

# Index

- $\chi^2$  test, 520, 523
- $\chi^2$  distribution, 521
- acoustic impedance, 384
- action potential, 437
- adaptive time step, 413
- adiabatic approximation, 29
- air drag, 21
- air drag at high altitudes, 30
- air drag, approximate theory, 22
- aliasing, 488
- amino acids, 390
- annealing, 402
- approach to equilibrium, 204, 279
- Arnoldi-Saad method, 537
- arrow of time, 204
- autocorrelation function, 490
- avalanche, 447
- banjo, 373
- barrier potential, 318
- baseball, batted, 32
- baseball, effect of wind, 34
- baseball, long home  
    runs, 35
- baseball, spin-dependent force, 38
- baseball, trajectory of a curveball, 36
- baseball, trajectory of a knuckleball, 42
- Bernoulli effect, 37
- bicycles, 18
- bifurcation, 67
- billiard problem, 82
- Biot-Savart law, 148
- bisection, 471
- blind ant, 230
- Boltzmann factor, 237
- brain models, 418
- breadth-first search method, 225
- cannon shell trajectory, 25
- canonical ensemble, 237
- cellular automata, 445
- cellular automata, game of *life*, 445
- centered difference methods, 464
- central limit theorem, 521
- chaos and noise, 89
- chaos, Feigenbaum  $\delta$ , 69
- chaos, pendulum, 60
- chaos, period doubling, 73
- chaos, sensitivity to initial conditions, 61
- chaos, strange attractors, 65
- chaotic motion of Hyperion, 123
- cluster growth, 206
- cluster labeling method, 220
- cluster, fractal dimensionality, 210
- coarse graining, 195
- correlation function, 255
- Crank-Nicholson method, 338
- cream-in-coffee problem, 182, 197
- critical exponents,  $\alpha$ , 253
- critical exponents,  $\beta$ , 243
- critical exponents,  $\gamma$ , 255
- critical phenomena and fluctuations, 257
- critical temperature, 241
- critical temperature, 2-D Ising model, 250
- data collapsing, 267
- data fitting, 493
- debugging and checking, 11
- depth-first search, 191
- derivative, finite difference form, 2
- detailed balance, 246
- diffusion, 131, 181, 185, 291
- diffusion and entropy, 203
- diffusion and fluctuations, 186
- diffusion and probability, 195
- diffusion constant, 184
- diffusion equation, 196
- diffusion limited aggregation, 206
- diffusion on a fractal, 229
- dimensionality of a cluster, 209
- Dirac delta function, 480
- discrete Fourier transform, 481
- dispersion, 171
- dynamical matrix, 374
- earthquakes, 407
- Eden model, 206
- eigenfunctions, 527
- eigenvalue problems, 304, 324, 373, 527

## 542 Index

- eigenvalue problems and random walks, 231
- eigenvalue problems, approximate methods, 537
- electric field, 135
- electric potential, 129
- energy landscape, 426
- entropy, 203
- equilibrium, 204
- equipartition, 279
- ergodic hypothesis, 204
- error, global, 457, 458
- error, local, 457, 458
- Euler method, 3, 20, 456
- Euler-Cromer method, 52, 97, 462
- exchange interaction, 237
- fast Fourier transform, 483
- Feigenbaum  $\delta$ , 69
- Fermi-Pasta-Ulam problem, 294
- ferromagnet, 236
- FFT, 483
- finite difference, first derivative, 2
- finite difference, fourth derivative, 170
- finite difference, second derivative, 157
- first-order phase transitions, 259
- fluctuation-dissipation theorem, 254, 255
- forest fire problem, 227
- Fourier analysis, 89, 165, 360
- Fourier transform, 479
- fractal clusters, 210
- fractal coastlines, 216
- fractal dimension, 210
- fractal dimensionality of a curve, 212
- free energy, 241
- free energy landscape, 401
- friction, 370, 409
- gas, dilute, 280
- Gauss-Jordan elimination, 530
- Gauss-Seidel method, 142, 534
- Gaussian quadrature, 504
- Gaussian elimination, 528
- general relativity, effect on mercury, 108
- generating fractal curves, 212
- genetic algorithms, 473
- golden mean, 471
- golf, 44
- golf ball, effect of dimples, 45
- graphing results, 10
- guitar, 357
- guitar string, 163
- guitar, standing waves, 359
- Gutenberg-Richter law, 406
- half-life, 2
- Halley’s comet, 100
- Hamming distance, 427
- Hebbian learning, 427
- Heisenberg model, 238
- Heisenberg uncertainty principle, 340
- Helmholtz motion, 368
- Hodgkin-Huxley model, 439
- homogeneous functions and scaling, 265
- Hoshen-Kopelman algorithm, 221
- hypercubic lattice, 184
- Hyperion, chaotic tumbling, 123
- hysteresis, 260
- initial value problem, 2
- integration, 500
- inverse square law, 101, 103
- ion channels, 438
- Ising model, 236
- Jacobi method, 131
- Kepler’s laws, 98
- Kirkwood gaps, 119
- Koch curve, 212
- Laplace’s equation, 129
- leapfrog method, 335, 383
- least squares, 494, 497
- least-squares fitting, 112
- Lennard-Jones potential, 273, 318, 327
- Levinthal’s paradox, 392
- linear congruent random number generator, 512
- linear regression, 494
- linear systems, 527
- logistic map, 70
- Lorenz butterfly, 81
- Lorenz model, 75
- LU decomposition, 531
- Lyapunov exponent, 62
- magnetic field of a solenoid, 152
- magnetic fields, 148
- magnetic fields and spin systems, 239

- magnetization, 238
- Magnus force, 37
- matrix method in quantum mechanics, 323
- Maxwell velocity distribution, 282
- mean field approximation, 240
- mean free path, 271
- melting, 285
- metastable states, 260, 400
- Metropolis algorithm, 245
- molecular dynamics, 270
- Monte Carlo integration, 506
- Monte Carlo method, 235, 244, 395, 423, 474
- multiple linear regression, 498
- neural networks, 418
- neural networks, Hopfield model, 434
- neuron, 418
- neurons and Ising spins, 421
- Newton-Cotes methods, 502
- Newton-Raphson method, 469
- nonlinear springs, 295
- normal distribution, 521
- normal modes, 296
- Nyquist frequency, 483
- octave stretching, 173
- optimization, 469, 472
- ordinary differential equations, 456
- parity, 308
- pendulum, chaotic, 58
- pendulum, damped and nonlinear, 54
- pendulum, driven, 55
- pendulum, simple, 48
- perceptron, 434
- percolation, 218
- percolation and phase transitions, 222
- percolation clusters, 218
- percolation clusters and fractals, 224
- percolation threshold, 219
- period doubling, 68, 73
- periodic boundary conditions, 249, 275
- phase diagrams, 261
- phase space, 62
- phase transition, 235
- piano, 362
- piano tone spectrum, 168
- planetary data, 97
- planetary orbits, 101
- planetary orbits, stability and the inverse square law, 103
- Poincaré section, 63
- Poisson’s equation, 144
- power laws, 243
- power method, 325
- power spectrum, 89, 165, 490
- precession of the perihelion of mercury, 108
- program listings, 4
- programming guidelines, 14
- programming languages, 3
- projectile motion, 18
- protein folding, 390
- proteins, primary structure, 390
- proteins, tertiary structure, 390
- pseudocode, 3
- Q factor, 387
- quantum mechanics, anharmonic oscillator, 322
- quantum mechanics, matching method, 315
- quantum mechanics, shooting method, 307
- quantum mechanics, two-dimensional harmonic oscillator, 329
- quantum mechanics, variational principle, 326
- quantum mechanics, variational-Monte Carlo method, 328
- quantum mechanics, wave packet spreading, 340
- radioactive decay, 1
- random number generators, 512
- random numbers, 183
- random numbers, nonuniform distributions, 516
- random numbers, quality tests, 514
- random numbers, rejection method, 517
- random numbers, transformation method, 516
- random systems, 181
- random walk, 182
- random walk in one dimension, 183
- recursion, 212
- regression, linear, 494
- regression, multiple linear, 498
- relaxation method, 131, 533

## 544 Index

- relaxation method, diffusion, 131
- resonance, 387
- Richardson’s formula, 503
- Romberg integration, 503
- root finding, 469
- round-off error, 12
- routes to chaos, intermittency, 80
- routes to chaos, period doubling, 68
- Runge-Kutta methods, 458
- sandpile, 447
- scaling, 264
- Schrödinger equation, Monte-Carlo methods, 328
- Schrödinger equation, time-dependent, 333, 345, 350
- Schrödinger equation, time-independent, 303
- Schrödinger equation, two-dimensional harmonic oscillator, 329
- Schrödinger equation, variational method, 326
- secant method, 471
- second order differential equations, 460
- second order phase transitions, 223
- second-order phase transitions, 243
- second-order transition, 260
- self-avoiding walk, 189
- self-organized criticality, 407, 448
- shooting method, 307, 309
- simple harmonic oscillator, 48
- Simpson’s rule, 502
- simulated annealing, 473
- simultaneous over-relaxation, 142
- solar system, 94
- spanning cluster, 218
- specific heat, 253
- spectral methods, 174, 350
- stadium billiard, 82
- staggered grid, 383
- step sizes, 13
- stick-slip motion, 370
- stochastic systems, 181
- Stokes’ law, 21
- strange attractor, 65
- susceptibility, 254
- Taylor expansion, 2
- three-body problem, 113
- time-dependent Schrödinger equation, 333
- time-dependent Schrödinger equation, spectral method, 350
- time-dependent Schrödinger equation, two dimensions, 345
- time-independent Schrödinger equation, 303
- trapezoidal rule, 502
- traveling salesman problem, 475
- triangular lattice, 287
- tunneling, 318
- turbulence, 75
- two-dimensional harmonic oscillator, 329
- unitarity, 337
- variational principle, 326
- Verlet method, 272, 463
- vibrating membrane, 373
- violin, 368
- virial theorem, 285
- viscosity, 24
- wave equation, 156, 359, 363
- wave equation and stability, 161
- wave equation for a stiff string, 170
- wave equation for sound, 383
- wave equation in two dimensions, 376
- wave equation, solution, 158
- wave packet, 339
- waves, 156
- waves on a string, 159
- waves, reflection, 162
- waves, spectral methods, 174
- XY model, 238