

Magnetic excitations in the high- T_c iron pnictides

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We calculate the expected finite frequency neutron-scattering intensity based on the two-sublattice collinear antiferromagnet found by recent neutron-scattering experiments as well as by theoretical analysis on the iron oxypnictide LaOFeAs. We consider two types of superexchange couplings between Fe atoms: nearest-neighbor coupling J_1 and next-nearest-neighbor coupling J_2 . We show how to distinguish experimentally between ferromagnetic and antiferromagnetic J_1 . Whereas magnetic excitations in the cuprates display a so-called resonance peak at (π, π) (corresponding to a saddlepoint in the magnetic spectrum), which is at a wave vector that is at least close to nesting Fermi-surface-like structures—no such corresponding excitations exist in the iron pnictides. Rather, we find saddlepoints near $(\pi, \pi/2)$ and $(0, \pi/2)$ (and symmetry related points), which are not close to nesting the Fermi surfaces.

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The recent discovery of superconductivity exceeding 50 K in a different class of materials holds tremendous potential for understanding the origin of high-temperature superconductivity.^{1–6} Similar to the cuprate superconductors, the iron pnictides also have a layered structure and display magnetism in the undoped parent compound.

Both become superconducting upon doping. And like the cuprates, the transition-metal layer is believed to play an important role in the superconducting pairing. On the other hand, the parent compound of LaOFeAs is a poor metal at room temperature as opposed to a correlated insulator as in the cuprates.

Initially band-structure calculations suggested that the materials are nonmagnetic but close to a strong magnetic instability.^{7–9} However, subsequent calculations have shown that the antiferromagnetic (AFM) state has lower energy than the nonmagnetic state because of Fermi-surface nesting.^{10–12} In Ref. 12, a stripe-like AFM ground state was suggested based on strong nesting effects. Recent neutron-scattering experiments¹³ have shown that the parent compound of FeOFeAs is a long-range ordered antiferromagnet with a type of spin stripe order [i.e., unidirectional spin-density wave (SDW)]. However, the magnetic moment was found to be $0.36(5)\mu_B$ per iron, which is much smaller than the calculated value of $\sim 2.3\mu_B$ per iron.^{10–12}

From an analysis of the superexchange interactions, Ref. 14 suggested that the next-nearest-neighbor interaction J_2 is AFM while the nearest-neighbor interaction J_1 is ferromagnetic (FM). However, a first-principles band-structure calculation predicts that the nearest-neighbor interaction is also AFM.^{15,16} They predict that $|J_2|$ is almost twice as large as J_1 . In both cases, the competition between J_1 and J_2 leads to a type of stripe-ordered two-sublattice AFM ground state (Fig. 1) when $|J_2/J_1|$ is larger than the critical value.^{17,18} While the interactions J_1 and J_2 can compete, the uniaxial SDW considered in Fig. 1 is a classical ground state of the system and it is thus not frustrated in the sense of having a macroscopic ground-state degeneracy.

We use linearized spin-wave theory to calculate the magnetic excitations and sublattice magnetization for the two-sublattice collinear antiferromagnet with nearest-neighbor superexchange coupling J_1 and AFM next-nearest-neighbor superexchange coupling J_2 . We present results for FM cou-

pling J_1 as well as for AFM coupling J_1 (see Fig. 1). We find that the results are quite different for the two cases, so that comparing our calculations with future neutron-scattering results at finite frequency will be able to distinguish these two cases.

The model Hamiltonian is described by the Heisenberg spin model on the square lattice,

$$H = J_1 \sum_{\langle ij \rangle_{nn}} \mathbf{S}_i \cdot \mathbf{S}_j + J_2 \sum_{\langle ij \rangle_{nnn}} \mathbf{S}_i \cdot \mathbf{S}_j, \quad (1)$$

where $\langle ij \rangle_{nn}$ and $\langle ij \rangle_{nnn}$ are the nearest-neighbor and next-nearest-neighbor spin pairs, respectively. There are two spins in each unit cell as shown in Fig. 1. We study the elementary excitations of the classical ground state of this model by using the well-known Holstein-Primakoff boson method. The dispersion and intensities are calculated by quantizing the classical spin waves.

We use Holstein-Primakoff bosons to quantize about the collinear AFM ground state found in recent neutron scattering,¹³

$$H = E_{Cl} + S \sum_{\mathbf{k}} \left[A_{\mathbf{k}} a_{\mathbf{k}}^+ a_{\mathbf{k}} + \frac{1}{2} (B_{\mathbf{k}} a_{\mathbf{k}}^+ a_{-\mathbf{k}}^+ + B_{-\mathbf{k}}^* a_{\mathbf{k}} a_{-\mathbf{k}}) \right], \quad (2)$$

where $E_{Cl} = -2J_2NS^2$ is the classical ground-state energy and

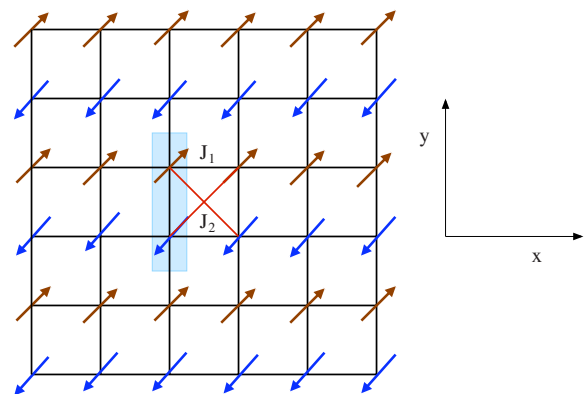


FIG. 1. (Color online) Two-sublattice collinear antiferromagnet on the Fe-square lattice. Shaded region is the magnetic unit cell.

$$A_{\mathbf{k}} = (4J_2 + 2J_1 \cos k_x), \quad (3)$$

$$B_{\mathbf{k}} = (2J_1 \cos k_y + 4J_2 \cos k_x \cos k_y). \quad (4)$$

We can diagonalize the Hamiltonian using the Bogoliubov transformation

$$b_{\mathbf{k}} = \cosh \theta_{\mathbf{k}} a_{\mathbf{k}} - \sinh \theta_{\mathbf{k}} a_{-\mathbf{k}}^\dagger. \quad (5)$$

The diagonalized Hamiltonian is

$$H = \sum_{\mathbf{k}} \omega(\mathbf{k}) b_{\mathbf{k}}^\dagger b_{\mathbf{k}} + E_{\text{Cl}} + E_0, \quad (6)$$

where $\omega(\mathbf{k})$ is the spin-wave dispersion

$$\omega(\mathbf{k}) = S \sqrt{A_{\mathbf{k}}^2 - B_{\mathbf{k}}^2}, \quad (7)$$

and E_0 is the quantum zero-point energy correction

$$E_0 = \frac{S}{2} \sum_{\mathbf{k}} [-A_{\mathbf{k}} + \omega(\mathbf{k})]. \quad (8)$$

For $|J_1|=1$ and $J_2=2$, we get $E_0 = -0.332NS$.

We find that there is only one spin-wave band,

$$\begin{aligned} \omega(k_x, k_y) \\ = 2S \sqrt{(2J_2 + J_1 \cos k_x)^2 - (J_1 \cos k_y + 2J_2 \cos k_x \cos k_y)^2}. \end{aligned} \quad (9)$$

The associated spin-wave velocities are

$$v_x = 2S \sqrt{-J_1^2 + 4J_2^2}, \quad (10)$$

$$v_y = 2S |J_1 + 2J_2|. \quad (11)$$

Notice that v_x becomes imaginary for $|J_1| > 2|J_2|$, indicating a change in the classical ground-state configuration.

Figure 2 shows the spin-wave band with the nearest-neighbor coupling both AFM [Fig. 2(a)] and FM [Fig. 2(b)]. The presence of saddlepoints can be seen—we will return to this point later. In addition, because the (π, π) point is a magnetic reciprocal-lattice vector, the dispersion must have $\omega \rightarrow 0$ at this point, although as we will see there is no zero-frequency intensity associated with this part of the dispersion. This precludes finite frequency weight at the (π, π) point from this band.

We calculate the zero-temperature dynamic structure factor using the same method,^{19,20}

$$S(\mathbf{k}, \omega) = \sum_f \sum_{i=x,y,z} |\langle f | S^i(\mathbf{k}) | 0 \rangle|^2 \delta(\omega - \omega_f). \quad (12)$$

Here $|0\rangle$ is the magnon vacuum state and $|f\rangle$ denotes the final state of the spin system with excitation energy ω_f . S^z does not change the number of magnons contributing to the elastic part of the structure factor. $S^x(\mathbf{k})$ and $S^y(\mathbf{k})$ contribute to the inelastic dynamic structure factor through single magnon excitations.

In Figs. 3 and 4, we show the expected neutron-scattering intensity for constant-energy cuts in $\mathbf{k}$ space. We show our predictions from spin-wave theory for both FM and AFM J_1 . Figure 3 shows the expected neutron-scattering intensity

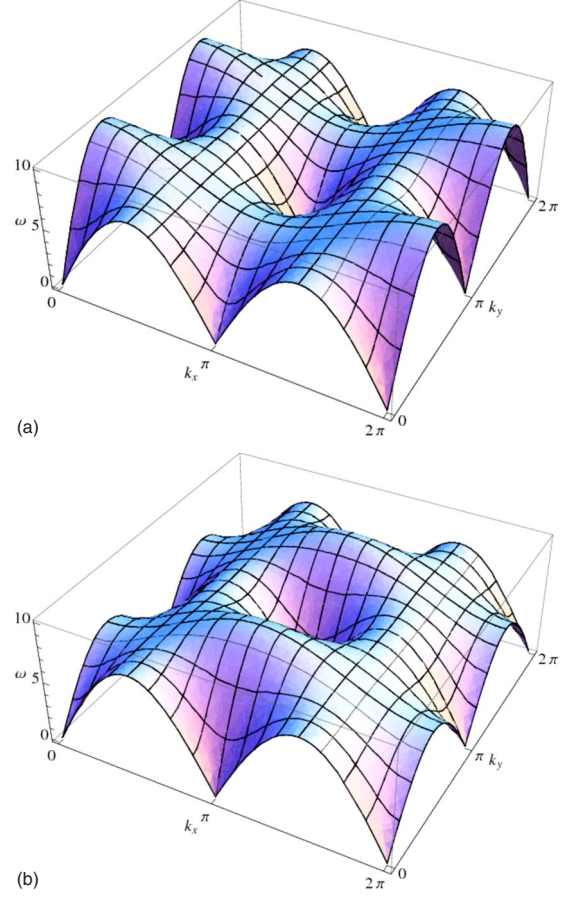


FIG. 2. (Color online) Spin-wave dispersion band for the two-sublattice collinear antiferromagnet shown in Fig. 1. (a) Here, both couplings are antiferromagnetic. Here we have set $J_1=1$ (AFM) with $J_2=2$ (AFM). (b) Dispersion with ferromagnetic nearest-neighbor coupling. Here we have set $J_1=-1$ (FM) with $J_2=2$ (AFM).

from a single domain of the magnetic order (i.e., for an untwinned case) and Fig. 4 shows the expected scattering intensity for the case where there is an equal contribution from domains with both orientations of the magnetic order (i.e., for a twinned case).

For FM J_1 (at a low frequency), the strongest diffraction peaks are located at $(0, \pi)$ (see Fig. 3). However, more intensity weight shifts to $(\pi, 0)$ when J_1 is AFM. There is also a spin-wave cone emerging from (π, π) but the intensity is much weaker than the cones emanating from other magnetic reciprocal-lattice vectors, since zero-frequency weight is forbidden at (π, π) for the magnetic order we consider. At high energy, the difference between FM J_1 and AFM J_1 becomes more apparent. For example, for FM J_1 , there are two strong spots along the (π, k_y) direction, whereas for AFM J_1 , they are along the $(0, k_y)$ direction. In real materials, stripe order can be twinned due to a finite correlation length, local disorder pinning, or crystal twinning. Therefore, we show the twinned constant-energy cut plots in Fig. 4 for both FM and AFM nearest-neighbor coupling J_1 .

As can be seen from the dispersion in Fig. 2, there are saddlepoints in the spin-wave excitation spectrum at various points in k space. For the case of both couplings being AFM,

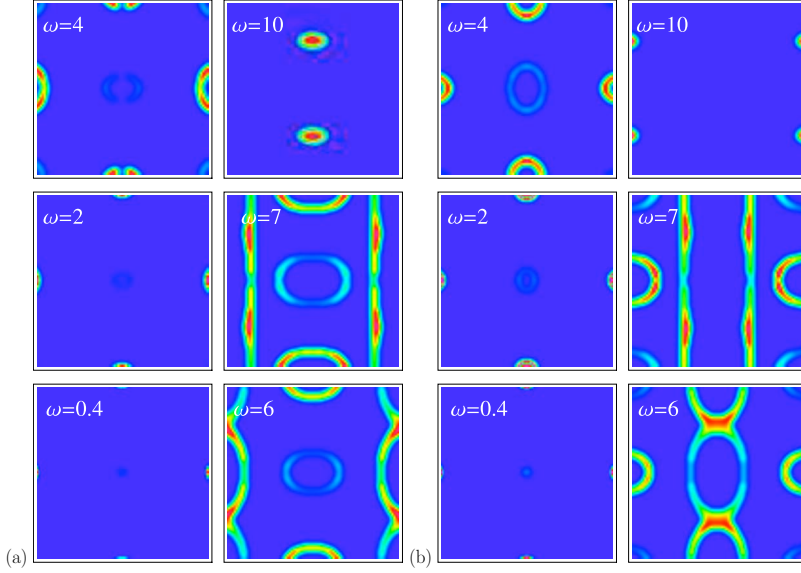


FIG. 3. (Color online) Constant-energy cuts (untwinned) of the dynamic structure factor $S(\mathbf{k}, \omega)$ for $J_2=2$ (AFM): (a) $J_1=-1$ (FM) and (b) $J_1=1$ (AFM). The x axis and y axis correspond to k_x and k_y , respectively, with the range $(0, 2\pi)$. We have integrated over an energy window of $\pm 0.2|J_1|S$.

these occur at $(\pi/2, 0)$ and $(\pi, \pi/2)$ and symmetry related points. For FM nearest-neighbor coupling, saddlepoints can be seen at $(0, \pi/2)$ along with weak saddlepoints possible at $(\pi/2, 0)$ and $(\pi/2, \pi)$ and symmetry related points. The integrated intensity is generally large at such saddlepoints. In the cuprates, the “resonance peak” is a saddlepoint in the magnetic excitations at (π, π) , which has been empirically connected to superconductivity, i.e., it increases in intensity at the onset of superconductivity. There has been much discussion concerning this scattering phenomenon in the cuprates, particularly because it is close to nesting vectors for the corresponding Fermi surface. However, in the case of the iron pnictides, the saddlepoints we find here are quite far from any nesting vectors.

Experimentally, the magnetic moment per iron was found to be $0.36(5)\mu_B$, which is much smaller than the expected value of $\sim 2.3\mu_B$ per iron site.^{10–12} The zero-point energy of the spin waves reduces the sublattice magnetization. It was suggested in Ref. 14 that the competition between J_1 and J_2

may be responsible for the small moment observed in the experiment. The sublattice magnetization m is defined as

$$m = \langle S_i^Z \rangle = S - \Delta m, \quad (13)$$

where Δm is the deviation of sublattice magnetization from the saturation value,

$$\Delta m = \langle a_i^+ a_i \rangle = \sum_{\mathbf{k}} \langle a_{\mathbf{k}}^+ a_{\mathbf{k}} \rangle = \frac{1}{2V_{\mathbf{k}}} \sum_{\mathbf{k}} \left[\frac{SA_{\mathbf{k}}}{\omega(\mathbf{k})} - 1 \right] + \frac{1}{V_{\mathbf{k}}} \sum_{\mathbf{k}} \frac{SA_{\mathbf{k}}}{\omega(\mathbf{k})} \frac{1}{e^{\beta\omega(\mathbf{k})} - 1} = \Delta m^{\text{quantum}} + \Delta m^{\text{thermal}}. \quad (14)$$

The first term $\Delta m^{\text{quantum}}$ comes from quantum zero-point fluctuations. The second term $\Delta m^{\text{thermal}}$ comes from the classical thermal fluctuation, which is divergent at any finite temperature in agreement with the Mermin-Wagner theorem. (The very presence of the broken symmetry observed in the

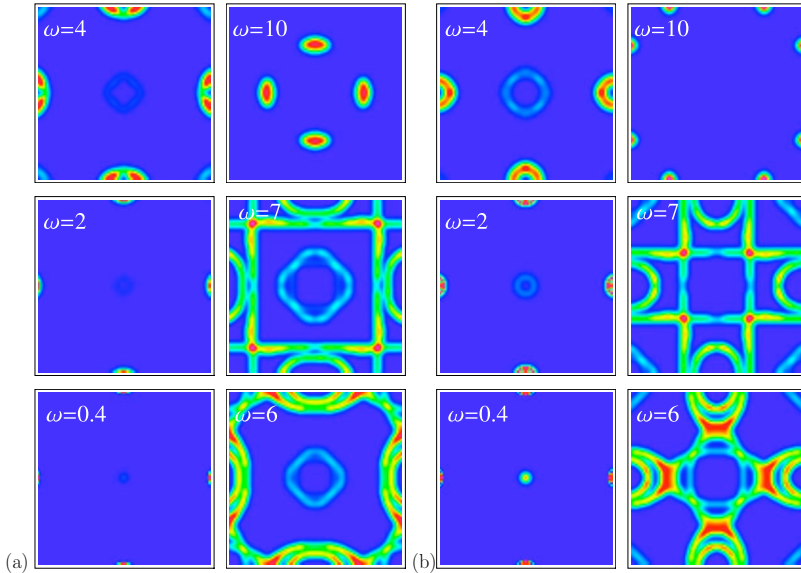


FIG. 4. (Color online) Constant-energy cuts (twinned) of the dynamic structure factor $S(\mathbf{k}, \omega)$ for $J_2=2$ (AFM): (a) $J_1=-1$ (FM) and (b) $J_1=1$ (AFM). The x axis and y axis correspond to k_x and k_y , respectively, with the range $(0, 2\pi)$. We have integrated over an energy window of $\pm 0.2|J_1|S$.

experiment implies that there is some finite coupling between planes, however weak.)

Here we calculate $\Delta m^{\text{quantum}}$ by

$$\Delta m^{\text{quantum}} = \frac{1}{2} \int_0^{2\pi} \int_0^{2\pi} \frac{dk_x dk_y}{2\pi} \frac{SA_k}{\omega(\mathbf{k})} - \frac{1}{2}. \quad (15)$$

It is difficult to get the analytical form of the integral. Thus, we numerically calculate $\Delta m^{\text{quantum}}$. From the symmetry, the above integral does not change when J_1 changes sign. In Fig. 5, $\Delta m^{\text{quantum}}$ is plotted as a function of the superexchange coupling ratio $|J_2/J_1|$. It is S independent. If S is in between 1 and $\frac{3}{2}$, it will reduce the m by 13%–20%. $\Delta m^{\text{quantum}}$ decreases with increasing J_2/J_1 because stronger J_2 stabilizes the two-sublattice collinear antiferromagnet state. This deviation is not sufficient to explain the observed value of the sublattice magnetization.

In conclusion, we have used spin-wave theory to calculate the magnetic excitations and sublattice magnetization for the two-sublattice collinear AFM state of the $\text{La}(\text{O}_{1-x}\text{F}_x)\text{FeAs}$ high- T_c superconductors. We have studied both FM and AFM nearest-neighbor coupling J_1 with AFM next-nearest-neighbor coupling J_2 . We calculate the predicted inelastic neutron-scattering pattern based on spin-wave theory. Comparison with future inelastic neutron-scattering studies can be used to distinguish the sign of J_1 . We find that the sublattice magnetization can be reduced by the zero-point motion of spin waves, although not enough to account for the small moments observed in the experiment. In addition, we identify several saddlepoints in the magnetic excitation spectrum. While magnetic excitations in these regions are expected to

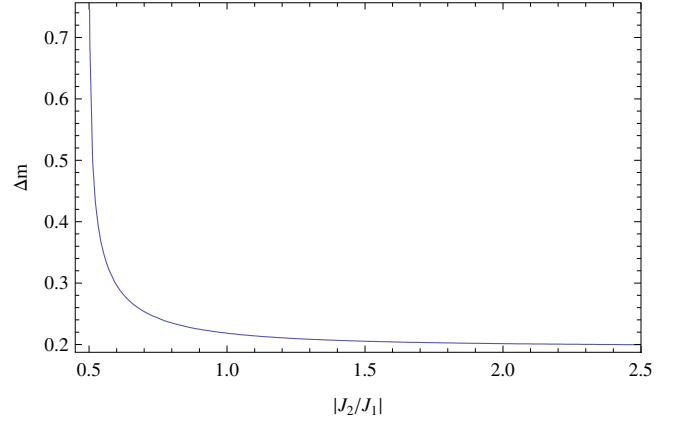


FIG. 5. (Color online) $|J_2/J_1|$ dependence of the reduction in the sublattice magnetization due to zero-point energy of the spin waves. Here we have used $|J_1|=1$.

have extra intensity due to the saddlepoint structure, these corresponding wave vectors are not near nesting vectors of the Fermi surface.

Note added. Some results from spin-wave calculations have also been reported by Ref. 21. In the latest version of Ref. 15, J_1 is claimed to be close to J_2 . A further consideration of the magnetic moment is given recently by Ref. 22.

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