

Further we have let each coupling constant be re-scaled by $g \rightarrow -2g$ so that they coincide with our choices in the SM — hence

$$F_{\mu\nu}^i = \partial_\mu A_\nu^i - \partial_\nu A_\mu^i + g_2 \epsilon_{ijk} A_\mu^j A_\nu^k$$

$$B_{\mu\nu} = \partial_\mu B_\nu - \partial_\nu B_\mu$$

$$G_{\mu\nu}^m = \partial_\mu G_\nu^m - \partial_\nu G_\mu^m + g_3 f_{mnp} G_\mu^n G_\nu^p$$

and similarly in the covariant derivatives.

Next consider the form of the gauged Kähler potential action term!
In general it has the form

$$\overline{K}_K = \frac{1}{16} \int dV K_S \quad \text{with}$$

$$K_S = Z_k(\theta, \bar{\theta}) \phi e^{\mathcal{L}^{V.T.}} \bar{\phi}$$

where recall that ϕ is in a particular representation of the gauge group

$$\phi'_a = (e^{ig\Lambda^i T^i})_{ab} \phi_b$$

$$\phi'_a = \phi_b (e^{-ig\bar{\Lambda}^i T^i})_{ba}$$

with chiral gauge parameters $D_\alpha \bar{\Lambda}^i = 0$ &
 $\bar{D}_{\dot{\alpha}} \Lambda^i = 0$. The gauge field recall

transforms as

$$e^{gV^i T^i} = e^{ig\bar{\Lambda} \cdot T} e^{gV \cdot T} e^{-ig\Lambda \cdot T}$$

So that

$$K = K(\phi e^{gV \cdot T} \phi) = \phi_a (e^{gV^i T^i})_{ab} \phi_b$$

is gauge invariant $K' = K$.

Once again we can transform to the $W-Z$ gauge so that

$$V^i = \theta \sigma^\mu \bar{\theta} A_\mu^i + \frac{1}{2} \theta^2 \theta^\alpha \lambda_\alpha^i + \frac{1}{2} \theta^2 \bar{\theta}_{\dot{\alpha}} \bar{\lambda}^{\dot{\alpha} i} + \frac{1}{4} \theta^2 \bar{\theta}^2 D^i$$

with $A_\mu, \lambda, \bar{\lambda}, D$ in the $W-Z$ gauge as
 is the matter field ϕ_a

i.e. $\phi'_a = (e^{ig\Lambda_{WZ} \cdot T})_{ab} \phi_b \xrightarrow{\text{re-label}} \phi_a, \text{ etc.}$

As before we are left with a residual "ordinary" gauge transformation after the W-Z gauge is chosen;

$$\phi'_a = (e^{ig\Lambda \cdot T})_{ab} \phi_b \quad \text{with } \Lambda^i = e^{-i\theta\gamma\bar{\theta}} \omega^i(x)$$

$$\bar{\phi}'_a = \bar{\phi}_b (e^{-ig\bar{\Lambda} \cdot T})_{ba} \quad \text{with } \bar{\Lambda}^i = e^{+i\theta\gamma\bar{\theta}} \omega^i(x)$$

i.e. $\omega^{it} = \omega^i$.

From the chiral & anti-chiral representation point of view, we have

$$\begin{aligned} \phi'_a &= e^{-i\theta\gamma\bar{\theta}} (A'_a + \theta\chi'_a + \theta^2 F'_a) \\ &= e^{-i\theta\gamma\bar{\theta}} (e^{ig\omega \cdot T})_{ab} (A_b + \theta\chi_b + \theta^2 F_b) \end{aligned}$$

&

$$\begin{aligned} \bar{\phi}'_a &= e^{+i\theta\gamma\bar{\theta}} (\bar{A}'_a + \bar{\theta}\bar{\chi}'_a + \bar{\theta}^2 \bar{F}'_a) \\ &= e^{+i\theta\gamma\bar{\theta}} (\bar{A}_b + \bar{\theta}\bar{\chi}_b + \bar{\theta}^2 \bar{F}_b) (e^{-ig\omega \cdot T})_{ba} \end{aligned}$$

Once again we can expand $e^{gV \cdot T}$ in the W-2 gauge

$$\begin{aligned}
 e^{\pm gV \cdot T} &= 1 \pm gV \cdot T + \frac{1}{2} g^2 (V \cdot T)(V \cdot T) \\
 &= 1 \pm g \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) \pm \frac{g}{2} \theta^2 \bar{\theta}_2 (\Sigma^2 \cdot T) \\
 &\quad \pm \frac{g}{2} \bar{\theta}^2 \theta^\alpha (\lambda_\alpha \cdot T) \\
 &\quad \pm \frac{g}{4} \theta^2 \bar{\theta}^2 (D \cdot T \pm g (A_\mu \cdot T)(A^\mu \cdot T))
 \end{aligned}$$

Along with the matter fields

$$\begin{aligned}
 \phi_a \phi_b &= (e^{+i\theta\gamma\bar{\theta}} (\bar{A}_a + \theta\bar{\chi}_a + \theta^2 \bar{F}_a)) (e^{-i\theta\gamma\bar{\theta}} (A_b + \theta\chi_b + \theta^2 F_b)) \\
 &= [\bar{A}_a + \theta\bar{\chi}_a + \theta^2 \bar{F}_a + i\theta\gamma\bar{\theta} \bar{A}_a - \frac{i}{2} \theta^2 \theta\gamma\bar{\theta} \bar{\chi}_a \\
 &\quad - \frac{1}{4} \theta^2 \bar{\theta}^2 \gamma^2 \bar{A}_a] \times [A_b + \theta\chi_b + \theta^2 F_b - i\theta\gamma\bar{\theta} A_b \\
 &\quad + \frac{i}{2} \theta^2 \bar{\chi}_b \gamma\bar{\theta} - \frac{1}{4} \theta^2 \bar{\theta}^2 \gamma^2 A_b]
 \end{aligned}$$

Recall also that the soft SUSY breaking terms are included in the $\theta, \bar{\theta}$ dependent wave-function factor

$$Z_K(\theta, \bar{\theta}) = Z_K (1 - m_k \theta^2 - \bar{m}_k \bar{\theta}^2 - m^2 \theta^2 \bar{\theta}^2)$$

For the SUSY invariant matter kinetic energy terms we must integrate over the vector measure picking out the D-term from this big product, that is the $\theta^2 \bar{\theta}^2$ term

$$\Gamma_{SK} = \frac{1}{16} \int dV K_s = \frac{1}{16} \int dV Z_k(\theta, \bar{\theta}) \phi_a (e^{gV})_{ab} \phi_b$$

Consider the soft-breaking terms first:

- 1) $-Z_k m^2 \theta^2 \bar{\theta}^2 \phi_a (e^{gV})_{ab} \phi_b = -Z_k m^2 \theta^2 \bar{\theta}^2 A_a^\dagger A_a$
- 2) $-Z_k m_k \theta^2 \phi e^{gV} \phi = -Z_k m_k \theta^2 [\bar{\theta}^2 F_a A_a]$
- 3) $-Z_k \bar{m}_k \bar{\theta}^2 \phi e^{gV} \phi = -Z_k \bar{m}_k \bar{\theta}^2 [\theta^2 \bar{A}_a F_a]$

Finally we are left with the SUSY invariant kinetic energy terms ^{gauge}

$$\begin{aligned} (\phi e^{gV} \phi)_D &= \frac{g}{4} \theta^2 \bar{\theta}^2 \bar{A} (\not{D} \cdot T + g (A_{\mu} \cdot T) (A^{\mu} \cdot T)) A \\ &+ \frac{g}{2} \bar{A} \bar{\theta}^2 \theta^\alpha (\not{\lambda}_\alpha \cdot T) \theta^4 + \frac{g}{2} \bar{\theta} \not{\lambda} \bar{\theta}^2 \bar{\theta}_\alpha (\not{\lambda}^\alpha \cdot T) A \\ &+ g \bar{A} \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) (-i \not{\theta} \not{\lambda} \bar{\theta} A) + g \bar{\theta} \not{\lambda} \bar{\theta} \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) \theta^4 \\ &+ g i \not{\theta} \not{\lambda} \bar{\theta} \bar{A} \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) A + \bar{A} (-\frac{g}{4} \theta^2 \bar{\theta}^2 \delta^2 A) \end{aligned}$$

$$\begin{aligned}
& + \bar{\theta} \bar{\chi}_a \frac{i}{2} \theta^2 \delta_{\mu}^{\nu} \chi_a \sigma^{\mu} \bar{\theta} + \theta^2 \bar{F}_a \theta^2 F_a \\
& + i \theta \not{\chi} \bar{\theta} \bar{A}_a (-i \theta \not{\chi} \theta A_a) - \frac{i}{2} \bar{\theta}^2 \theta \not{\chi} \bar{\chi}_a \theta \chi_a \\
& - \frac{1}{4} \theta^2 \bar{\theta}^2 \delta^{\mu\nu} \bar{A}_a A_a .
\end{aligned}$$

As usual we must exploit the θ & σ^{μ} identities:

The last 6 terms which came from the $\mathbb{1}$ in $e^{gU \cdot T}$ we analysed earlier see p. -283- to -285- to obtain

$$\theta^2 \bar{\theta}^2 \left[\bar{F}_a F_a + \frac{i}{4} \chi_a \not{\chi} \bar{\chi}_a + \delta_{\mu}^{\nu} \bar{A}_a \delta^{\mu} A_a - \frac{1}{4} \delta^2 (\bar{A}_a A_a) \right]$$

Some are left with the gauge coupling terms to analyze:

$$\begin{aligned}
\checkmark \quad \frac{g}{2} \bar{A} \bar{\theta}^2 \theta^{\alpha} (\lambda_{\alpha} \cdot T) \theta \chi &= -\frac{g}{2} \bar{A} \bar{\theta}^2 \theta^{\alpha} \theta^{\beta} (\lambda_{\alpha} \cdot T) \chi_{\beta} \\
&= -\frac{g}{4} \theta^2 \bar{\theta}^2 \bar{A} (\lambda \cdot T) \chi
\end{aligned}$$

$$\begin{aligned}
\checkmark \quad \frac{g}{2} \bar{\theta} \bar{\chi} \theta^2 \bar{\theta}_{\dot{\alpha}} (\bar{\lambda}^{\dot{\alpha}} \cdot T) A &= \frac{g}{2} \bar{\theta}_{\dot{\beta}} \bar{\chi}^{\dot{\beta}} \theta^2 \bar{\theta}_{\dot{\alpha}} (\bar{\lambda}^{\dot{\alpha}} \cdot T) A \\
&= -\frac{g}{2} \theta^2 \bar{\theta}^{\dot{\beta}} \bar{\theta}_{\dot{\alpha}} \bar{\chi}_{\dot{\beta}} (\bar{\lambda}^{\dot{\alpha}} \cdot T) A \\
&= -\frac{g}{4} \theta^2 \bar{\theta}^2 \bar{\chi} (\bar{\lambda} \cdot T) A
\end{aligned}$$

$$\begin{aligned}
 & \checkmark \quad g \bar{A} \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) (-i \theta \not{\partial} \bar{\theta} A) \\
 & = -ig \bar{A} \theta^\alpha \bar{\theta}^{\dot{\alpha}} (\sigma^\mu_{\alpha\dot{\alpha}} A_\mu \cdot T) \theta^\beta \bar{\theta}^{\dot{\beta}} \not{\partial}_{\beta\dot{\beta}} A \\
 & = -\frac{ig}{4} \theta^2 \bar{\theta}^2 \bar{A} (\sigma^\mu_{\alpha\dot{\alpha}} A_\mu \cdot T) \bar{\not{\partial}}^{\alpha\dot{\alpha}} A \\
 & = -\frac{ig}{2} \theta^2 \bar{\theta}^2 \bar{A} (A_\mu \cdot T) \not{\partial}^\mu A
 \end{aligned}$$

$$(\text{Tr}[\sigma^\mu \bar{\sigma}^\nu] = 2\eta^{\mu\nu})$$

$$\begin{aligned}
 & \checkmark \quad g i \theta \not{\partial} \bar{\theta} \bar{A} \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) A \\
 & = ig \theta^\alpha \bar{\theta}^{\dot{\alpha}} \not{\partial}_{\alpha\dot{\alpha}} \bar{A} \theta^\beta \bar{\theta}^{\dot{\beta}} (\sigma^\mu_{\beta\dot{\beta}} A_\mu \cdot T) A \\
 & = \frac{ig}{4} \theta^2 \bar{\theta}^2 \not{\partial}_{\alpha\dot{\alpha}} \bar{A} \bar{\sigma}^{\mu\alpha\dot{\alpha}} (A_\mu \cdot T) A \\
 & = \frac{ig}{2} \theta^2 \bar{\theta}^2 \not{\partial}^\mu \bar{A} (A_\mu \cdot T) A
 \end{aligned}$$

$$\begin{aligned}
 & \checkmark \quad g \bar{\theta} \not{\partial} \theta \theta \sigma^\mu \bar{\theta} (A_\mu \cdot T) \theta \not{\partial} \bar{\theta} \\
 & = -g \bar{\theta}^{\dot{\alpha}} \not{\partial}_{\dot{\alpha}\alpha} \theta^\alpha \sigma^\mu_{\beta\dot{\beta}} \bar{\theta}^{\dot{\beta}} (A_\mu \cdot T) \theta^\beta \not{\partial}_{\beta\dot{\beta}} \bar{\theta} \\
 & = -\frac{g}{4} \theta^2 \bar{\theta}^2 \not{\partial}_{\dot{\alpha}\alpha} \theta^\alpha \bar{\sigma}^{\mu\dot{\alpha}\alpha} (A_\mu \cdot T) \not{\partial}_{\beta\dot{\beta}} \bar{\theta}^{\dot{\beta}} = +\frac{g}{4} \theta^2 \bar{\theta}^2 \not{\partial}^\mu (A_\mu \cdot T) \not{\partial} \bar{\theta}
 \end{aligned}$$

So bringing this altogether we find

$$\begin{array}{c}
 \uparrow \\
 \text{TT} \\
 \frac{n}{1} \times
 \end{array}$$

$$\begin{aligned}
(\bar{\psi} e^{gV \cdot T} \psi)_{\mathcal{S}} &= \theta^2 \bar{\theta}^2 \left[\bar{F}_a F_a + \frac{g}{4} \bar{A} T^i A \mathcal{D}^i \right. \\
&\quad \left. - \frac{1}{4} \delta^2 (\bar{A}_a A_a) \right. \\
&\quad \left. + \frac{i}{4} \bar{\psi} \bar{\sigma}^\mu \left[\partial_\mu \psi + \frac{ig}{2} (A_\mu \cdot T) \psi \right] \right. \\
&\quad \left. - \frac{i}{4} \left[\partial_\mu \bar{\psi} - \frac{ig}{2} \bar{\psi} (A_\mu \cdot T) \right] \bar{\sigma}^\mu \psi \right. \\
&\quad \left. + \left[\partial_\mu \bar{A} - \frac{ig}{2} \bar{A} (A_\mu \cdot T) \right] \left[\partial^\mu A + \frac{ig}{2} (A^\mu \cdot T) A \right] \right. \\
&\quad \left. - \frac{g}{4} \left[\bar{A} (\lambda \cdot T) \psi + \bar{\psi} (\lambda \cdot T) A \right] \right]
\end{aligned}$$

Hence we find

$$\begin{aligned}
\Gamma_{\mathcal{S}\mathcal{K}} &= \frac{1}{16} \int dV K_{\mathcal{S}} = \frac{1}{16} \int dV Z_{\mathcal{K}} |\theta, \bar{\theta}| \bar{\psi} e^{gV \cdot T} \psi \\
&= \int d^4x \mathcal{L}_{\mathcal{S}\mathcal{K}} = \int d^4x (\mathcal{L}_{\mathcal{K}} + \mathcal{L}_{\mathcal{S}\mathcal{K}})
\end{aligned}$$

where

$$\begin{aligned}
\mathcal{L}_{\mathcal{S}\mathcal{K}} = & -m^2 A_a^\dagger A_a - m_{\mathcal{K}} \bar{F}_a A_a \\
& - \bar{m}_{\mathcal{K}} A_a^\dagger F_a
\end{aligned}$$

while the SUSY invariant Lagrangian is

$$\mathcal{L}_K = F_a^\dagger F_a - g (A_a^\dagger T_{ab}^i A_b) D^i + \frac{i}{2} \bar{\psi} \sigma^\mu \overleftrightarrow{D}_\mu \psi + (D_\mu A)^\dagger D^\mu A + g\sqrt{2} (A^\dagger (\lambda \cdot T) \psi + \bar{\psi} (\bar{\lambda} \cdot T) A)$$

where once again we have chosen $Z_K = 1$ and re-scaled $g \rightarrow -2g$ and

$$\begin{aligned} \psi &\rightarrow \sqrt{2} \psi & D &\rightarrow \sqrt{4} D \\ \bar{\psi} &\rightarrow \sqrt{2} \bar{\psi} & \lambda &\rightarrow \sqrt{4} \lambda \\ & & \bar{\lambda} &\rightarrow \sqrt{4} \bar{\lambda} \end{aligned}$$

Thus we see that the Kähler action results in the usual gauge coupling of the matter & smatter fields with the additional gaugino "Yukawa" type coupling to the matter-smatter pair. Finally it includes the auxiliary F-field quadratic as well as the D-field coupling to the scalar field bi-linear $A^\dagger T^i A$.

The covariant derivatives are given by

$$D_\mu A_a = \partial_\mu A_a - ig (A_\mu \cdot T)_{ab} A_b$$

$$(D_\mu A_a)^\dagger = \partial_\mu A_a^\dagger + ig A_b^\dagger (A_\mu \cdot T)_{ba}$$

$$D_\mu \psi_a = \partial_\mu \psi_a - ig (A_\mu \cdot T)_{ab} \psi_b$$

$$D_\mu \bar{\psi}_a = \partial_\mu \bar{\psi}_a + ig \bar{\psi}_b (A_\mu \cdot T)_{ba}$$

Note: Since $T_{ij}^\dagger = T_{ji} \Leftrightarrow T_{ij}^\dagger = T_{ji}^*$

$$D_\mu \bar{\psi}_a = \partial_\mu \bar{\psi}_a + ig (A_\mu \cdot T^*)_{ab} \bar{\psi}_b \text{ as well.}$$

$$\begin{aligned} \text{That is } \bar{\psi} \sigma^\mu (A_\mu \cdot T) \psi &= - \bar{\psi} (A_\mu \cdot T^\dagger) \sigma^\mu \psi \\ &= - \bar{\psi} (A_\mu \cdot T^*) \sigma^\mu \psi \end{aligned}$$

$$\begin{aligned} \text{So } \frac{i}{2} \bar{\psi} \sigma^\mu [\partial_\mu - ig (A_\mu \cdot T)] \psi &= - \frac{i}{2} [\partial_\mu \psi - ig \psi (A_\mu \cdot T^*)] \sigma^\mu \bar{\psi} \\ &\quad - \frac{i}{2} [\partial_\mu \bar{\psi} + ig \bar{\psi} (A_\mu \cdot T)] \sigma^\mu \psi \\ &= + \frac{i}{2} \bar{\psi} \sigma^\mu [\partial_\mu \bar{\psi} + ig (A_\mu \cdot T^*) \bar{\psi}] \end{aligned}$$

Hence

$$\frac{i}{2} \bar{\psi} \sigma^{\mu} \overleftrightarrow{D}_{\mu} \psi = + \frac{i}{2} \psi \sigma^{\mu} \overleftrightarrow{D}_{\mu}^{*} \bar{\psi}$$

where

$$D_{\mu}^{*} \psi = \partial_{\mu} \psi - ig \psi (A_{\mu} \cdot T)^{*}$$

$$D_{\mu}^{*} \bar{\psi} = \partial_{\mu} \bar{\psi} + ig \bar{\psi} (A_{\mu} \cdot T)^{*}$$

Or we can write the kinetic terms as

$$\begin{aligned} & \frac{i}{2} \bar{\psi} \sigma^{\mu} [\partial_{\mu} \psi - ig (A_{\mu} \cdot T) \psi] \\ & - \frac{i}{2} [\partial_{\mu} \bar{\psi} + ig \bar{\psi} (A_{\mu} \cdot T)] \sigma^{\mu} \psi \\ & = \frac{i}{2} \bar{\psi} \sigma^{\mu} [\partial_{\mu} \psi - ig (A_{\mu} \cdot T) \psi] \\ & + \frac{i}{2} \psi \sigma^{\mu} [\partial_{\mu} \bar{\psi} - ig (A_{\mu} \cdot (-T^{*})) \bar{\psi}] \end{aligned}$$

we see that if ψ is a representation d then $\bar{\psi}$ is representation d^{*} transforming with $-T^{*}$ instead of T .

$$\text{Since } [-T_i^{*}, -T_j^{*}] = [T_i^T, T_j^T]$$

$$= [T_j, T_i]^T = if_{jki} T_k^T$$

$$= -if_{ikj} T_k^T = if_{ijk} (-T_k^{*})$$

any rep. T_i then also $(-T_i^{*})$ is a rep. (d^{*})

Hence we can list the Kähler terms for the MSSM using this general result.

First recall all the matter superfields:

<u>Superfield</u>	<u>SMF field</u>	<u>spartner</u>	<u>(3, 2, 1)</u>
$L_m = \begin{pmatrix} \nu_m \\ e_m \end{pmatrix}$	$l_{mL} = \begin{pmatrix} \nu_{mL} \\ e_{mL} \end{pmatrix}$	$\tilde{l}_m = \begin{pmatrix} \tilde{\nu}_m \\ \tilde{e}_m \end{pmatrix}$	$(1, 2, -\frac{1}{2})$

$Q_m^a = \begin{pmatrix} u_m^a \\ d_m^a \end{pmatrix}$	$q_{mL}^a = \begin{pmatrix} u_{mL}^a \\ d_{mL}^a \end{pmatrix}$	$\tilde{q}_m^a = \begin{pmatrix} \tilde{u}_m^a \\ \tilde{d}_m^a \end{pmatrix}$	$(3, 2, +\frac{1}{6})$
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E_m^c	$e_{mL}^c = e_{mL}^+$	\tilde{e}_m^c	$(1, 1, +1)$
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U_m^{ca}	u_{mL}^{ca}	\tilde{u}_m^{ca}	$(\bar{3}, 1, -\frac{2}{3})$
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D_m^{ca}	d_{mL}^{ca}	\tilde{d}_m^{ca}	$(\bar{3}, 1, +\frac{1}{3})$
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H_u	$H_u = \begin{pmatrix} H_u^+ \\ H_u^0 \\ H_u^- \end{pmatrix}$	\tilde{H}_u	$(1, 2, +\frac{1}{2})$
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H_d	$H_d = \begin{pmatrix} H_d^0 \\ H_d^- \end{pmatrix}$	\tilde{H}_d	$(1, 2, -\frac{1}{2})$
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(Recall: $\mathbb{F}_D = \begin{pmatrix} 2 \\ \bar{3} \end{pmatrix}$; $\mathbb{F}_L = \begin{pmatrix} 2 \\ 0 \end{pmatrix}$; $\mathbb{F}_R = \begin{pmatrix} 0 \\ \bar{3} \end{pmatrix}$)
 (also $Q = T_3 + Y$)

Let the "left" fields be Weyl: $\psi_L = \psi$; $e_L = e$ etc.
 Suppress L everywhere

So we see that the Kähler terms will be quite lengthy; in order to simplify integrate by parts so that the fermion KE becomes

$$\frac{i}{2} \bar{\psi} \gamma^\mu \overleftrightarrow{D}_\mu \psi \rightarrow i \bar{\psi} \gamma^\mu D_\mu \psi$$

with $D_\mu \psi = \partial_\mu \psi - ig (A_\mu \cdot T) \psi$

So we find for the MSSM

$$\mathcal{L}_K = \bar{F}_{2m} F_{2m} + \bar{F}_{em} F_{em} + \bar{F}_{2m}^a F_{2m}^a + \bar{F}_{dm}^a F_{dm}^a$$

$$+ \bar{F}_{ecm} F_{ecm} + \bar{F}_{ucm}^a F_{ucm}^a + \bar{F}_{dcm}^a F_{dcm}^a$$

$$+ \bar{F}_u^+ F_u^+ + \bar{F}_u^0 F_u^0 + \bar{F}_d^0 F_d^0 + \bar{F}_d^- F_d^-$$

$$\begin{aligned} & - g_1 D_1 \left[-\frac{1}{2} \tilde{L}_m^+ \tilde{L}_m^+ - \frac{1}{2} \tilde{e}_m^+ \tilde{e}_m^+ + \frac{1}{6} \tilde{u}_m^+ \tilde{u}_m^+ \right. \\ & \quad \left. + \frac{1}{6} \tilde{d}_m^+ \tilde{d}_m^+ + \tilde{e}_m^+ \tilde{e}_m^+ - \frac{2}{3} \tilde{u}_m^+ \tilde{u}_m^+ \right. \\ & \quad \left. + \frac{1}{3} \tilde{d}_m^+ \tilde{d}_m^+ + \frac{1}{2} H_u^+ H_u^+ - \frac{1}{2} H_d^+ H_d^+ \right] \end{aligned}$$

$$\begin{aligned} & - g_2 D_2 \left[\tilde{L}_m^+ \frac{\sigma^i}{2} \tilde{L}_m^+ + \tilde{q}_m^+ \frac{\sigma^i}{2} \tilde{q}_m^+ \right. \\ & \quad \left. + H_u^+ \frac{\sigma^i}{2} H_u^+ + H_d^+ \frac{\sigma^i}{2} H_d^+ \right] \end{aligned}$$

(let $F=1,2,3$ family index instead of 'm' if confusion)

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$$- g_3 D_3^m \left[\begin{array}{l} \tilde{q}_F^+ \frac{\lambda^m}{2} \tilde{q}_F - \tilde{u}_F^+ \frac{\lambda^m}{2} \tilde{u}_F^c \\ - \tilde{d}_F^+ \frac{\lambda^m}{2} \tilde{d}_F^c \end{array} \right]$$

$$+ \sqrt{2} g_1 \left[\begin{array}{l} \tilde{l}_F^+ \tilde{B} \tilde{l}_F + \frac{1}{6} \tilde{q}_F^+ \tilde{B} \tilde{q}_F^a \\ - \frac{1}{2} \tilde{l}_F \tilde{B} \tilde{l}_F + \frac{1}{6} \tilde{q}_F^a \tilde{B} \tilde{q}_F^a \end{array} \right]$$

$$+ e_m^+ \tilde{B} e_m^c + \bar{e}_m^c \tilde{B} \bar{e}_m^c$$

$$- \frac{2}{3} \tilde{u}_F^+ \tilde{B} \tilde{u}_F^c - \frac{2}{3} \bar{u}_F^c \tilde{B} \bar{u}_F^c$$

$$+ \frac{1}{3} \tilde{d}_F^+ \tilde{B} \tilde{d}_F^c + \frac{1}{3} \bar{d}_F^c \tilde{B} \bar{d}_F^c$$

$$+ \frac{1}{2} \tilde{H}_u^+ \tilde{B} \tilde{H}_u + \frac{1}{2} \bar{H}_u \tilde{B} \bar{H}_u$$

$$- \frac{1}{2} \tilde{H}_d^+ \tilde{B} \tilde{H}_d - \frac{1}{2} \bar{H}_d \tilde{B} \bar{H}_d \left. \right]$$

$$+ \sqrt{2} g_2 \left[\begin{array}{l} \tilde{l}_F^+ (\tilde{A}^i \frac{\sigma_i}{2}) \tilde{l}_F + \bar{l}_F (\tilde{A}^i \frac{\sigma_i}{2}) \bar{l}_F \end{array} \right]$$

$$+ \tilde{q}_F^+ (\tilde{A}^i \frac{\sigma_i}{2}) \tilde{q}_F^a + \bar{q}_F^a (\tilde{A}^i \frac{\sigma_i}{2}) \bar{q}_F^a$$

$$+ \tilde{H}_u^+ (\tilde{A}^i \frac{\sigma_i}{2}) \tilde{H}_u + \bar{H}_u (\tilde{A}^i \frac{\sigma_i}{2}) \bar{H}_u$$

$$+ \tilde{H}_d^+ (\tilde{A}^i \frac{\sigma_i}{2}) \tilde{H}_d + \bar{H}_d (\tilde{A}^i \frac{\sigma_i}{2}) \bar{H}_d \left. \right]$$

$$\begin{aligned}
& + \frac{1}{2} g_3 \left[\tilde{g}_F^\dagger \left(\tilde{G}^m \frac{\lambda^m}{2} \right) \tilde{g}_F + \bar{\tilde{g}}_F \left(\tilde{G}^m \frac{\lambda^m}{2} \right) \tilde{g}_F \right. \\
& \quad - \tilde{u}_F^\dagger \left(\tilde{G}^m \frac{\lambda^m}{2} \right) \tilde{u}_F - \bar{\tilde{u}}_F \left(\tilde{G}^m \frac{\lambda^m}{2} \right) \tilde{u}_F \\
& \quad \left. - \tilde{d}_F^\dagger \left(\tilde{G}^m \frac{\lambda^m}{2} \right) \tilde{d}_F - \bar{\tilde{d}}_F \left(\tilde{G}^m \frac{\lambda^m}{2} \right) \tilde{d}_F \right]
\end{aligned}$$

$$\begin{aligned}
& + i \bar{\tilde{l}}_F \bar{\sigma}^\mu D_\mu \tilde{l}_F + i \bar{\tilde{q}}_F \bar{\sigma}^\mu D_\mu \tilde{q}_F \\
& + i \bar{e}_F^\dagger \bar{\sigma}^\mu D_\mu e_F^\dagger + i \bar{\tilde{u}}_F^\dagger \bar{\sigma}^\mu D_\mu \tilde{u}_F^\dagger \\
& + i \bar{\tilde{d}}_F^\dagger \bar{\sigma}^\mu D_\mu \tilde{d}_F^\dagger + i \tilde{H}_u \bar{\sigma}^\mu D_\mu \tilde{H}_u \\
& + i \tilde{H}_d \bar{\sigma}^\mu D_\mu \tilde{H}_d
\end{aligned}$$

$$\begin{aligned}
& + (D_\mu \tilde{l}_F)^\dagger (D^\mu \tilde{l}_F) + (D_\mu \tilde{q}_F)^\dagger (D^\mu \tilde{q}_F) \\
& + (D_\mu e_F^\dagger)^\dagger (D^\mu e_F^\dagger) + (D_\mu \tilde{u}_F^\dagger)^\dagger (D^\mu \tilde{u}_F^\dagger) \\
& + (D_\mu \tilde{d}_F^\dagger)^\dagger (D^\mu \tilde{d}_F^\dagger) + (D_\mu \tilde{H}_u)^\dagger (D^\mu \tilde{H}_u) \\
& + (D_\mu \tilde{H}_d)^\dagger (D^\mu \tilde{H}_d)
\end{aligned}$$

where the covariant derivatives are given by

$$D_\mu l_F = \left[\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu + \frac{ig_1}{2} B_\mu \right] l_F$$

$$D_\mu \tilde{l}_F = \left[\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu + \frac{ig_1}{2} B_\mu \right] \tilde{l}_F$$

$$D_\mu g_F^{ab} = \left[\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu - \frac{ig_1}{6} B_\mu \right. \\ \left. - \frac{ig_3}{2} (\vec{\lambda} \cdot \vec{G}_\mu)_{ab} \right] g_F^{ab}$$

$$D_\mu \tilde{g}_F^{ab} = \left[\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu - \frac{ig_1}{6} B_\mu \right. \\ \left. - \frac{ig_3}{2} (\vec{\lambda} \cdot \vec{G}_\mu)_{ab} \right] \tilde{g}_F^{ab}$$

$$D_\mu e_F^c = (\partial_\mu - ig_1 B_\mu) e_F^c$$

$$D_\mu \mathcal{U}_F^{ab} = \left[(\partial_\mu + \frac{2i}{3} g_1 B_\mu) \delta^{ab} + \frac{ig_3}{2} (\vec{\lambda} \cdot \vec{G}_\mu)_{ab}^* \right] \mathcal{U}_F^{ab}$$

$$D_\mu d_F^{ab} = \left[(\partial_\mu - \frac{i}{3} g_1 B_\mu) \delta^{ab} + \frac{ig_3}{2} (\vec{\lambda} \cdot \vec{G}_\mu)_{ab}^T \right] d_F^{ab}$$

$$D_\mu \tilde{e}_F^c = (\partial_\mu - ig_1 B_\mu) \tilde{e}_F^c$$

$$D_\mu \tilde{\mathcal{U}}_F^{ab} = \left[(\partial_\mu + \frac{2i}{3} g_1 B_\mu) \delta^{ab} + \frac{ig_3}{2} (\vec{\lambda} \cdot \vec{G}_\mu)_{ab}^T \right] \tilde{\mathcal{U}}_F^{ab}$$

$$D_\mu \tilde{d}_F^{ab} = \left[(\partial_\mu - \frac{i}{3} g_1 B_\mu) \delta^{ab} + \frac{ig_3}{2} (\vec{\lambda} \cdot \vec{G}_\mu)_{ab}^T \right] \tilde{d}_F^{ab}$$

$$D_\mu H_u = \left(\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu - \frac{ig_1}{2} B_\mu \right) H_u$$

$$D_\mu H_d = \left(\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu + \frac{ig_1}{2} B_\mu \right) H_d$$

$$D_\mu \tilde{H}_u = \left(\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu - \frac{ig_1}{2} B_\mu \right) \tilde{H}_u$$

$$D_\mu \tilde{H}_d = \left(\partial_\mu - \frac{ig_2}{2} \vec{\sigma} \cdot \vec{A}_\mu + \frac{ig_1}{2} B_\mu \right) \tilde{H}_d$$

Quite a few terms!!

Finally we have the soft-SUSY breaking terms

$$\mathcal{L}_{\text{BK}} = - \sum_F^{\text{qt}} m_{LFG}^2 \tilde{l}_G - F_{LF}^{\dagger} m_{LFG} \tilde{l}_G - \sum_F^{\text{qt}} \bar{m}_{LFG} F_{LF}$$

$$- \sum_F^{\text{qt}} m_{gFG}^2 \tilde{g}_G - F_g^{\dagger} m_{gFG} \tilde{g}_G - \sum_F^{\text{qt}} \bar{m}_{gFG} F_g$$

$$- \sum_F^{\text{qt}} m_{ec}^2 \tilde{e}^c - F_{ec}^{\dagger} m_{ec} \tilde{e}^c - \sum_F^{\text{qt}} \bar{m}_{ec} F_{ec}$$

$$- \sum_F^{\text{qt}} m_{uc}^2 \tilde{u}^c - F_{uc}^{\dagger} m_{uc} \tilde{u}^c - \sum_F^{\text{qt}} \bar{m}_{uc} F_{uc}$$

$$- \sum_F^{\text{qt}} m_{dc}^2 \tilde{d}^c - F_{dc}^{\dagger} m_{dc} \tilde{d}^c - \sum_F^{\text{qt}} \bar{m}_{dc} F_{dc}$$

$$- m_{H_u}^2 H_u^{\dagger} H_u - M_{KH_u}^{\dagger} F_{H_u}^{\dagger} H_u - \bar{m}_{KH_u} H_u^{\dagger} F_{H_u}$$

$$- m_{H_d}^2 H_d^{\dagger} H_d - M_{KH_d}^{\dagger} F_{H_d}^{\dagger} H_d - \bar{m}_{KH_d} H_d^{\dagger} F_{H_d}$$