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Physics 220 - Exam #1

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This exam consist of 11 problems. Please check that you have them all.

Formules and constants:

$$v = v_0 + at$$

$$x = v_0 t + 0.5 at^2$$

$$v^2 = v_0^2 + 2ax$$

$$x = 0.5(v_0 + v)t$$

$$y = v_0 t + 0.5 at^2$$

$$v^2 = v_0^2 + 2ay$$

$$y = 0.5(v_0 + v)t$$

KEY

$$F = ma$$

$$F_{\text{gravity}} = G \frac{m_1 m_2}{r^2}$$

$$G = 6.67 \times 10^{-11} \text{ N m}^2/\text{kg}^2$$

$$\text{Mass of the Earth} = 5.98 \times 10^{24} \text{ kg}$$

$$\text{Radius of the Earth} = 6.38 \times 10^6 \text{ m}$$

$$\text{Mass of the Mars} = 6.43 \times 10^{23} \text{ kg}$$

$$\text{Radius of the Mars} = 3.37 \times 10^6 \text{ m}$$

$$g = -9.8 \text{ m/s}^2$$

1. Your car ($m = 1000 \text{ kg}$) has a dead battery, and is initially at rest. You want to push it so that it reaches a velocity of 1.25 m/s in 60 seconds. What is the force that you must exert on the car? The road is horizontal.

- (1) 24 N
- (2) 0.024 N
- (3) 9.8 N
- (4) 13,000 N
- (5) 48 N
- (6) 0.5 N
- (7) 10.0 N
- (8) 0.021 N
- (9) 4.9 N
- (10) 21 N

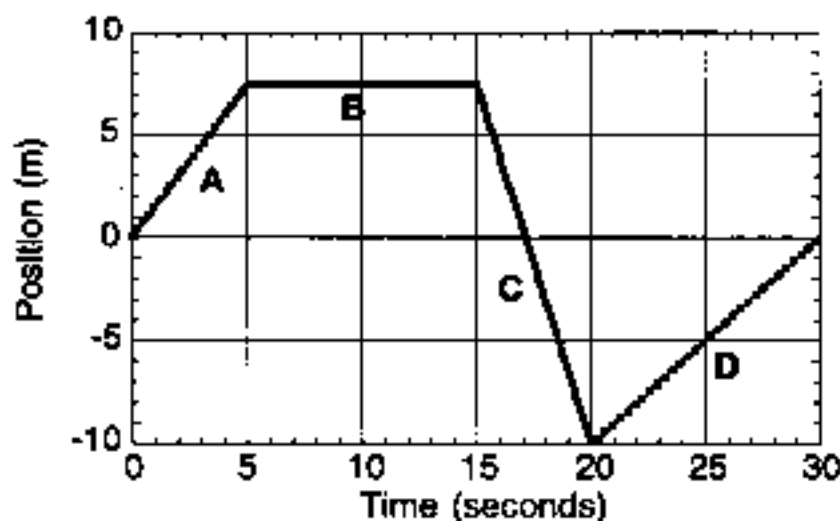
$$V = v_0 + at$$

$$a = \frac{v}{t} = \frac{1.25}{60} = 0.02083 \text{ m/s}^2$$

$$F = ma = 1000 \cdot 0.02083 = 20.83 \text{ N} \sim 21$$

2. A football is kicked at an angle θ with respect to the horizontal. Which one of the following statements best describes the acceleration of the football during this event if air resistance is neglected?

- (1) The acceleration is zero at all times.
- (2) The acceleration is 9.8 m/s^2 at all times.
- (3) The acceleration is zero when the football has reached the highest point in its trajectory.
- (4) The acceleration is positive as the football rises, and it is negative as the football falls.
- (5) The acceleration starts at 9.8 m/s^2 and drops to some constant lower value as the ball approaches the ground.
- (6) None of the above



Questions 3, 4 and 5 pertain to the graph shown above and is described as follow: An object is moving along the x axis. The graph shows its position from the starting point as a function of time. Various segments of the graph are identified by the letters A, B, C and D.

3. Which segment(s) of the graph represent(s) a constant velocity of $+1.0$ m/s?

- (1) A
- (2) B
- (3) C
- (4) D
- (5) E
- (6) A and C
- (7) A and D
- (8) C and D
- (9) A, C and D
- (10) B and D

4. What was the instantaneous velocity of the object at the end of the eighth second?

- (1) -0.94 m/s
- (2) 0 m/s
- (3) +0.94 m/s
- (4) 1.1 m/s
- (5) -1.1 m/s
- (6) 7.5 m/s
- (7) 9.8 m/s
- (8) 2.5 m/s
- (9) -2.5 m/s
- (10) -7.5 m/s

5. During which interval is the object moving the negative x direction?

- (1) during interval A only
- (2) during interval B only
- (3) during interval C only
- (4) during interval D only
- (5) during intervals A and C
- (6) during intervals B and C
- (7) during intervals C and D
- (8) during intervals B and D
- (9) during intervals A, C and D
- (10) during intervals B, C and D

6. A student is stranded on a raft (mass of man + raft = 600 kg). By paddling, he causes an average force of 17 N to be applied to the raft in the direction due East (positive x direction). The wind exerts a force of 15 N due West. At the moment the forces begin acting on the raft, the velocity of the raft is 0.18 m/s in the direction due East. Assuming the forces are maintained for 75 seconds, find the displacement of the raft. Ignore water resistance.

- (1) 48 m
 (2) 23 m
 (3) 53 m
 (4) 0.0033 m
 (5) 8400 m
 (6) 0.5 m
 (7) 1.5 m
 (8) 220 m
 (9) 9.8 m
 (10) 33 m

$$\sum F_x = m a_x$$

$$17 - 15 = 600 a$$

$$a_x = 0.003333$$

$$x = v_0 t + \frac{1}{2} a_x t^2$$

$$x = 0.18(75) + \frac{1}{2} 0.003333 (75)^2$$

$$x = 22.87 \sim 23 \text{ m}$$

7. A space probe weighs 5390 N on Earth and 2079 N on Mars. What is the acceleration due to gravity on Mars in m/s^2 ?

$$g_E = 9.8$$

$$m = \frac{W_E}{g_E}$$

$$m = \frac{W_M}{g_M}$$

$$g_M = \frac{W_M}{W_E} g_E = 3.78 \text{ m/s}^2$$

- (1) 0
 (2) 0.265
 (3) 1.61
 (4) 2.73
 (5) 3.78
 (6) 4.9
 (7) 5.70
 (8) 7.63
 (9) 9.8
 (10) 25.4

8. A football player kicks a football at an angle of 30° from the horizontal. The initial speed of the ball is 20 m/s. Ignore air resistance. Find the maximum height that the ball attains in meters.

- (1) 0
 (2) 10
 (3) 2.2
 (4) 9.8
 (5) 49
 (6) 0.033
 (7) 7.5
 (8) 2.5
 (9) 0.19
 (10) 5.1

$$V_0 = 20 \text{ m/s}$$

$$\theta = 30^\circ$$

$$V_y^2 = V_{0y}^2 + 2a_y y$$

$$y = \frac{V_y^2 - V_{0y}^2}{2a_y} = \frac{-(V_0 \sin 30^\circ)^2}{2(-9.8)} = 5.1 \text{ m}$$

$$\frac{V_0^2 \sin^2 \theta}{2g}$$

9. A communications satellite has a mass of 12,600 kg and orbits the Earth 600 km above the Earth's surface. Determine the weight (in Newtons) of the satellite in its orbit above the Earth's surface.

- (1) 0.951×10^5
 (2) 0
 (3) 1.23×10^4
 (4) 2.65×10^5
 (5) 0.0226×10^5
 (6) 5.65×10^5
 (7) 12.8×10^5
 (8) 0.84×10^5
 (9) 1.18×10^5
 (10) 1.03×10^5

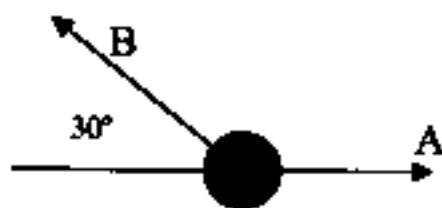
$$W = \frac{G M_E m_s}{(r_E + \text{orbit})^2}$$

$$W = \frac{6.67 \times 10^{-11} \times 5.98 \times 10^{24} \times 12,600}{(6.38 \times 10^6 + 600 \times 10^3)^2}$$

$$W = 1.03 \times 10^5$$

10. The only two forces acting on a 5.00 kg mass are indicated in the figure below as A and B. The magnitude of force A is 50 N. The magnitude of force B is 200 N. The directions of forces A and B are given in the figure. Determine the magnitude of the acceleration of the mass.

- (1) 40.0 m/s²
 (2) 24.6 m/s²
 (3) 41.2 m/s²
 (4) 48.8 m/s²
 (5) 31.7 m/s²
 (6) 20.0 m/s²
 (7) 44.7 m/s²
 (8) 30.0 m/s²
 (9) 9.8 m/s²
 (10) 12.2 m/s²



$$\vec{A} = 50 \hat{x}$$

$$\vec{B} = (200 \cos 30) \hat{x} + (200 \sin 30) \hat{y}$$

$$= -173.3 \hat{x} + 100 \hat{y}$$

$$\sum F_x = 50 - 173 = m a_x = 5 a_x$$

$$a_x = -24.6$$

$$\sum F_y = 100 = m a_y = 5 a_y$$

$$a_y = 20$$

$$a = \sqrt{a_x^2 + a_y^2} = 31.7 \text{ m/s}^2$$

11. You kick a soccer ball at a speed of 10.0 m/s off a 100 m high cliff. The initial velocity vector is 30° above the horizontal direction as the ball leaves your foot. Determine the time of flight of the ball.

$$v_0 = 10.0 \text{ m/s} \quad \theta = 30^\circ$$

$$y = -100 \text{ m}$$

$$y = v_0 t + \frac{1}{2} a t^2$$

$$\frac{1}{2} a_y t^2 + v_{0y} t - y = 0$$

$$\frac{1}{2} (-9.8) t^2 + v_0 (\sin 30) t + 100 = 0$$

$$t = 5.05 \text{ s}$$

- (1) 0 s
 (2) 4.03 s
 (3) 2.53 s
 (4) 2.01 s
 (5) 5.05 s
 (6) 0.065 s
 (7) 7.52 s
 (8) 10.2 s
 (9) 20.4 s
 (10) 9.69 s

The other solution $t = -4.03$ occurs prior to kickoff - so it doesn't apply.