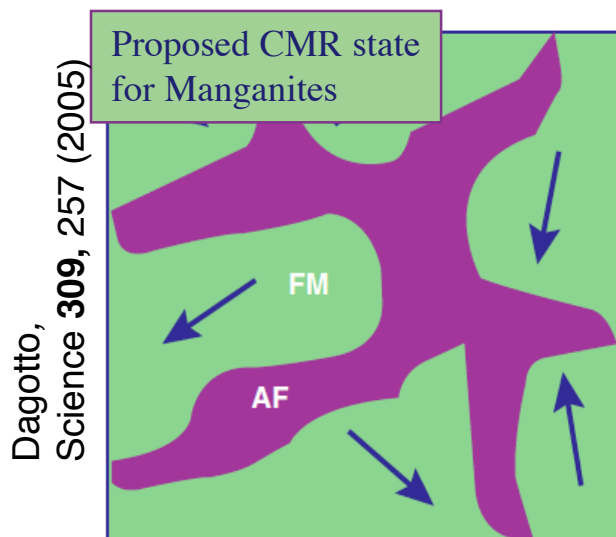


## Many degrees of freedom

Spin  
Charge  
Orbital  
Lattice

## Strong Correlation + Many DOF

Many Phases Possible  
Different Phases Compete



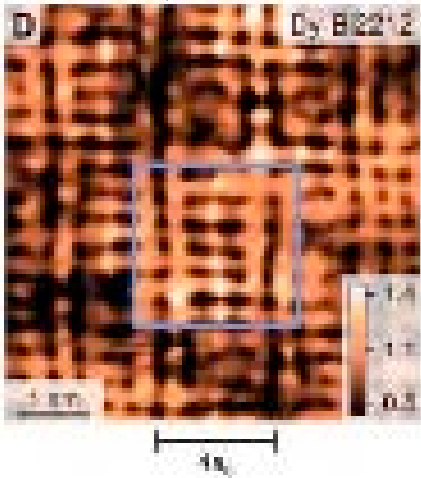
## Competing Phases + Disorder

Nanoscale pattern formation  
Complexity

# A Way Forward

---

Important nanoscale structure missed by the definition of a phase!



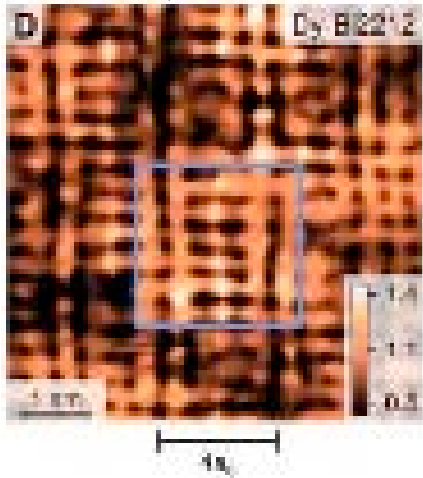
Kohsaka *et al.*,  
Science **315**, 1380 (2007)

## PROBLEM:

Most theoretical and experimental tools  
are designed to characterize and detect  
long distance behavior

# A Way Forward

Important nanoscale structure missed by the definition of a phase!



Kohsaka *et al.*,  
Science **315**, 1380 (2007)

## PROBLEM:

Most theoretical and experimental tools are designed to characterize and detect long distance behavior

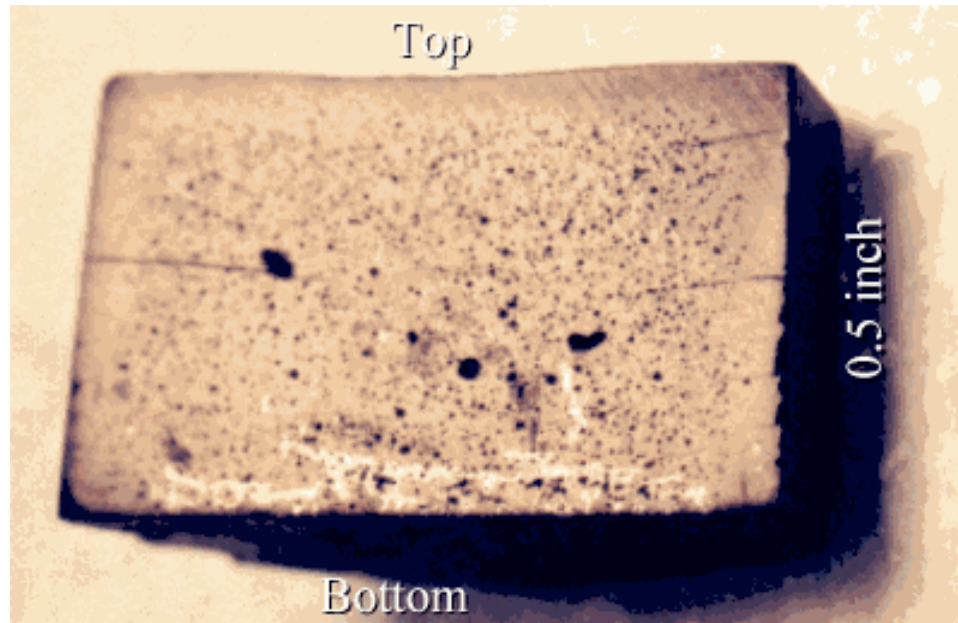
## One Solution:

Exploit Disorder, Using Noise and Nonequilibrium Effects to Characterize and Detect Nanoscale Pattern Formation

# Cuprate Superconductors

---

Brittle  
Ceramic  
Not Shiny  
Not Metallic

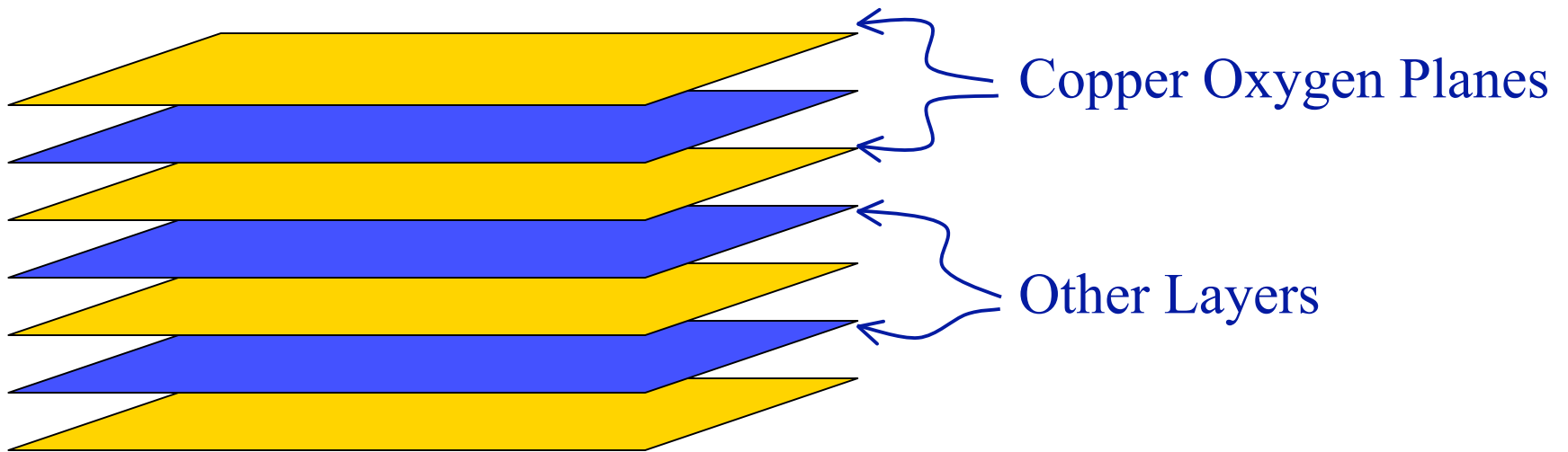


Discovered in 1986 and still unexplained  
There is still no consensus on the phase diagram  
Is our outdated definition of a phase hindering progress?



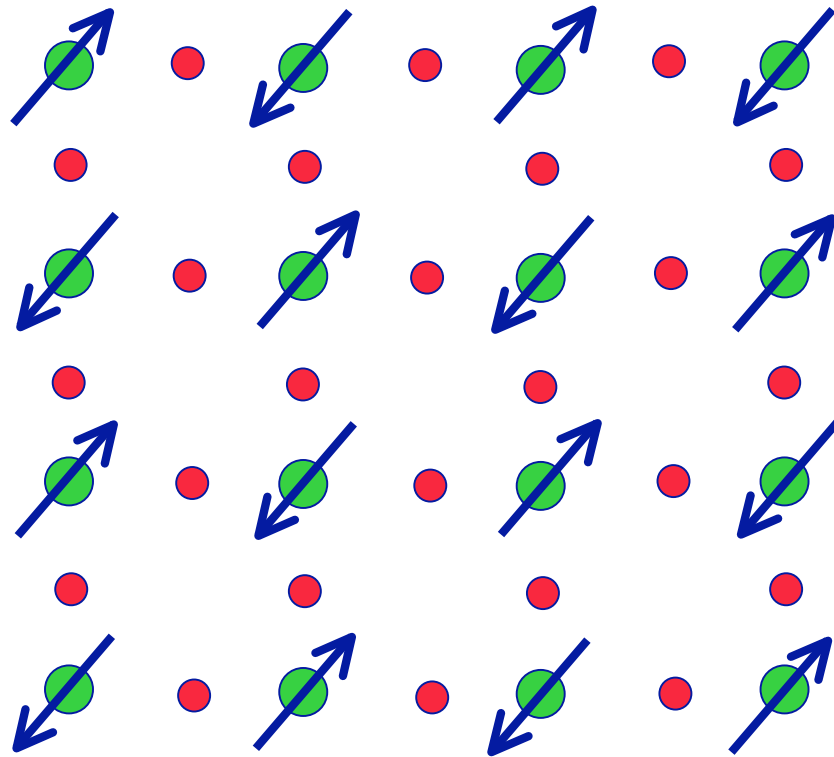
# Cuprate Superconductors

---



Layered structure  $\rightarrow$  quasi-2D system

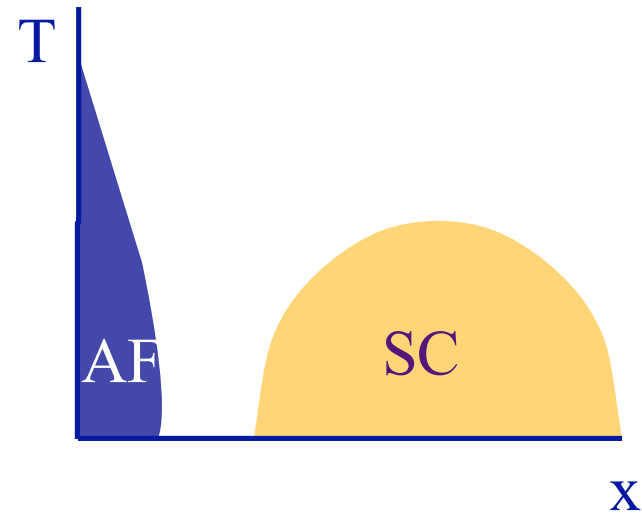
# Cuprate Superconductors



● Oxygen    ● Copper

Dope with holes

Superconducts at certain dopings



# Cuprate Superconductors

High pairing scale  $\Rightarrow$  Short range order may be key

*Pseudogap*: Many possible phases. Which one(s) is(are) happening?

*Disorder only compounds the problem!*

Stripes in cuprates?

So far, detected in only a subset of materials

Are they ubiquitous?

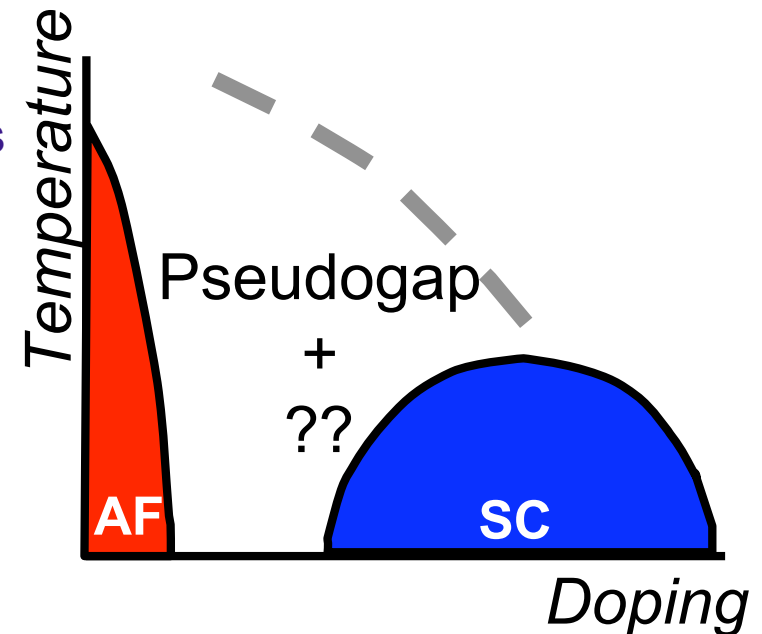
Even short stripes can generate pairing

Hard to detect!

Disorder (chemical dopants)

Rounds transitions

Can destroy order!

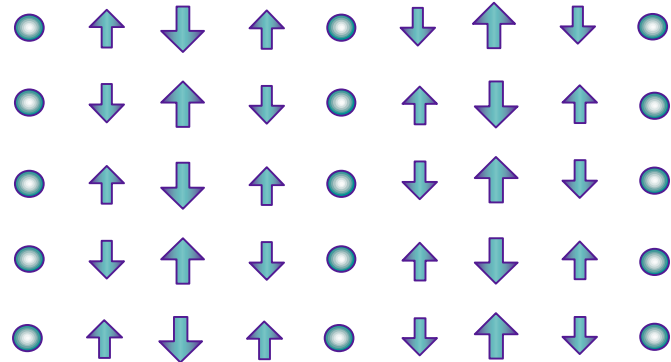


How do we define and detect phases  
with nanoscale pattern formation?

# What's a Stripe?

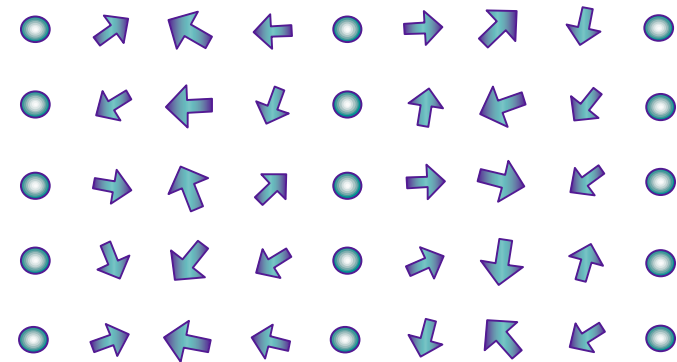
---

Most Ordered



*Unidirectional Spin and  
Charge Density Wave*

Less Ordered

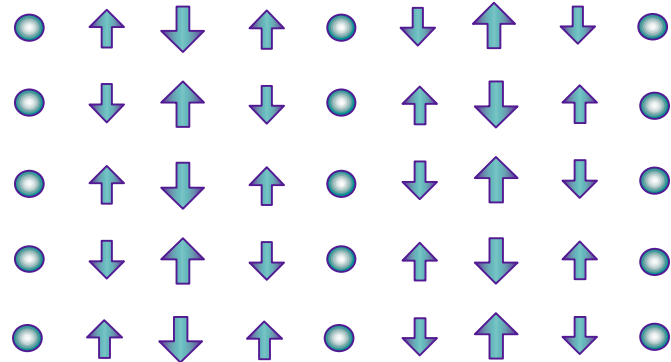


*Unidirectional Charge  
Density Wave*

# What's a Stripe?

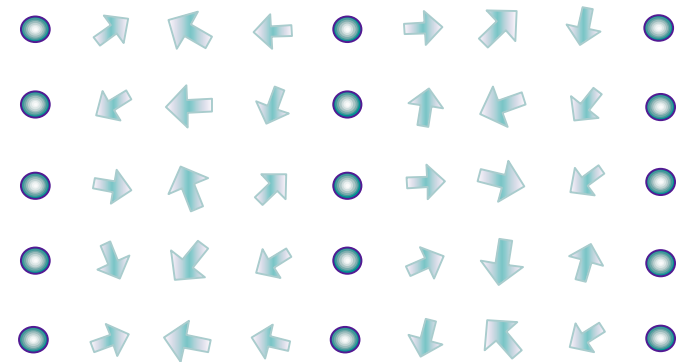
---

Most Ordered



*Unidirectional Spin and  
Charge Density Wave*

Less Ordered

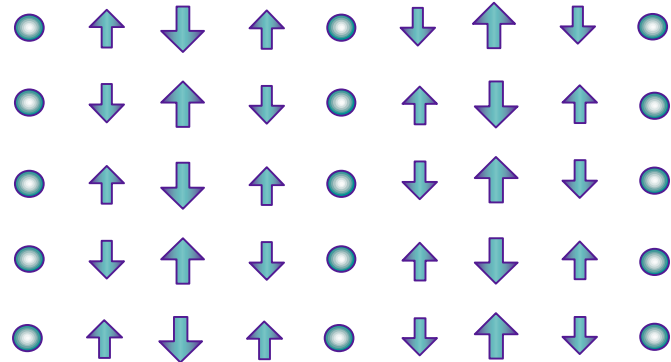


*Unidirectional Charge  
Density Wave*

# What's a Stripe?

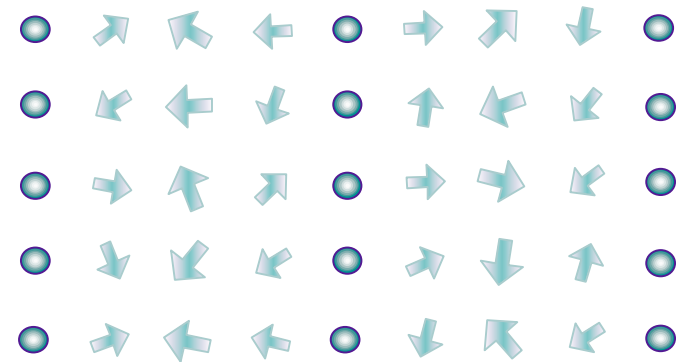
---

Most Ordered



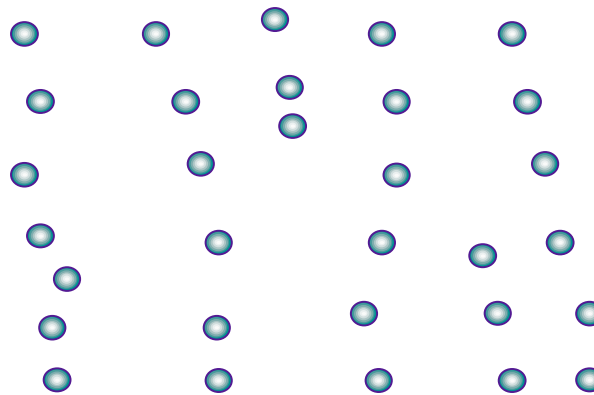
*Unidirectional Spin and  
Charge Density Wave*

Less Ordered



*Unidirectional Charge  
Density Wave*

Even Less Ordered

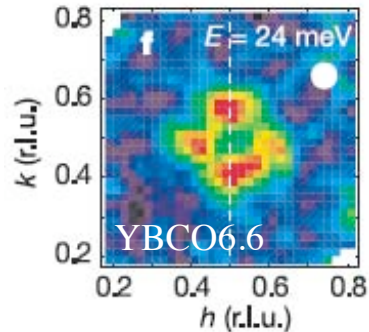


*Oriented Charge  
(nematic)*



# Stripes in what probes?

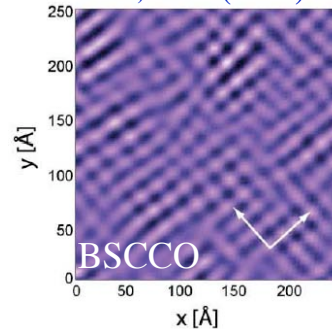
Hayden *et al.*, Nature (2004)



**Neutron Scattering**  
(*bulk probe*)

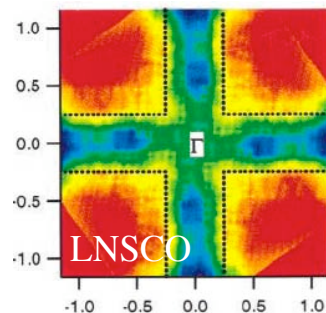
LaSrCuO, LaCuO, YBaCuO (not BiSrCaCuO)

Howald *et al.*, PRB (2003)



**Scanning Tunneling Microscopy**  
(*surface probe*)  
BiSrCaCuO

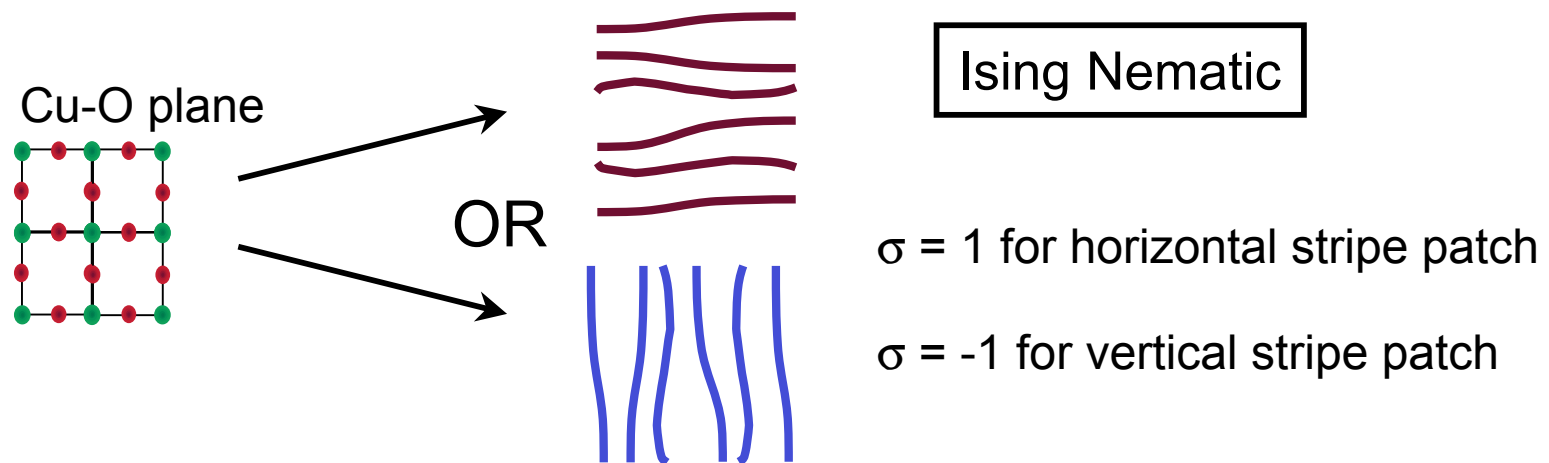
Zhou *et al.*, Science (1999)



**Angle-Resolved Photoemission Spectroscopy**  
(*surface probe*)  
BiSrCaCuO, YBaCuO

# Stripes + Disorder → Random Field Ising Model

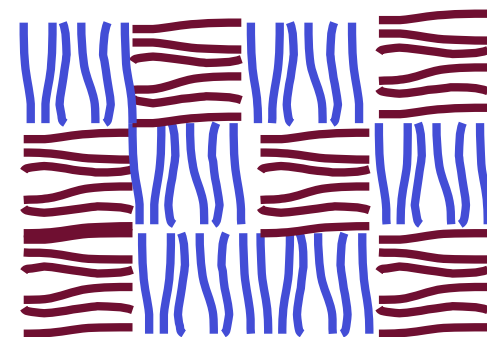
Stripes lock to a crystal direction



Disorder favors one direction locally

$$H = -J \sum_{\langle i,j \rangle} \sigma_i \sigma_j - \sum_i (H + h_i) \sigma_i$$

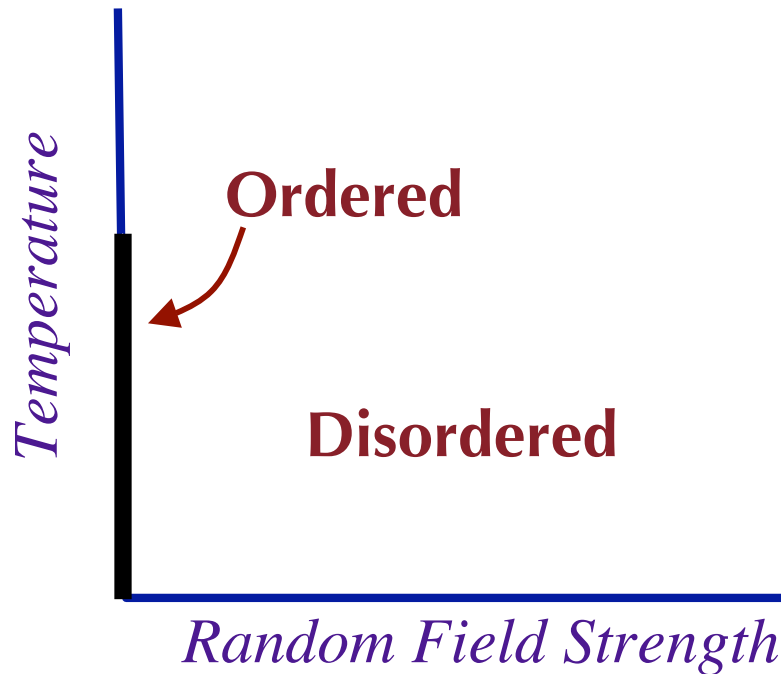
RANDOM FIELD ISING MODEL



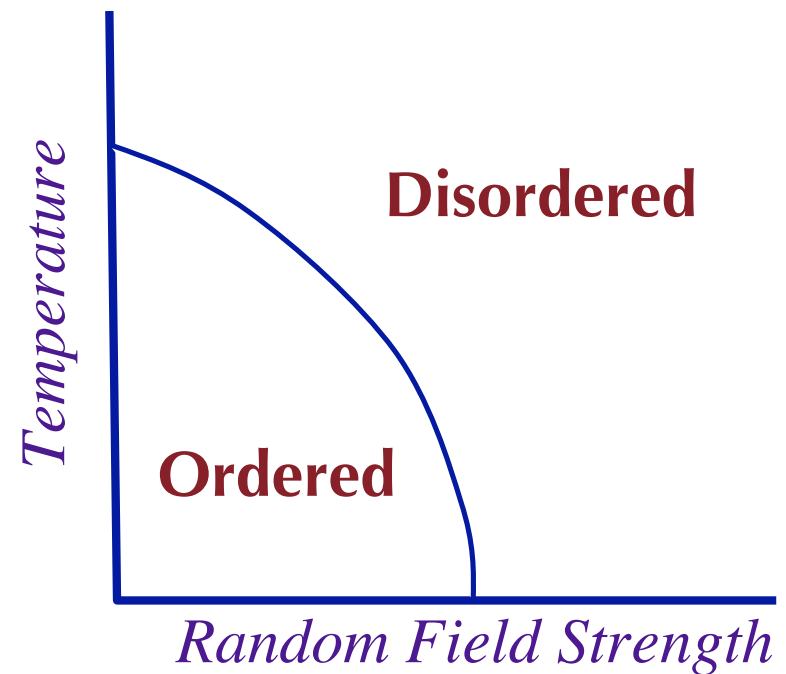
# Random Field Ising Model

---

**Two Dimensions**



**Three Dimensions**



$$H = -J \sum_{\langle i,j \rangle} \sigma_i \sigma_j - \sum_i h_i \sigma_i$$

# Noise: Snap, Crackle, Pop

---

Pencil



*Snap*

Fire



*Crackle*

Popcorn



*Pop*

Snap:

One large, system-size event

Crackle:

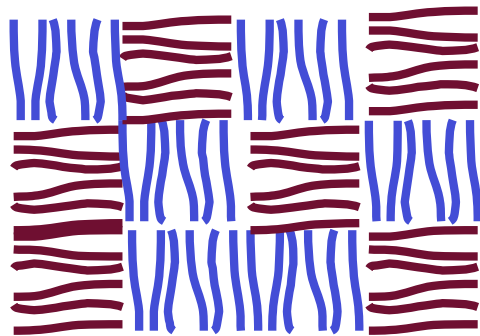
Many events at random times, of random sizes.

Pop:

Many small, same-sized events at random times

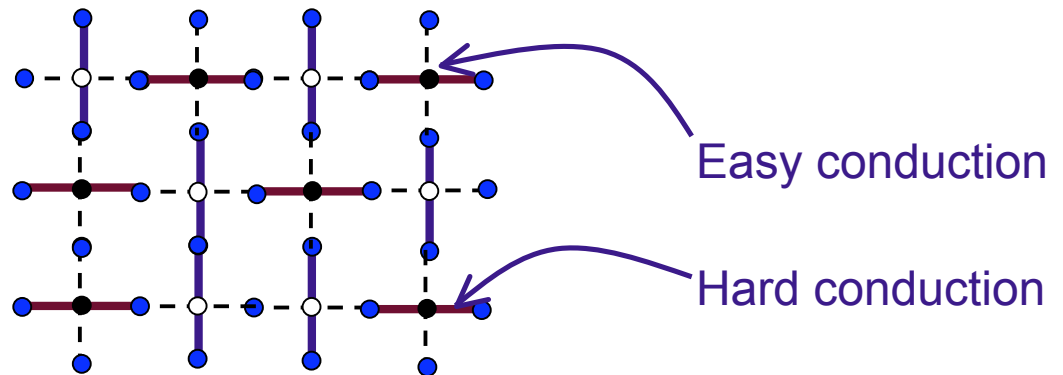
# Transport

Stripe Patches



Maps To

Resistor Network



Calculations:

Monte Carlo Simulation of random field Ising Model

Each configuration maps to a resistor network

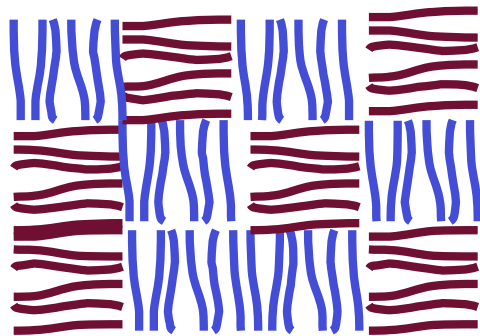
$R_{xx}$  and  $R_{yy}$  calculated via

bond propagation algorithm (Frank *et al.*, PRB 1988)

(Generalized to planar Ising models: Loh, EC, PRL 2006)

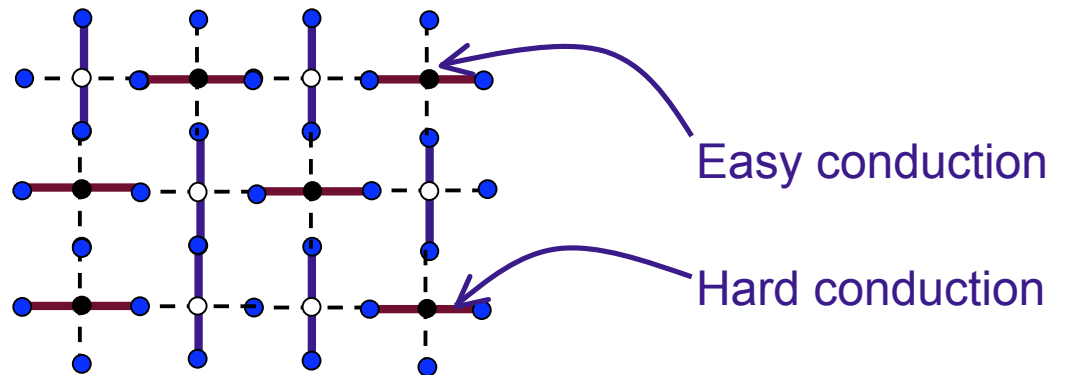
# Transport

## Stripe Patches



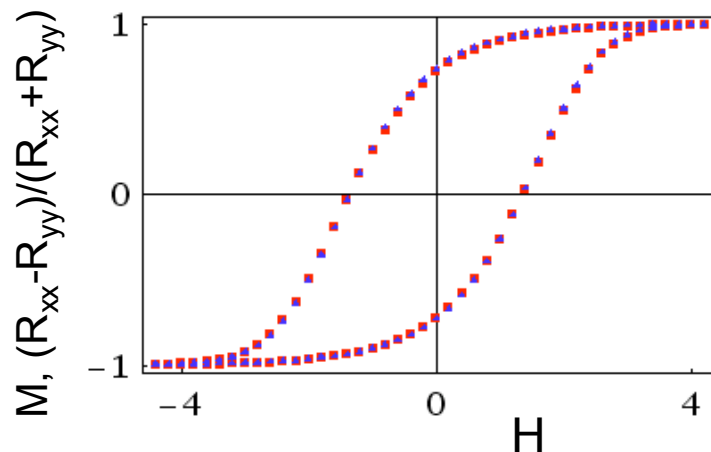
Maps To

## Resistor Network



Resistance Anisotropy and RFIM Magnetization exhibit hysteresis

“Magnetization” = orientational order



■ Orientational Order

▲  $(R_{xx} - R_{yy}) / (R_{xx} + R_{yy})$

LXL = 300X300

$T=0$ ;  $\Delta = 2.8$  J;  $R_{\text{large}}/R_{\text{small}} = 2$

# Confined Geometries: Telegraph Noise

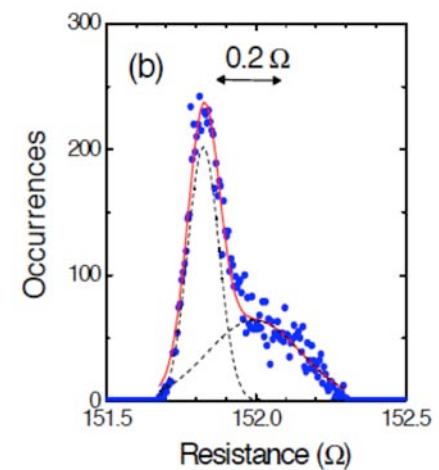
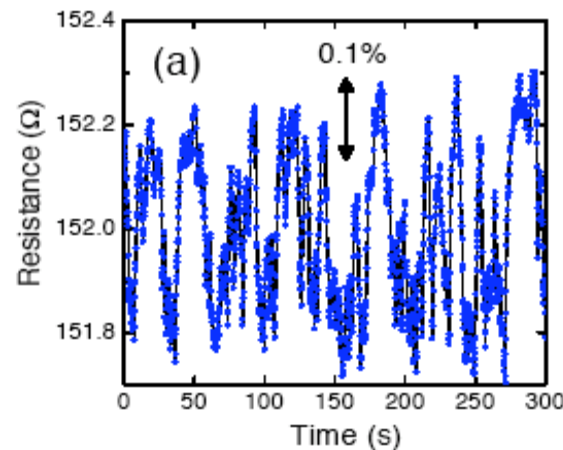
## Experiment

Bonetti *et al.*, PRL 93, 087002 (2004).

YBCO nanowire  
(underdoped)

$T=100\text{K}$   
 $500\text{nm}\times 250\text{nm}$

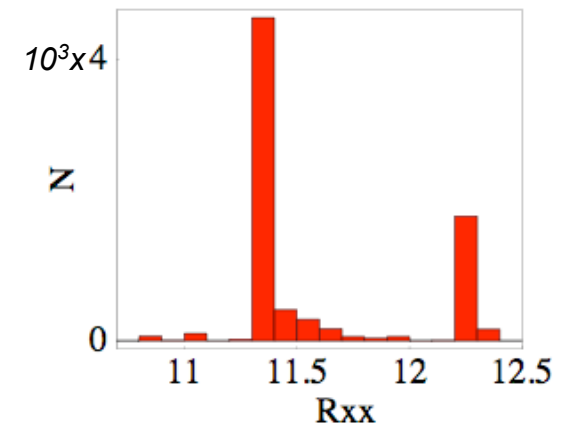
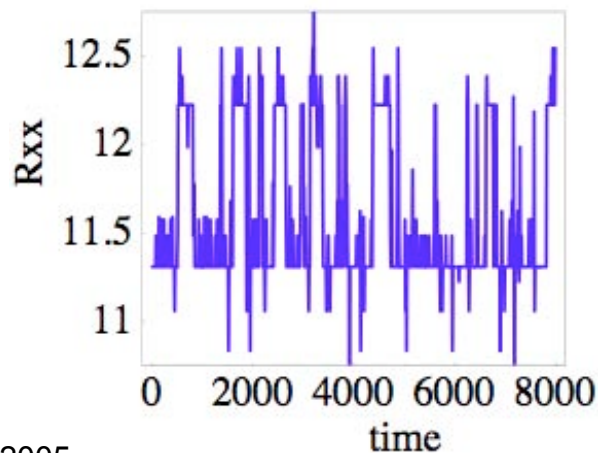
Large switch  $\approx 5$  patches



## Theory

EC *et al.*, PRL 96, 097003 (2006).

- $R_{\text{large}}/R_{\text{small}} = 2$
- Size: 6X6 patches
- Disorder  $R=2.8$  J
- $T = .5$  J
- Dimension = 2
- Stripe correlation length  
~ 40nm(from neutron data)

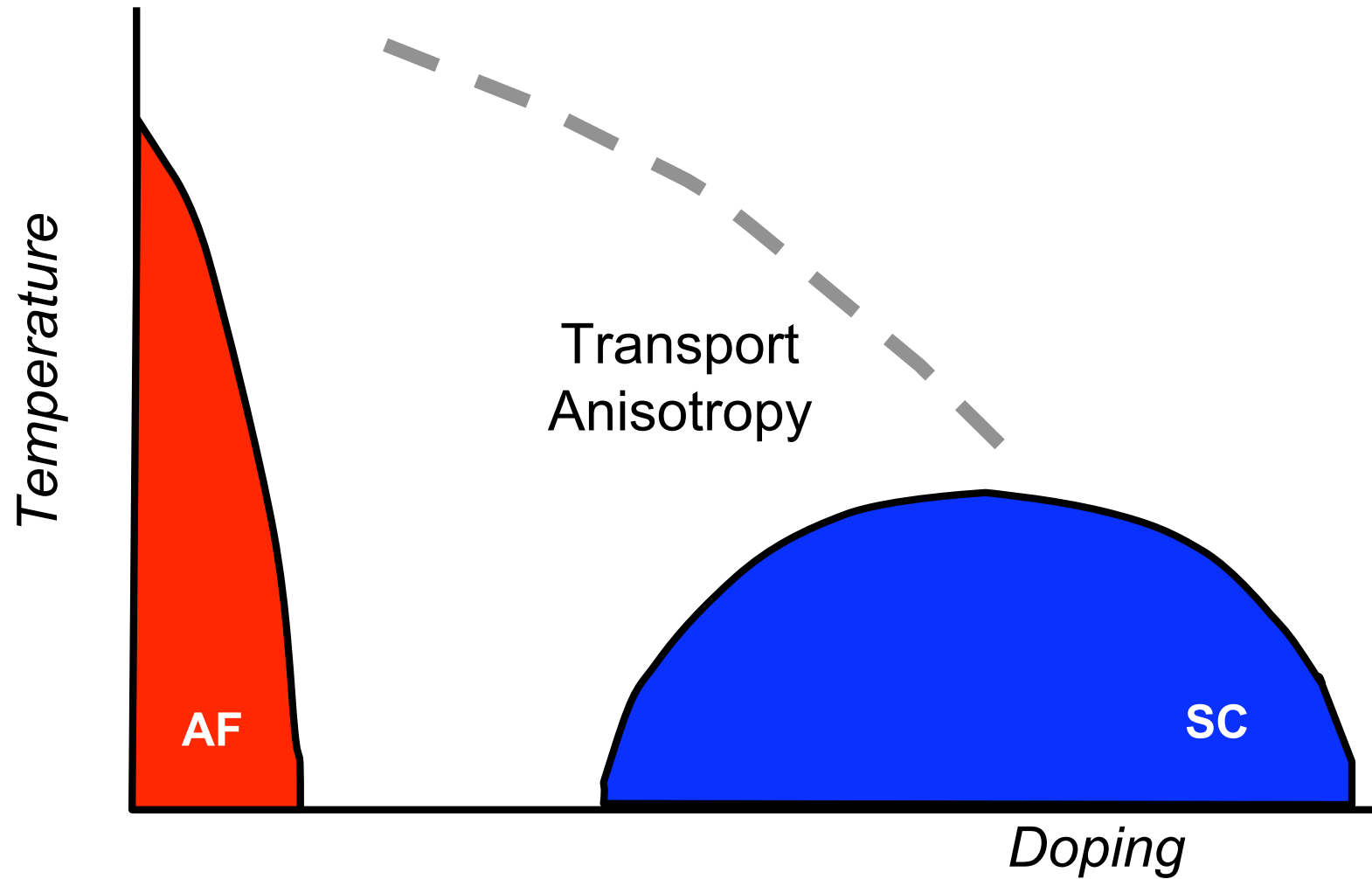


see also Reichhardt *et al.*, Europhys. Lett. 2005



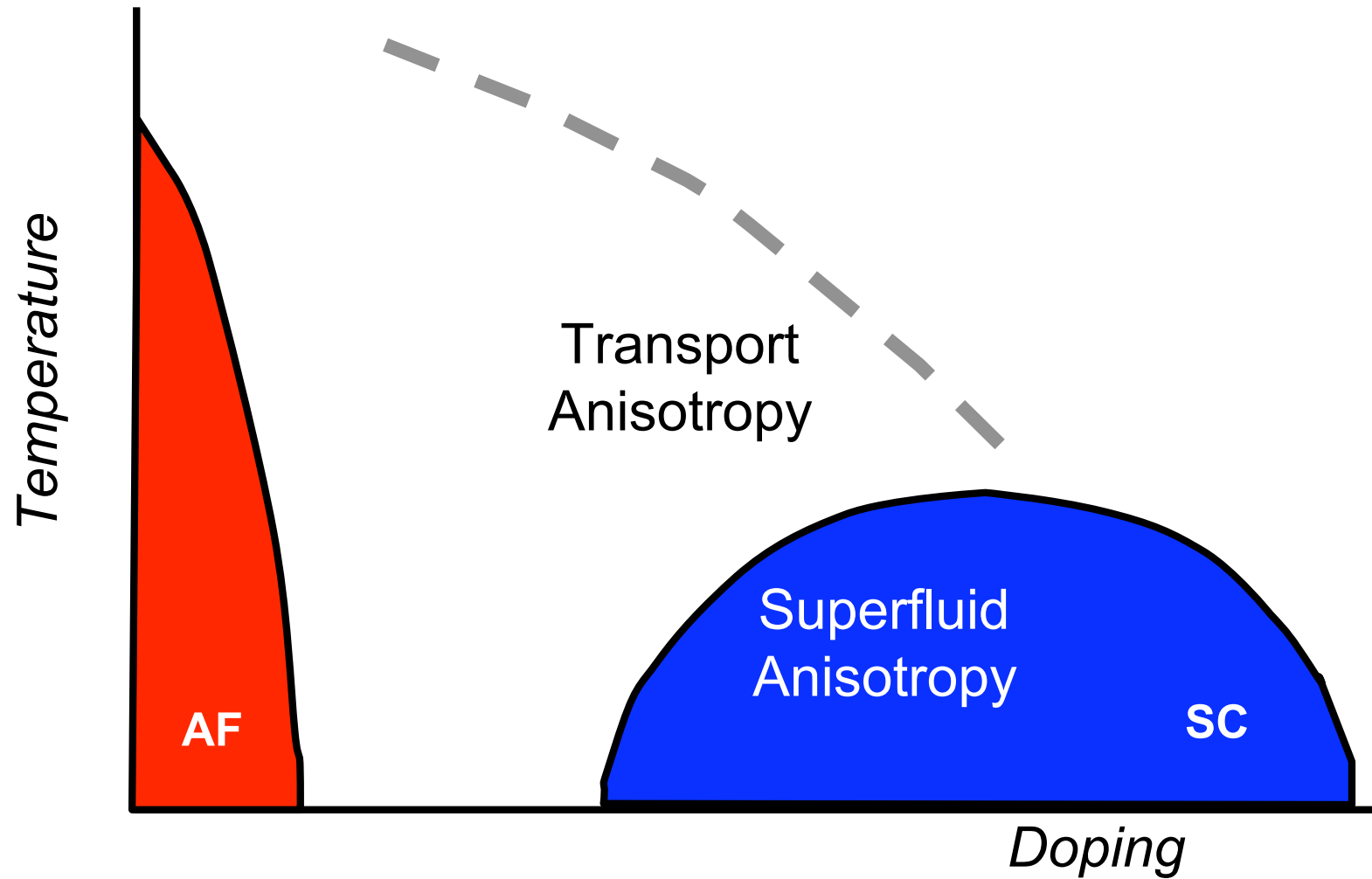
That was for the normal state...

---



That was for the normal state...

---



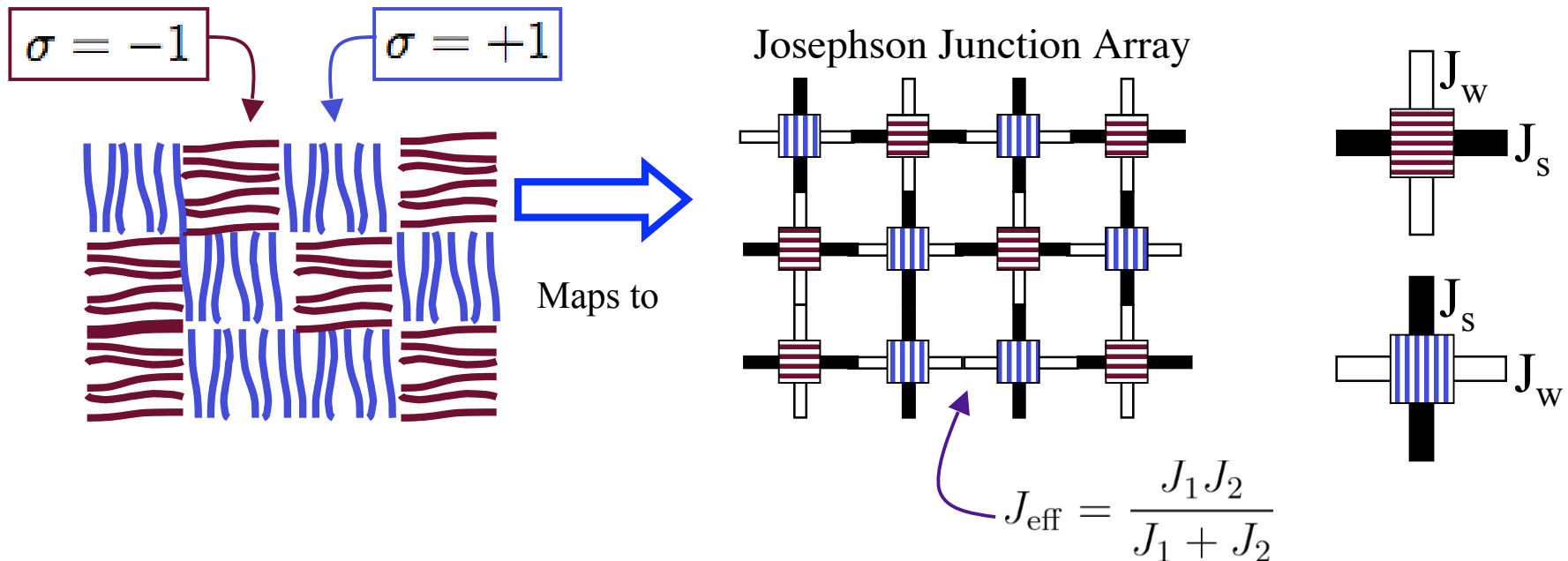
# Superfluid Density Anisotropy

Calculations:

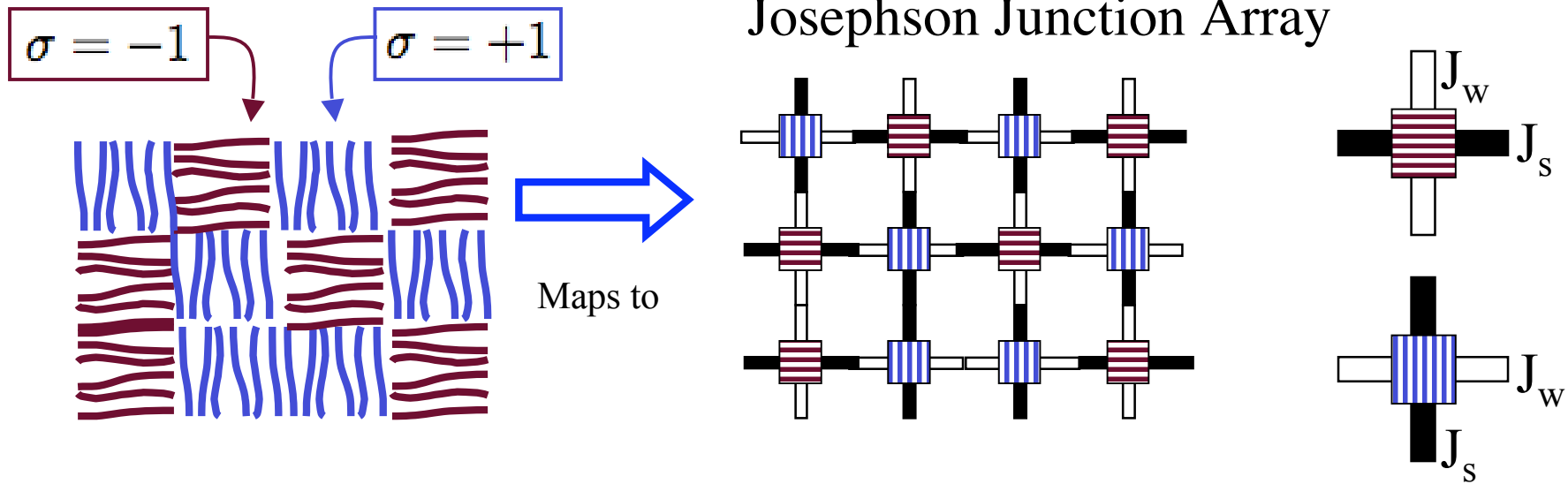
Monte Carlo Simulation of random field Ising Model

Each configuration maps to Josephson Junction Array (JJA)

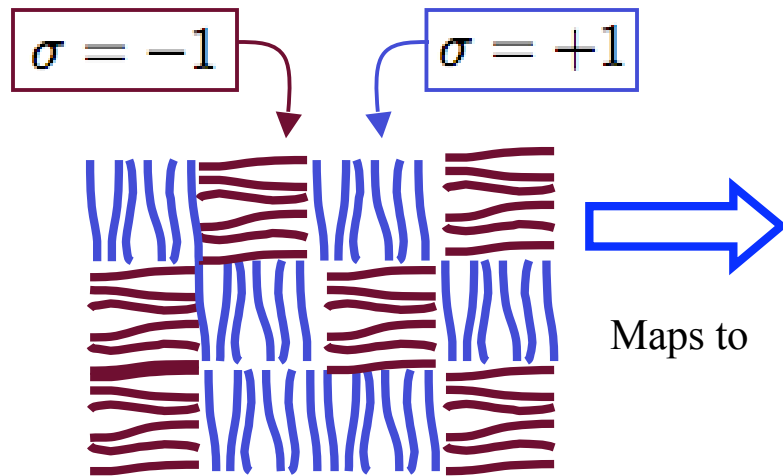
Monte Carlo simulation for each JJA pattern



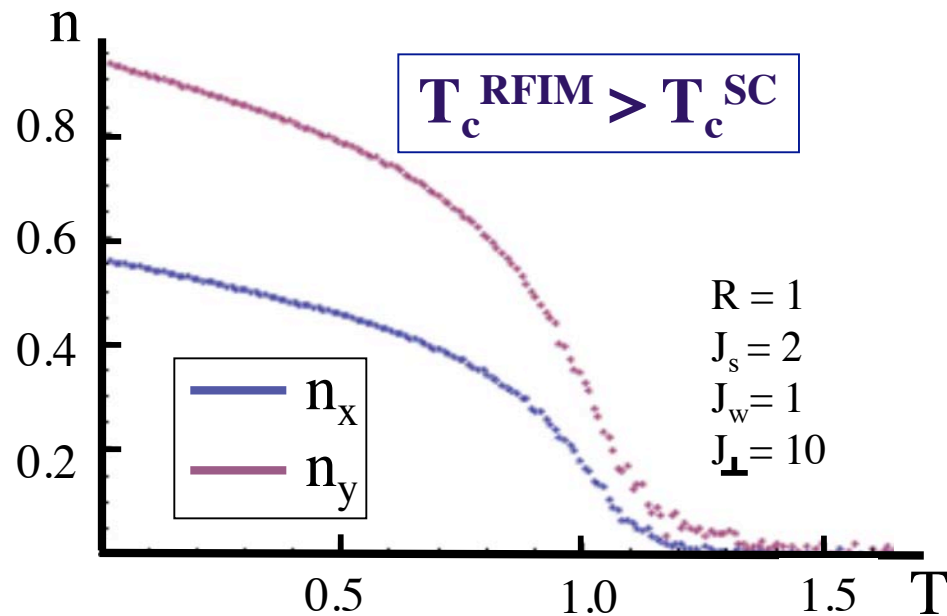
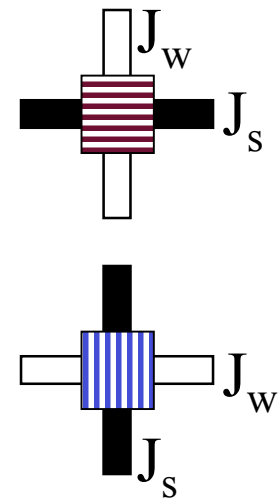
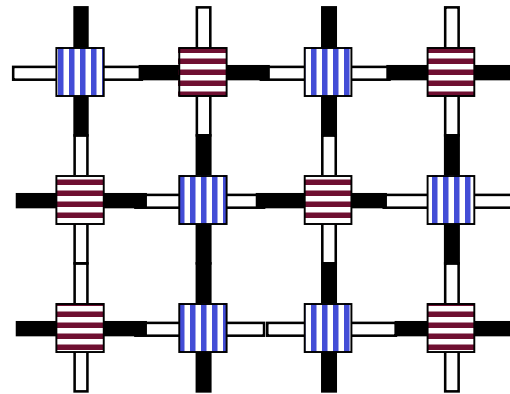
# Superfluid Density Anisotropy



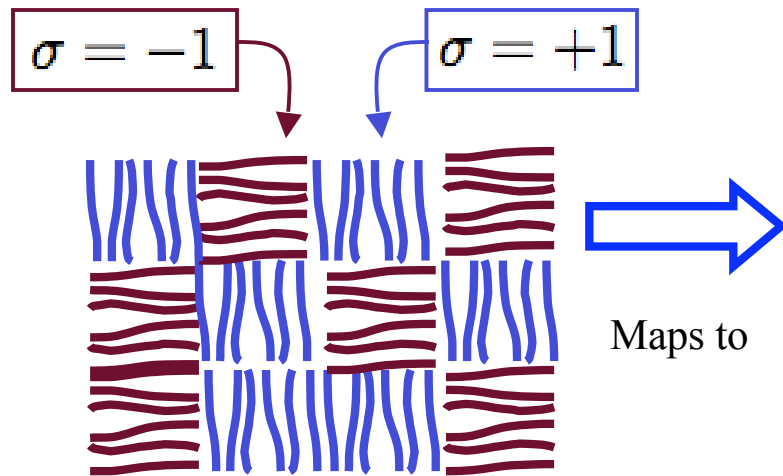
# Superfluid Density Anisotropy



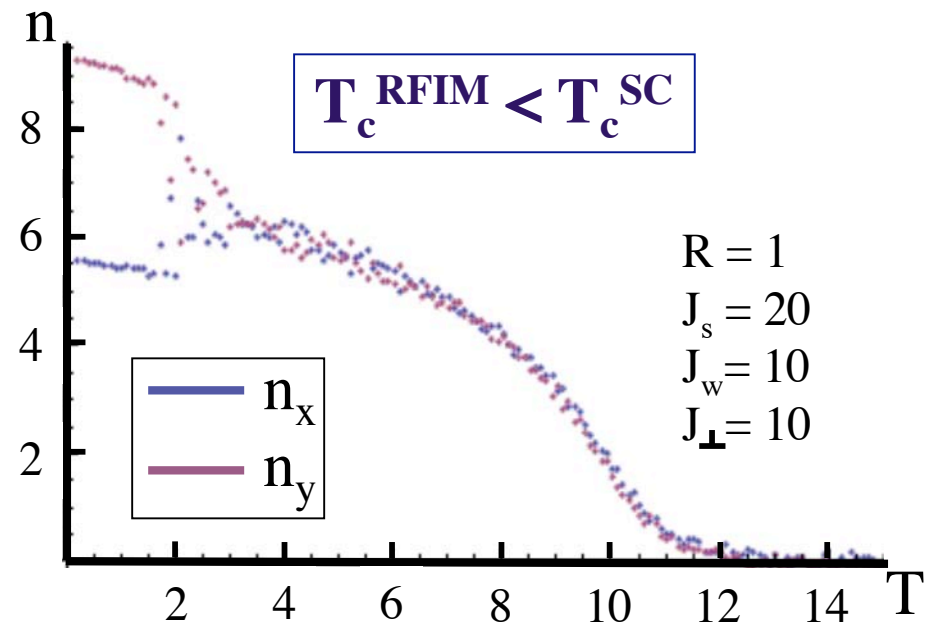
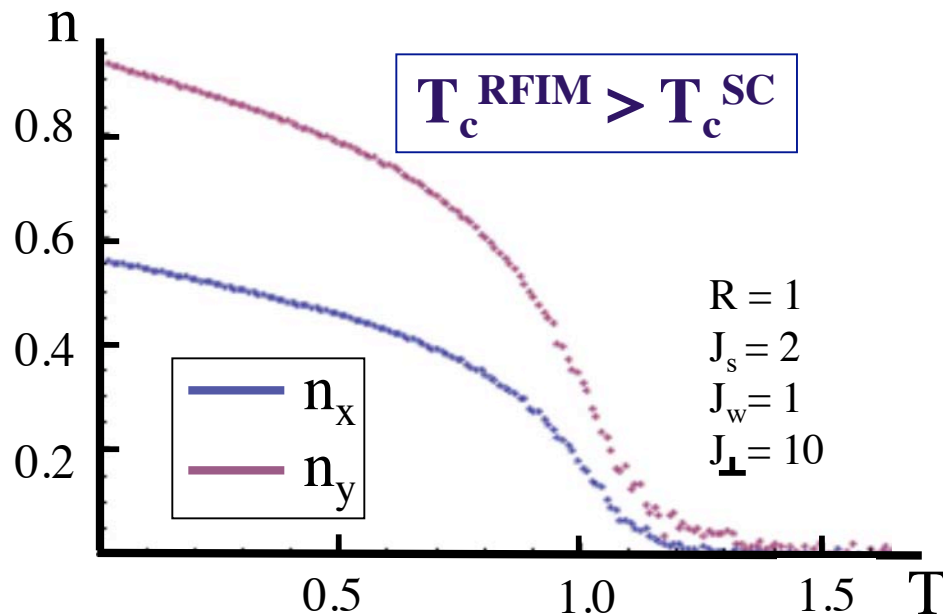
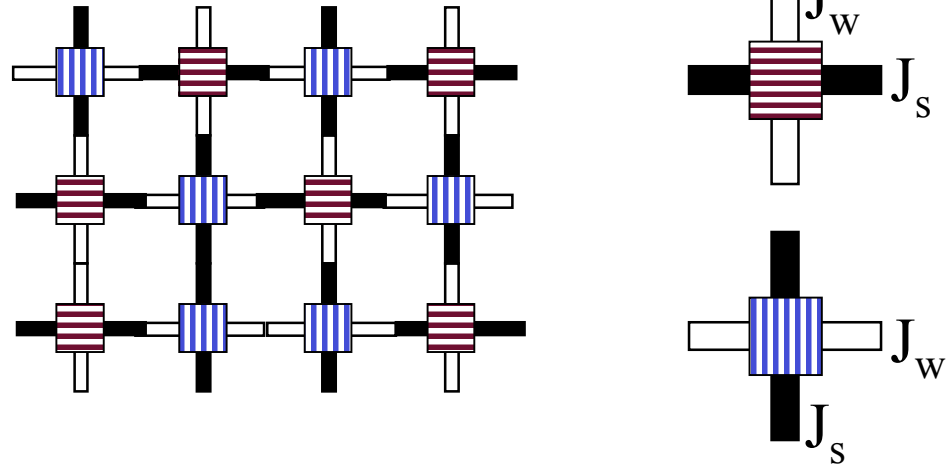
Josephson Junction Array



# Superfluid Density Anisotropy



Josephson Junction Array



# Hysteretic Superfluid Density Anisotropy

Apply an orienting field, “H”

*e.g.*, Uniaxial Strain on a Thin Film

*Stripe Orientation*

Ordered

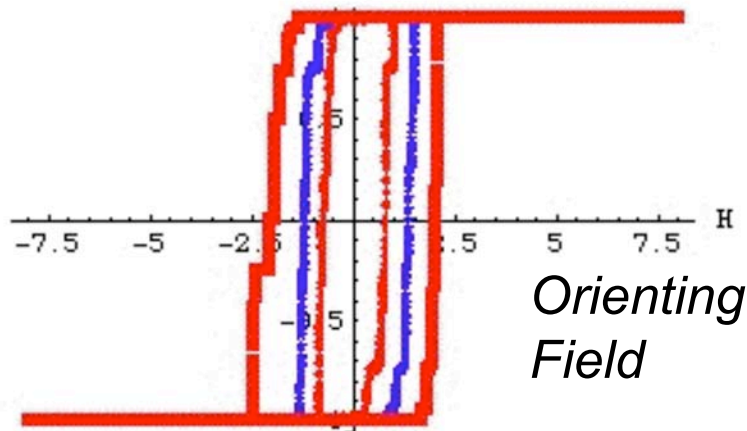
$\Delta=1$

$J_s=2$

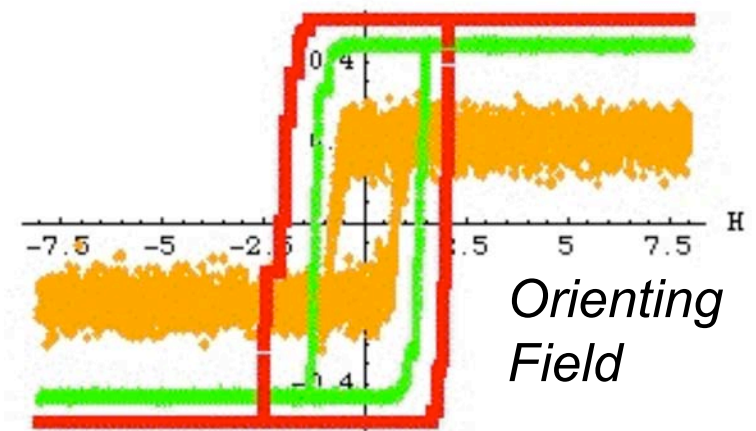
$J_w=1$

$L=8$

$T=0,.5,1$



*Superfluid Anisotropy*



**Intermediate disorder:** Weak disorder within planes, Strong disorder between planes.  
Planes “snap” individually

*with B. Phillabaum, Y. Loh*

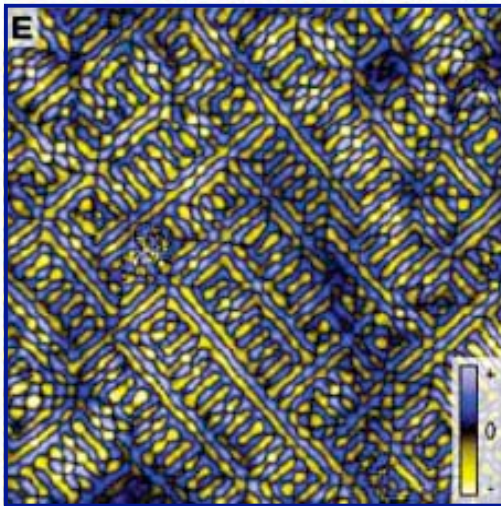


# Comparisons to STM

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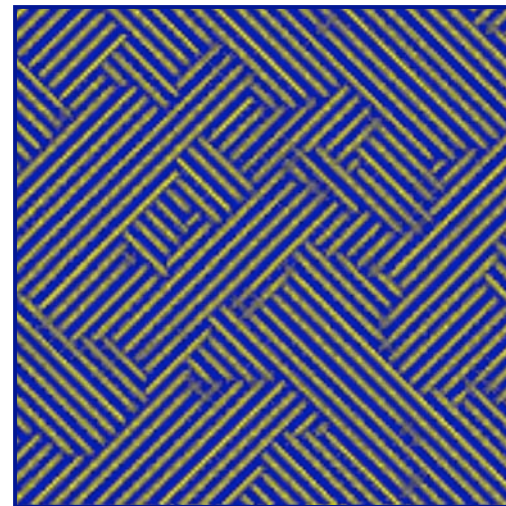
## Low Temperature Electronic Glass with Unidirectional Domains

Experiment



$\text{Ca}_{1.88}\text{Na}_{.12}\text{CuO}_2\text{Cl}_2$   
 $T=4.2\text{K}$   
Kohsaka *et al.*,  
Science **315**, 1380 (2007)

Theory

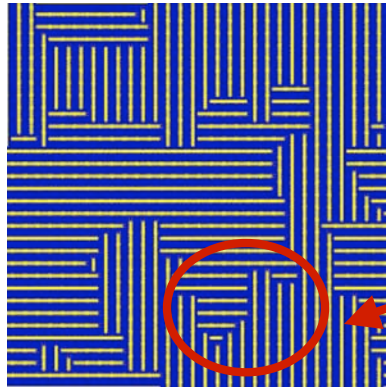


Layered system  
 $J_{\perp}=J_{\parallel}/10$  (Ising couplings)  
 $T=1.5J_{\parallel}$   
 $\Delta=1.5$  (disorder strength)

# Prediction: Telegraph Noise in STM

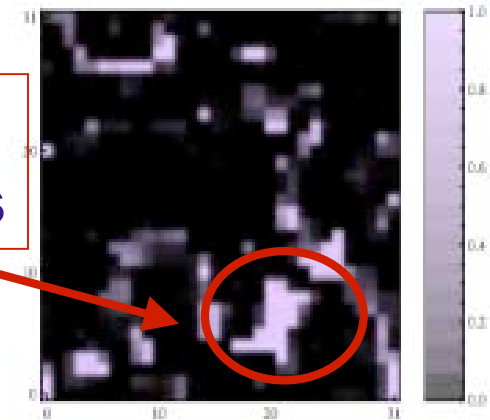
## Stripe Glass

$R=1.5$   
 $T=0.5$

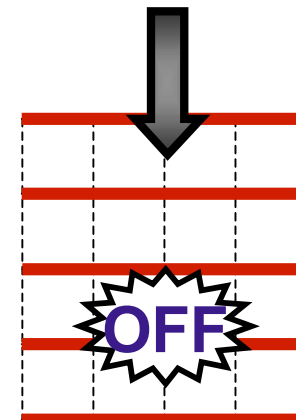
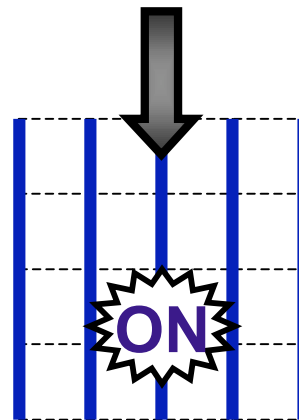


Active Regions are  
at Domain Boundaries

## Variance



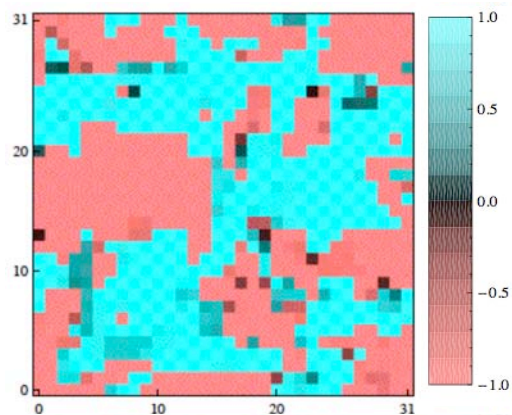
Place STM tip  
on a line at a  
stripe boundary



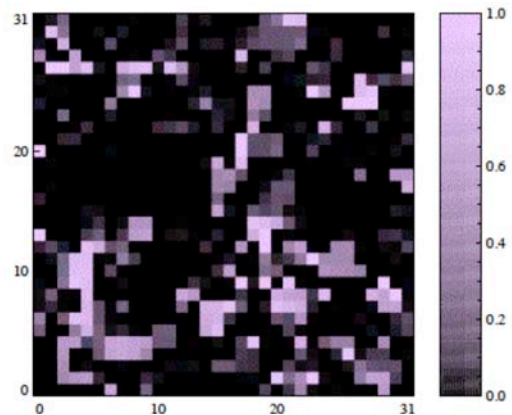
*Telegraph Noise*

**R=2.5**  
**T=0.5**

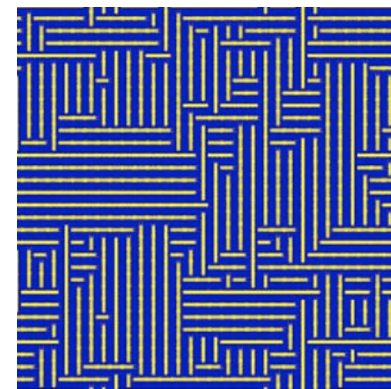
**Time Average**



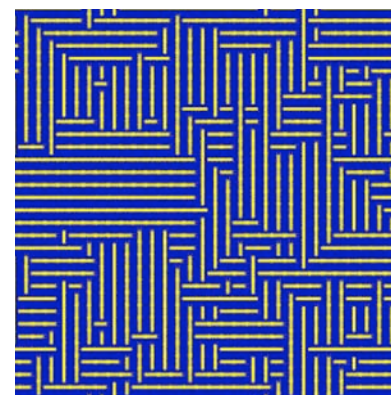
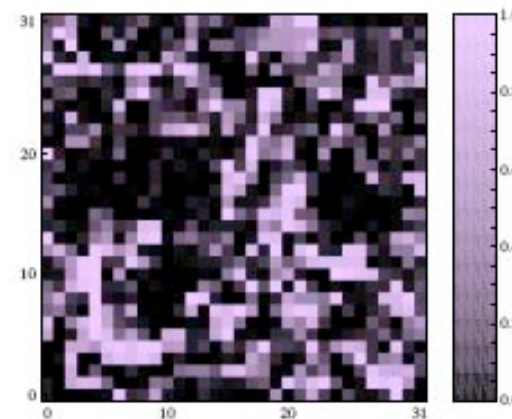
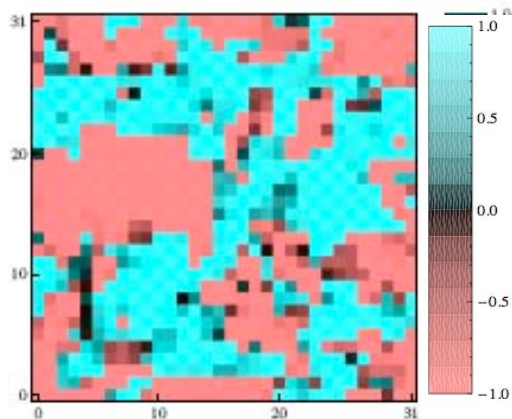
**Variance**



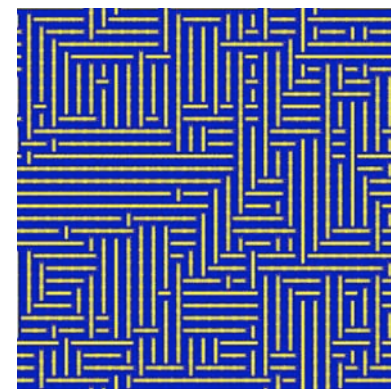
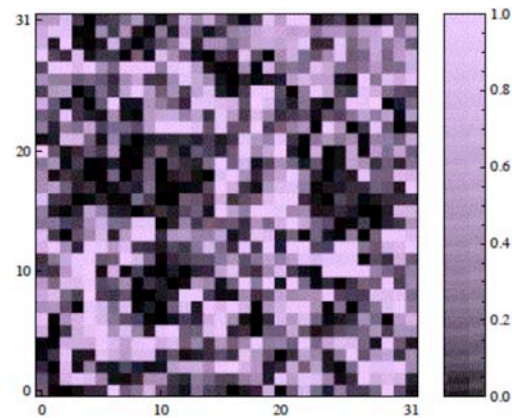
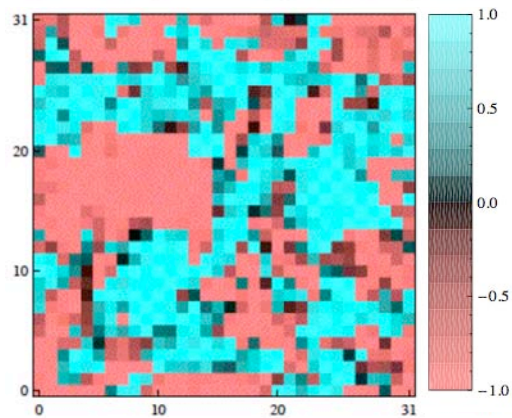
**Stripe Glass**



**R=2.5**  
**T=1.0**



**R=2.5**  
**T=1.5**



# Detecting Correlations

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Other possible sources of telegraph noise:

- Bad tip

- Defects hopping on surface

Power Spectrum

- Single uncorrelated switcher: Lorentzian power spectrum

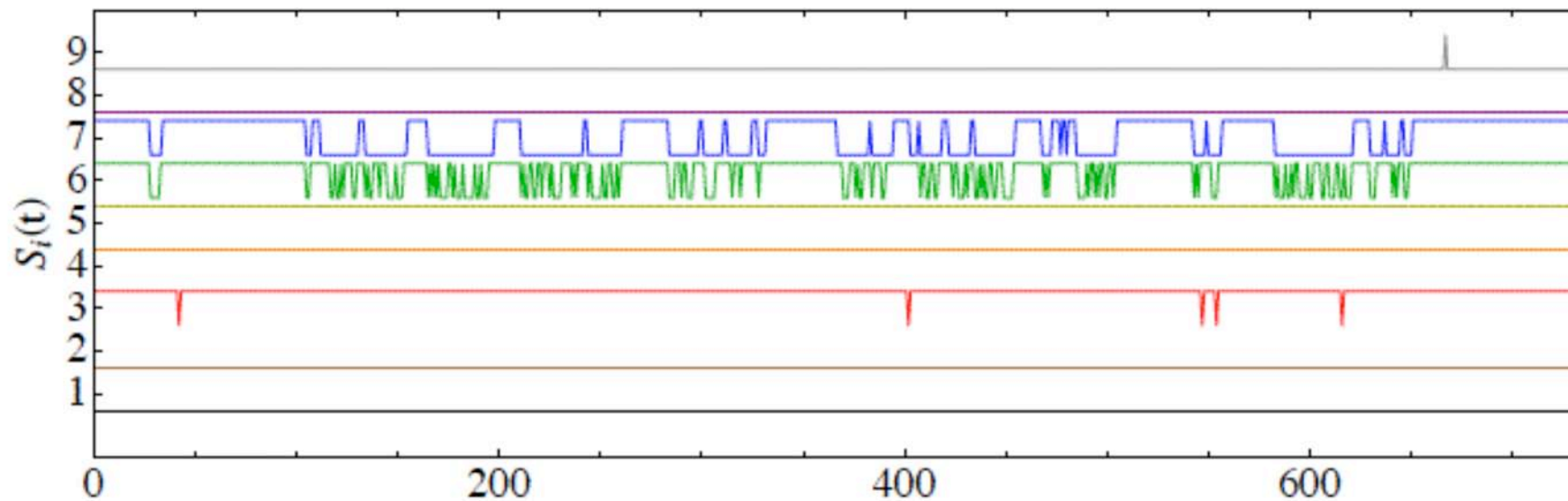
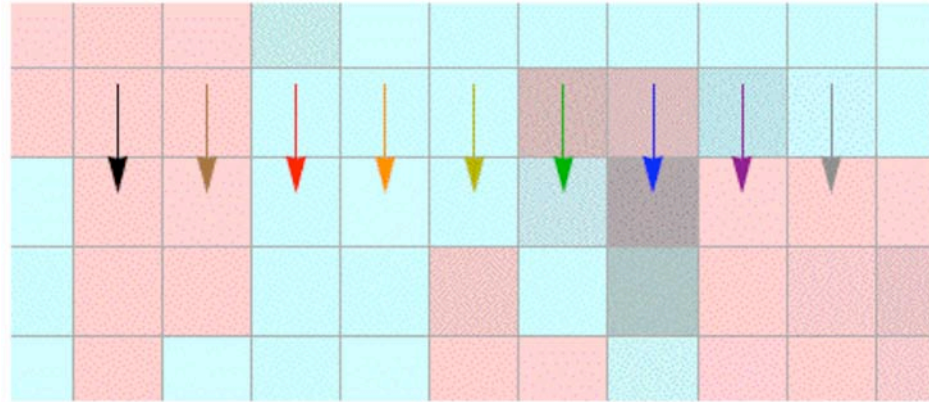
- Interactions cause deviations

Power spectrum is impractical for 25-60 second noise



# Spatial and Temporal Correlations in Noise

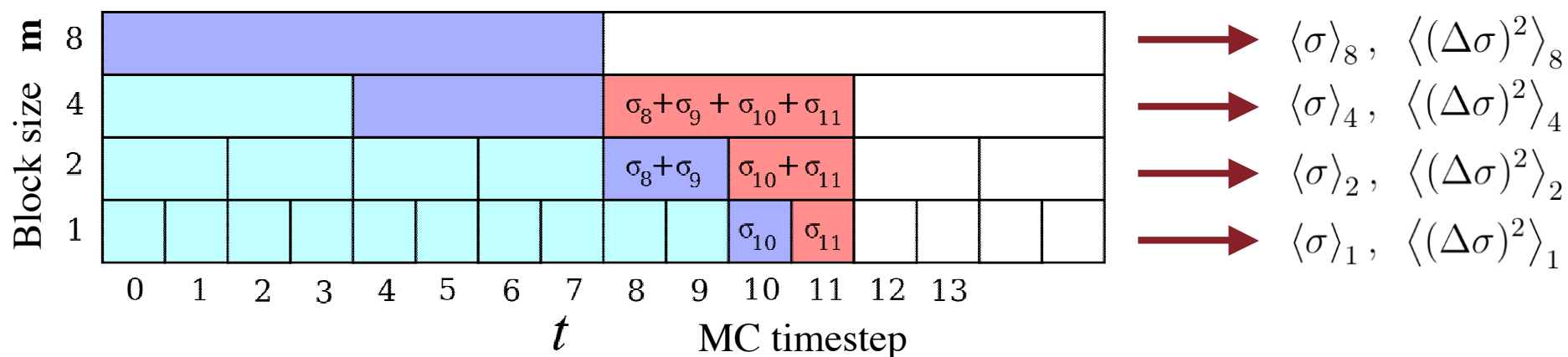
**R=2.5**  
**T=0.5**



# In-Situ Test for Correlations

"On-the-fly" Reblocking Algorithm

(Kent *et al.*, J. Comp. Chem. 2007)



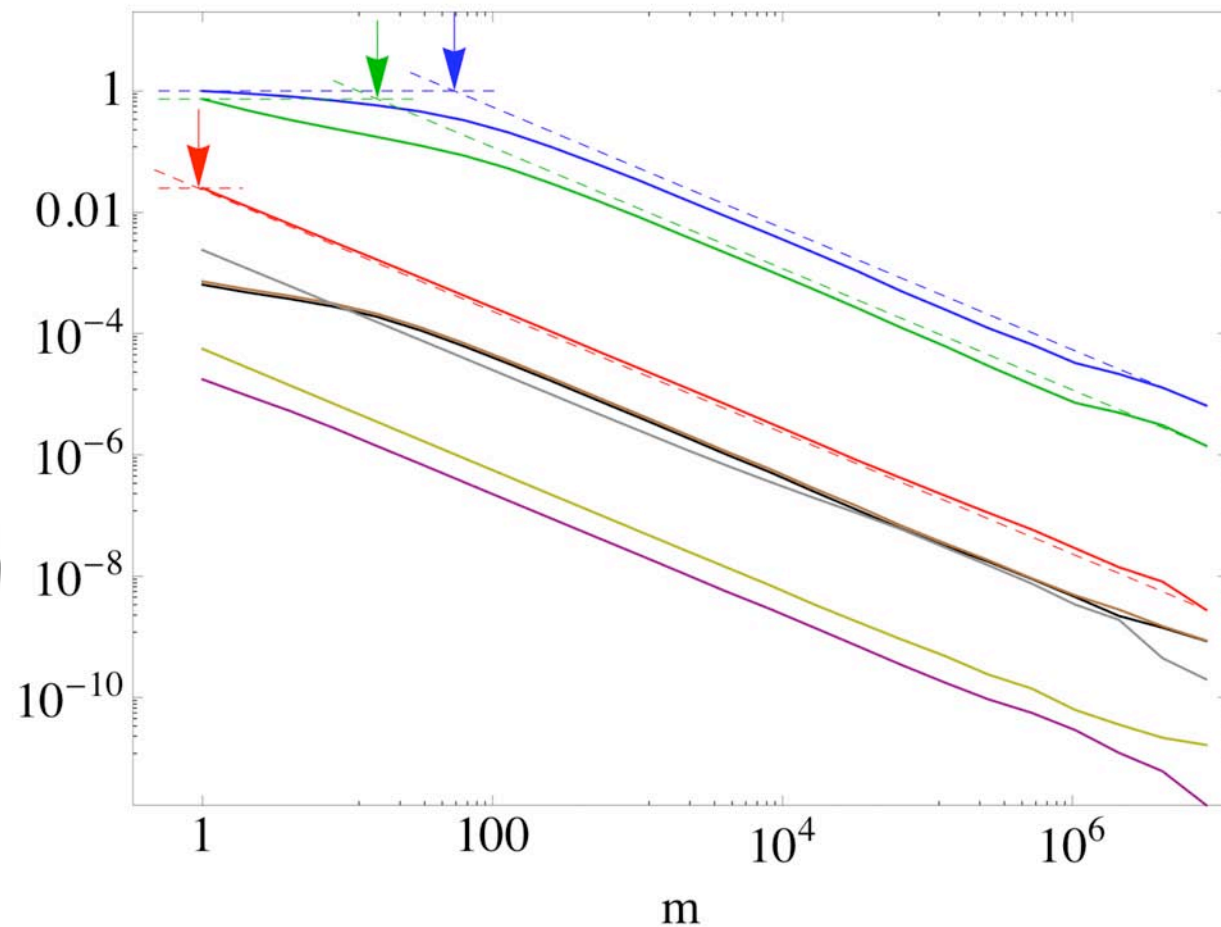
Each block spin is the average of the ones below it.

Accumulate averages and variances for each block size  $m$ .

Memory requirement =  $O(\log_2 N)$ , rather than  $O(N)$

# In-Situ Test for Correlations

Block  
Variance

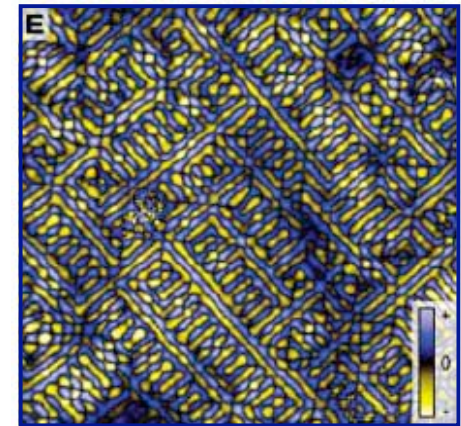


Low  $m$  deviations from horizontal line indicate correlations

Stripes + Host crystal + Disorder = Random Field Ising Model

Disorder makes stripes hard to detect. Need new ways to probe: *Noise, Hysteresis*

Transport: Switching noise in small systems in  $R_{xx}$   
Orientational Order measured by  $R_{xx}-R_{yy}$   
Similar for Superfluid Anisotropy



Scanning Noise Spectroscopy (STM):

Telegraph Noise at Domain Boundaries  
Active regions are at stripe cluster boundaries  
More active regions as temperature is raised  
Local Noise Maps out Stripe Clusters  
Spatial and Temporal Noise Correlations

