Observation of Quantum Interference and Coherent Control in a Photochemical Reaction

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Coherent control of reactants remains a long-standing challenge in quantum chemistry. In particular, we have studied laser-induced molecular formation (photoassociation) in a Raman-dressed spin-orbit-coupled $^{87}$Rb Bose-Einstein condensate, whose spin quantum state is a superposition of multiple bare spin components. In contrast to the notably different photoassociation-induced fractional atom losses observed for the bare spin components of a statistical mixture, a superposition state with a comparable spin composition displays the same fractional loss on every spin component. We interpret this as the superposition state itself undergoing photoassociation. For superposition states induced by a large Raman coupling and zero Raman detuning, we observe a nearly complete suppression of the photoassociation rate. This suppression is consistent with a model based upon quantum destructive interference between two photoassociation pathways for colliding atoms with different spin combinations. This model also explains the measured dependence of the photoassociation rate on the Raman detuning at a moderate Raman coupling. Our work thus suggests that preparing atoms in quantum superpositions may represent a powerful new technique to coherently control photochemical reactions.

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Quantum coherent control of atomic processes has been a significant triumph of atomic, molecular, and optical physics. Extending such coherent control to molecular processes is an active and interesting research area. In particular, the study of coherent control of photochemical molecular processes has focused on light-based control or control of the initial and final quantum states (for reviews see Refs. [1–4]). Theoretical studies have concerned both the manipulation of light parameters, such as the pulse trains, polarization, relative phases, etc., [5–12] and the initial or final quantum states [13]. Experimentally, tailored light pulses have been shown to control isomerization, photoassociation (PA), and photodissociation [14–21]. However, there is much lesser experimental study of influencing molecular processes by coherently controlling the reactants. Such a difficulty can arise from incoherent population in many scattering states due to finite experimental temperatures or an incomplete understanding of the quantum molecular processes.

In this work, we explore the following question: What happens in a chemical reaction if the reactants are prepared in quantum superposition states? Here we report spin-dependent PA experiments using a $^{87}$Rb Bose-Einstein condensate (BEC). Photoassociation [22] is a light-assisted chemical process where two atoms absorb a photon while scattering, and bind into an excited molecule. Our Bose-Einstein condensates are at ultracold temperatures and populate only a small number of scattering channels. In our experiment, we have prepared atoms in spin-momentum quantum superposition states, and a pair of such atoms can couple to an excited molecular state simultaneously through two atomic scattering channels. These two channels of different spin combinations both contribute to the coupling, but with opposite sign due to opposite Clebsch-Gordan (CG) coefficients. The relative amplitudes of the two contributions depend on the superposition state. The spin portion of a representative scattering state is shown in Fig. 1(a), along with the relevant molecular potential energy curves plotted against the internuclear separation $R$ in units of Bohr radius $a_0$ [23]. Our system exploits the intrinsic quantum nature of PA and our tunable superposition states of the reactant atoms allows us to observe a nearly total suppression of the molecular formation, thus representing a significant step forward for coherent chemistry.

Our experiment begins with a $^{87}$Rb BEC of $\sim 1.5 \times 10^4$ atoms in the $f = 1$ hyperfine state, which is produced via all optical evaporation in a cross-beam optical dipole trap created by a 1550 nm laser [24]. The trap has a characteristic trap frequency $\tilde{\omega} = (\omega_x, \omega_y, \omega_z)^{1/3} \sim 2\pi \times (140 \times 140 \times 37)^{1/3} \text{Hz} = 2\pi \times (90) \text{Hz}$. Tuning the magnetic field during the evaporation can lead to a BEC with bare $m_f = -1, 0, +1$ spin state, or a statistical mixture of all three.
band structures for Raman coupling quasimomentum along $\hbar$ photon recoil momentum of the Raman lasers with wave-states and mechanical momenta: the scattering state as that of various pairs of atoms (the position coefficients are denoted $C_{+i}$, $C_{0i}$, and $C_{-i}$; red, blue, and green represent $m_f = -1$, 0, and $+1$, respectively. The nonzero CG coefficients for the $|F = 0, m_f = 0\rangle$ component of the various pairs of bare spins in the scattering state are shown near the thin black arrows. (b) Laser geometry. Two Raman lasers with angular frequencies $\omega_R + \Delta \omega_R$ and $\omega_R$ propagate along $\hat{x}$ and $\hat{y}$ and have linear polarizations along $\hat{x}$ and $\hat{z}$. The frequency difference between the Raman beams $\Delta \omega_R/2\pi$ is 3.5 MHz. A PA laser propagates in the $x$-$z$ plane (due to spatial constraints) and has a linear polarization with components along all three axes. (c) Atomic energy diagram. A Zeeman bias magnetic field, $|\vec{B}_{\text{Bias}}| \approx 5$ G is used to tune the Raman detuning $\delta$. (d) Dressed band structures for Raman coupling $\Omega_R = 0$, 1.1, 3.2, 8.0, and 12$\Delta E_r$, all with $\delta = 0$. Dots represent BECs adiabatically loaded to the band minima at $q = 0$. Panels (a) to (c) are not to scale.

After preparing a bare BEC in spin state $m_f = 0$, we can load the BEC into a spin-momentum superposition by adiabatically applying a pair of counterpropagating Raman beams with wavelengths near 790.17 nm, see Fig. 1(b). The Raman beams couple the $m_f$ states, as shown in Fig. 1(c), and “dress” the atoms into superpositions of the $m_f$ spin states and mechanical momenta: $\sum_{i=1}^{3} C_i |m_f,p\rangle = C_{-1}|-1,\hat{h}(q + 2k_r)\rangle + C_{0}|0,hq\rangle + C_{+1}|+1,\hat{h}(q - 2k_r)\rangle$, where $p$ and $hq$ are the mechanical momentum and quasimomentum along $\hat{y}$, respectively, $\hbar k_r$ is the single photon recoil momentum of the Raman lasers with wavelengths near 790.17 nm, and $\hbar$ is the reduced Planck’s constant. The quasimomentum is the canonical momentum conjugate of the position along $y$. For more details of our setup, see Refs. [25,26]. Our Raman coupling scheme is largely similar to previous works [27,28]. The Hamiltonian for the Raman light-atom interaction is

$$
\mathcal{H} = \begin{pmatrix}
\frac{\hbar^2}{2m}(q + 2k_r)^2 - \delta & \Omega_R \frac{\hbar}{2} & 0 \\
\Omega_R \frac{\hbar}{2} & \frac{\hbar^2}{2m}q^2 + \epsilon_q & 0 \\
0 & 0 & \frac{\hbar^2}{2m}(q - 2k_r)^2 + \delta
\end{pmatrix},
$$

where $m$ is the $^{87}\text{Rb}$ mass, $\delta$ is the Raman detuning, $\Omega_R$ is the Raman coupling (calculated from the measured frequency of resonant Raman-Rabi oscillations), $E_r = \hbar^2 k_r^2/2m = \hbar \times (3.68 \text{ kHz})$ is the recoil energy, and $\epsilon_q = 0.65 E_r$ is the quadratic Zeeman shift. Unless otherwise stated, $\Omega_R$ and $\delta$ carry uncertainties of 10% and $\pm 0.5E_r$, respectively. The eigenstates of Eq. (1) are the “dressed” spin-momentum superposition states described above. The $q$-dependent eigenenergies of the atoms form the dressed bands, with a few representative examples shown in Fig. 1(d). Red, blue, and green colors reflect the proportion of $m_f = -1$, 0, and $+1$ in the spin-momentum superposition state. The small dots represent the BECs adiabatically prepared at the band minimum. Such Raman coupling has been used previously to induce synthetic partial waves [29], modify an $s$-wave Feshbach resonance [30], and couple singlet and triplet scattering states [31].

After preparing our BEC in a statistical mixture or a spin-momentum superposition state, we apply a PA laser with wavelength 781.70 nm and typical intensity $I_{PA}$ of a few $\text{W/cm}^2$ for a time $t_{PA}$ of a few ms [32]. The frequency of the PA laser is tuned to the $(21)_g$ excited molecular state with vibrational quantum number 152 [see again Fig. 1(a)], and corresponds to the PA line $e$ in the Fig. 1 of Ref. [33]. After the PA pulse, the PA, Raman (in the case of the superposition state), and the dipole lasers are simultaneously switched off to allow the BEC to undergo 15 ms of time-of-flight (TOF) expansion. During the initial portion of this expansion, we use a Stern-Gerlach magnetic field gradient to separate atoms in the different $m_f$ spin states. At the end of the TOF expansion, we apply absorption-based imaging to extract the atom numbers in different spin-momentum projections. Then, this sequence is repeated at various PA frequencies to obtain a PA spectrum.

To extract the PA rate constant, $k_{PA}$, due to a PA process, we follow a procedure similar to those in Refs. [34,35]. The two-body rate equation describing the time-dependent BEC density of the atoms participating in PA, $\rho(t, \vec{r})$, is

$$
d\rho(t, \vec{r})/dt = -k_{PA}\rho^2(t, \vec{r}).$$

In our experiment, $\Gamma_{\text{stim}} \ll \Gamma_{\text{spon}}$ (where $\Gamma_{\text{stim}}$ and $\Gamma_{\text{spon}}$ are the stimulated and spontaneous emission rates, respectively), and $k_{PA}$ has a Lorentzian dependence with respect to the PA frequency [36].
Solving for $\rho(t, \vec{r})$ and spatially integrating it over a Thomas-Fermi BEC density profile yields an expression for the atom number, $N(\eta)$, remaining after a PA pulse,

$$N(\eta) = N_0 \frac{15}{2} \eta^{-5/2} \left\{ \eta^{1/2} + \frac{1}{3} \eta^{3/2} \right\} - \left( 1 + \eta \right)^{1/2} \text{tanh}^{-1}\left[ \sqrt{\eta/(1 + \eta)} \right],$$

where $\eta = k_{PA} \rho_0 \omega_{PA}$ is a dimensionless parameter indicating the strength of the PA pulse, $\rho_0$ is the peak atomic density at the center of the BEC, and $N_0$ is the off-resonant atom number with no PA loss. We denote the resonant $k_{PA}$ for a BEC composed of $m_f = 0$ bare spin (or spin-momentum superposition) states as $k_{0,0}$ (or $k_{sup}$).

First, as shown in Fig. 2, we compared the PA of BECs in a spin statistical mixture to that of BECs in a spin-momentum superposition state, with a nearly identical atom number and spin composition in the two cases. For the spin-momentum superposition state, we used $\Omega_R = 8.0 \omega_c$ and $\delta = 0 \omega_c$ [see also Fig. 1(d)]. In panels (a) and (b), we show the optical density (OD) images for PA both on and off resonance for the spin statistical mixture (a) and the spin-momentum superposition state (b). (c), (d): The extracted normalized atom number ($N(\eta)$) versus a spin-momentum superposition state (b). For the spin statistical mixture, the PA-induced loss for the $m_f = 0$ component is notably larger than that for the $m_f = \pm 1$ components. The lower reduction of the OD was due to the lower $\rho_0$ for the $m_f = \pm 1$ components and that each molecule formed by the PA process reduced the $m_f = 0$ atom number by two, but for $m_f = \pm 1$, only by one each. However, for PA on a spin-momentum superposition state, we observed comparable PA-induced loss among all three $m_f$ components. In panels (c) and (d), for each $m_f$ component and the total, we show the normalized atom number ($N/N_0$) at various PA detunings ($\Delta \nu_{PA}$) from the resonance for the statistical mixture (c) and the spin-momentum superposition state (d). Each PA spectrum for every $m_f$ component or the total was fitted to Eq. (2) to extract the appropriate $N_0$ and then normalized. The $N_0$ were $\sim (1.2, 7.0, 1.1) \times 10^3$ and $(1.5, 6.9, 1.3) \times 10^4$ for the ($m_f = -1, 0, +1$) components of the statistical mixture and superposition state, respectively. For the spin statistical mixture, $(79 \pm 2\%)$ of the $m_f = 0$ atoms were lost on resonance, but less than $\sim 25\%$ were lost for the $m_f = \pm 1$ components. For the dressed BECs, all $m_f$ components lost $(36 \pm 2\%)$. All the data were taken using PA pulses with identical parameters.

To further explore this phenomenon, we prepared BECs with atoms in several spin-momentum superposition (or $m_f = 0$ spin) states by using $\Omega_R = 0, 1.1, 3.2,$ and $12 \omega_c$ with $\delta = 0 \omega_c$ (or $\delta \sim 100 \omega_c$) and plotted the normalized PA spectra in Figs. 3(a)–3(d) using red squares (or black circles). With $\delta \sim 100 \omega_c$, the Raman beams did not dress the atoms into spin-momentum superposition states, and these BECs therefore remained in the $m_f = 0$ bare spin state and displayed comparable loss ($\sim 40\%$) for all $\Omega_R$. However, the loss for BECs in spin-momentum superpositions decreases with increasing $\Omega_R$. At $\Omega_R = 12 \omega_c$, no loss is apparent. For all the data in panels (a) to (d), we used comparable total off-resonant BEC atom numbers $N_0 \sim (1.1 \pm 0.1) \times 10^4$ and square PA pulses with $t_{PA} = 3.2$ ms and $I_{PA} = 6.0 \pm 0.7$ W/cm².

We also fitted photoassociation spectra measured with $\delta = 0$ (or $\delta \sim 100 \omega_c$) to Eq. (2) and extracted $k_{sup}$ (or $k_{0,0}$), and then plotted $k_{sup}/k_{0,0}$ in Fig. 3(e). We used PA pulses with $I_{PA} = 6.1 \pm 0.7$ W/cm² and $t_{PA}$ of 2–8 ms to induce a repeatable but unsaturated loss of (10–40%). Also included are solid bands, which are predictions for $k_{sup}/k_{0,0}$ derived as follows. The molecular hyperfine state excited by our chosen PA transition has total angular momentum $F = 1$ and nuclear spin $I = 1$, and only couples to a pair of colliding atoms (represented by subscripts $a$ and $b$ in the following) whose total angular momentum $|F = f_a + f_b, m_F = m_{f_a} + m_{f_b} \rangle = (0, 0)$. Using the single particle basis, $|f_a, m_{f_a}, f_b, m_{f_b}, \rangle, \ |F = 0, m_F = 0 \rangle = (|1, +1\rangle|1, -1\rangle + |1, -1\rangle|1, +1\rangle - |1, 0\rangle|1, 0\rangle)/\sqrt{3}$. Thus,
there are two allowed pathways for the PA transition (after accommodating the indistinguishability of bosons): one in which both atoms have $m_f = 0$ and another with atoms in $m_f = \pm 1$. Both pathways contribute to this PA process with opposite signs due to the opposite CG coefficients $\pm 1/\sqrt{3}$.

We note $k_{PA} \propto \langle \psi_{mol} | d \cdot \vec{E} | \psi_{scat} \rangle^2$ with a spin independent proportionality factor [37], where $|\psi_{scat}\rangle$ and $|\psi_{mol}\rangle$ are the total wave functions for the scattering state and molecular state, respectively, $\vec{E}$ is the electric field of the PA laser, and $d$ is the dipole operator. The spin portion of $|\psi_{scat}\rangle$ for two Raman dressed atoms (labeled by subscripts $a$ and $b$) is $\sum_{i=-1}^{+1} \sum_{j=-1}^{+1} C_i C_j |f = 1, m_f = i\rangle_a \otimes |f = 1, m_f = j\rangle_b$. Using the CG coefficients, the probability amplitude of the $|F = 0, m_F = 0\rangle$ component of the scattering wave function is therefore $(2C_{-1}C_{+1} - C_0^2)/\sqrt{3}$. We arrive at [38]

$$k_{sup}/k_{0,0} = |C_0^2| + 4|C_{-1}C_{+1}|^2 - 4\text{Re}[C_0^2C_{-1}^*C_{+1}^*].$$

(3)

FIG. 4. Normalized photoassociation rate, $k_{sup}/k_{0,0}$, for BECs at Raman detuning $\delta$ from $-2.5$ to $+2.5E_r$ with Raman coupling $\Omega_R = 5.4E_r$. The orange (blue) bands are theoretical predictions with (without) the destructive interference term in Eq. (3). The band boundaries reflect one standard deviation of the predicted values given our experimental uncertainties. Inset: Dressed band structures for $\Omega_R = 5.4E_r$ and $\delta = -2$, 0, and $2E_r$. The dots represent BECs prepared at the band minima.

Describing the entire superposition BEC with one PA rate constant $k_{sup}$ is supported by our observation in Fig. 3 that all the bare spin components of the superposition state display identical fractional losses. In the limit of $\Omega_R \to 0$ with $\delta = 0$, $k_{sup}/k_{0,0} \to 1$ since $C_0 \to 1$ and $C_{-1} = C_{+1} \to 0$. However, interestingly, $k_{sup}/k_{0,0} \to 0$ for large $\Omega_R$ because $C_0 \to 1/\sqrt{2}$ and $C_{-1} = C_{+1} \to 1/2$ [all the superposition coefficients $C_i$ can be calculated by diagonalizing Eq. (1)]. In this case the third term of Eq. (3) cancels the first two, thus no molecular formation is predicted even with resonant PA light. This happens despite PA being allowed on both channels for associating two $m_f = 0$ atoms and associating two $m_f = \pm 1$ atoms [see Fig. 1(a)]. This complete destructive interference comes from the opposite CG coefficients $\pm 1/\sqrt{3}$. In Fig. 3, and also later in Fig. 4, the orange (blue) bands are theoretical predictions from Eq. (3) that show the range of theoretical predictions resulting from our typical experimental uncertainties, including (excluding) the destructive interference effect,
the last term of Eq. (3). The nearly total suppression of $k_{\text{sup}}/k_{0,0}$ at large $\Omega_R$ with $\delta = 0E_r$ is consistent with the prediction of Eq. (3) with the destructive interference term.

We also studied PA on BECs prepared with $\Omega_R = 5.4E_r$ and $\delta$ from $-2.5$ to $+2.5E_r$. Figure 4 shows $k_{\text{sup}}/k_{0,0}$ vs $\delta$, measured using square PA pulses with $t_{\text{PA}} = 5.5$ ms and $I_{\text{PA}} = 5.7 \pm 0.2$ W/cm$^2$. The experimental error bars reflect the aggregate uncertainty of $k_{\text{sup}}/k_{0,0}$. The inset contains calculated band structures for $\delta = -2.0$ and $+2.5E_r$. Using $\delta$ beyond $\sim \mp 2E_r$ polarizes the dressed BEC into majority $m_f = \pm 1$ and collisions between such atoms do not contribute to the $|F = 0, m_F = 0\rangle$ channel. This is consistent with our observed $k_{\text{sup}}/k_{0,0} \rightarrow 0$ with increasing $|\delta|$. This suppression is again consistent with Eq. (3) because $C_0$ and one of $C_{\pm 1}$ vanish, predicting $k_{\text{sup}}/k_{0,0} \rightarrow 0$.

Atoms in spin-momentum superpositions are novel reactants, and thus PA of such atoms represents a new type of photochemistry. We interpret observing the same fractional loss on all components of a spin-momentum superposition state as an indication that it is the superposition state itself that undergoes PA. Further, the different total fractional loss between BECs of a spin statistical mixture and a spin-momentum superposition state demonstrates a significant modification to the PA process due to the coherent quantum superposition. Lastly, we interpret the nearly full suppression of $k_{\text{sup}}/k_{0,0}$ as resulting from destructive interference between the two out-of-phase pathways ($m_f = 0$, $m_F = 0$ and the $m_f = +1$, $m_F = -1$). Our scattering state simultaneously accesses these two pathways as it couples to the chosen excited molecular state. Thus our observations suggest that scattering states of atoms in quantum superpositions may offer a powerful new approach to coherently control photochemical reactions.

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[32] The beam waist of both the PA and the Raman lasers at the BEC location is about an order of magnitude larger than the in situ BEC size.
[38] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.121.073202 for a derivation of Eq. (3). In writing Eq. (3), we have ignored in the Franck-Condon factor the relative momentum imparted from the Raman beams. For the purpose of our PA resonance, this is justifiable since the length scale set by the wavelength of the Raman beams is \( \sim 1 \mu \text{m} \), but the length scale of the PA process is significantly shorter, less than 2 nm.